

## UNIT NO 1 (FUNCTIONS AND LIMITS)

### I. CHOOSE THE CORRECT ANSWERS.

1. Domain of  $1/x$  is .....  
 (a)  $\mathbb{R}$  (b)  $\{0\} - \mathbb{R}$  (c)  $\mathbb{R} - \{0\}$  (d)  $\mathbb{N}$
2. If  $f(x) = 1/x$  then  $f^{-1} = \dots\dots\dots$   
 (a)  $x$  (b)  $1/x$  (c)  $1/x^2$  (d) None
3.  $y = \sqrt{x-1}$  is an ..... function  
 (a) Even (b) Explicit (c) Odd (d) Implicit
4.  $\operatorname{Cosec} h x = \dots\dots\dots$   
 (a)  $\frac{e^x - e^{-x}}{2}$  (b)  $\frac{2}{e^x - e^{-x}}$  (c)  $\frac{e^x + e^{-x}}{2}$  (d)  $\frac{2}{e^x + e^{-x}}$
5.  $\cos x$  is an ..... function.  
 (a) Explicit (b) Implicit (c) Odd (d) even
6. If  $f(x) = 1/x^2$   $g(x) = \sqrt{x}$  then  $f \circ g = \dots\dots\dots$   
 (a)  $\sqrt{x}$  (b)  $1/\sqrt{x}$  (c)  $x$  (d)  $1/x$
7.  $\lim_{x \rightarrow \infty} a/x = \dots\dots$  where  $a \in \mathbb{R}$   
 (a)  $a$  (b)  $x$  (c)  $\infty$  (d)  $0$
8.  $\lim_{h \rightarrow 0} (1+2h)^{1/h} = \dots\dots\dots$   
 (a)  $1$  (b)  $0$  (c)  $e$  (d)  $e^2$
9.  $\lim_{m \rightarrow \infty} (1+m)^{1/m} = \dots\dots\dots$   
 (a)  $e$  (b)  $0$  (c)  $\infty$  (d)  $e^m$

10.  $\lim_{\theta \rightarrow 0} \frac{\sin 7\theta}{\theta} = \dots\dots\dots$   
 (a) 7 (b)  $1/7$  (c) 0 (d)  $\infty$
11.  $\lim_{\theta \rightarrow 0} \frac{\cos \theta}{\theta} = \dots\dots\dots$   
 (a) 0 (b) 1 (c)  $\infty$  (d) None
12.  $\lim_{x \rightarrow 0} \frac{\sin x}{7x} = \dots\dots\dots$   
 (a) 1 (b) 7 (c)  $1/7$  (d) 0
13. If  $x = 10^y$  then  $y = \dots\dots\dots$   
 (a)  $\ln 10$  (b)  $\ln x$  (c)  $\ln 1$  (d)  $e$
14. If  $4^x = 1$  then  $x = \dots\dots\dots$   
 (a) 0 (b) 1 (c) 2 (d) 4
15. If  $2^x + 3^y = 13$  then  $x + y = \dots\dots\dots$   
 (a) 4 (b) 5 (c) 6 (d) 7
16.  $|x - 5| = x - 5$  If.....  
 (a)  $x = 5$  (b)  $x > 5$  (c)  $x < 5$  (d)  $x \geq -5$
17.  $\lim_{\theta \rightarrow 0} \frac{\sin \theta^0}{\theta} = \dots\dots\dots$   
 (a) 0 (b) 1 (c)  $\pi / 180$  (d)  $180/\pi$
18.  $\lim_{\theta \rightarrow 0} \frac{\theta}{\sin \theta} = \dots\dots\dots$   
 (a) Undefined (b) 0 (c) 1 (d) None

19. If  $3^x + 3^y = 3$  then  $x + y = \dots\dots\dots$
- (a) 0                      (b) 1                      (c) -1                      (d) 2
20. Tan x is an  $\dots\dots\dots$  function.
- (a) Even                      (b) Odd                      (c) Explicit                      (d) Implicit
21. Sin h x =  $\dots\dots\dots$
- (a)  $\frac{e^x + e^{-x}}{2i}$                       (b)  $\frac{e^x + e^{-x}}{2}$                       (c)  $\frac{e^x - e^{-x}}{2i}$                       (d)  $\frac{e^x - e^{-x}}{2}$
22.  $\lim_{x \rightarrow -\infty} \left[ \frac{1}{e^{-x}} \right]$
- (a) 0                      (b) 1                      (c)  $-\infty$                       (d)  $\infty$
23.  $\lim_{n \rightarrow \infty} (1 + 3/n)^{2n} = \dots\dots\dots$
- (a) e                      (b)  $e^2$                       (c)  $e^4$                       (d)  $e^6$
24. ln x is not defined at  $x = \dots\dots\dots$
- (a) 0                      (b) 1                      (c) e                      (d) None
25. If  $f(x, y) = 0$  then f is called an  $\dots\dots$  function.
- (a) Even                      (b) Odd                      (c) Explicit                      (d) Implicit

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## SHORT QUESTIONS

1. Show that the parametric equation  $x = a \cos t$  and  $y = a \sin t$  represent the Circle  $x^2 + y^2 = a^2$ .
2. Prove that  $\cos^2 x - \sin^2 x = 1$
3. Determine whether  $f(x) = x^{2/3} + 6$  is even or odd.
4. If  $f(x) = (-x + 9)^3$ ; verify  $f[f^{-1}(x)] = f^{-1}[f(x)] = x$
5. Show that  $\lim_{x \rightarrow a} \frac{x^n - a^n}{x - a} = n a^{n-1}$
6. Show that  $\lim_{x \rightarrow 0} \frac{\sqrt{x+a} - \sqrt{a}}{x} = \frac{1}{2\sqrt{a}}$
7. Evaluate  $\lim_{x \rightarrow 3} \frac{x - 3}{(\sqrt{x} - \sqrt{3})}$
8. Show that  $\lim_{x \rightarrow \infty} (1 + 1/n) = e$  where  $2 < e < 3$
9. Show that  $\lim_{x \rightarrow 0} \frac{a^x - 1}{x} = \ln a$
10. Evaluate  $\lim_{x \rightarrow \infty} (1 + 3/n)^{2n}$
11. Evaluate  $\lim_{x \rightarrow a} \frac{x^n - a^n}{x^m - a^m}$
12. Evaluate  $\lim_{x \rightarrow 0} \frac{\sin x}{x}$

13. Evaluate Limit  $\frac{\sin x}{\pi - x}$   
 $x \rightarrow \pi$
14. Evaluate Limit  $\frac{\tan \theta - \sin \theta}{\sin^3 \theta}$   
 $\theta \rightarrow 0$
15. Evaluate Limit  $(1 - 1/n)^n$   
 $n \rightarrow \infty$
16. Evaluate Limit  $(1 + 3x)^{2/3}$   
 $x \rightarrow 0$
17. Evaluate Limit  $[x / (1 + x)]^x$   
 $x \rightarrow \infty$
18. Evaluate Limit  $\frac{e^{1/x} - 1}{e^{1/x} + 1}$  ;  $x < 0$   
 $x \rightarrow 0$
19. Evaluate Limit  $\frac{e^{1/x} - 1}{e^{1/x} + 1}$  ;  $x > 0$   
 $x \rightarrow 0$
20. Evaluate Limit  $\sqrt{x+h} - \sqrt{x}$   
 $h \rightarrow 0$

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## UNIT # 2

### DERIVETIVES

1.  $\frac{d}{dx}(x^0) = \dots\dots\dots$   
 (a) Zero            (b)  $x$             (c)  $x^0$             (d) One
2. The notation  $dy/dx$  used by Mathematician.....  
 (a) Newton        (b) Leibnitz        (c) Lagrange        (d) Cauchy
3. Derivative of  $x^2$  w.r .t  $x$  at  $x = 1$  is .....  
 (a) 1                (b) 2                (c)  $2x$                 (d) None
4. Derivative of  $7^x$  w.r.t  $x$  is .....  
 (a)  $7^x$                 (b)  $7^x \ln x$         (c)  $7^x \ln 7$         (d)  $7^x / \ln 7$
5. Derivation of  $x^a$  w.r.t  $x$  is .....  
 (a)  $x^a \ln a$         (b)  $x^a \ln x$         (c)  $x^a / \ln a$         (d)  $ax^{a-1}$
6.  $\frac{d}{dx} \text{Sin}x^2 = \dots\dots\dots$   
 (a)  $2 \text{Sin}x \text{Cos}x$         (b)  $\text{Cos}x^2$         (c)  $2x\text{Cos}x^2$         (d)  $2\text{Sin}x$
7.  $\frac{d}{dx} \text{Cos}^2x = \dots\dots\dots$   
 (a)  $-\text{Sin}2x$         (b)  $2\text{Cos}x$         (c)  $\text{Sin}^2x$         (d) None
8.  $f$  is increasing on  $(a, b)$  if  $f'(x) \dots\dots\dots 0$   
 (a)  $<$                 (b)  $>$                 (c)  $=$                 (d)  $\leq$

9.  $\frac{d}{dx} (\ln e^x) = \dots\dots\dots$   
 (a)  $1/e^x$  (b)  $e^x \ln e$  (c) 1 (d)  $\ln e^x$
10.  $\frac{d}{dx} (\ln x^2) = \dots\dots\dots$   
 (a)  $1/x^2$  (b)  $2/x^2$  (c)  $1/x$  (d)  $2/x$
11.  $d/dx \sin \sqrt{x} = \dots\dots\dots$   
 (a)  $\cos \sqrt{x}$  (b)  $(1/2\sqrt{x}) / \cos \sqrt{x}$   
 (c)  $1/2x \cos \sqrt{x}$  (d)  $\cos \sqrt{x} / \sqrt{x}$
12.  $d/dx (\sin^{-1} x) = \dots\dots\dots$   
 (a)  $-\sin^{-2} x \cos x$  (b)  $-\sin x \cos x$   
 (c)  $1/\sqrt{x^2 - 1}$  (d)  $1/\sqrt{1 - x^2}$
13.  $d/dx (\tan^{-1} x) = \dots\dots\dots$   
 (a)  $1/(x^2 + 1)$  (b)  $1/\sqrt{x^2 + 1}$   
 (c)  $1/\sqrt{x^2 - 1}$  (d)  $1/(x^2 - 1)$
14.  $d/dx x^e = \dots\dots\dots$   
 (a)  $e^x$  (b)  $\ln x^e$  (c)  $e x^{e-1}$  (d)  $x^{e-1}$
15. A function of has Max value if // (c) ..... 0 at  $x = c$   
 (a)  $>$  (b)  $<$  (c)  $=$  (d)  $\leq$
16.  $d/dx \cos hx = \dots\dots\dots$   
 (a)  $\sin hx$  (b)  $-\sin hx$  (c)  $h \sin hx$  (d)  $-h \sin hx$

17.  $\frac{d}{dx} \operatorname{Sin h}^{-1} x = \dots\dots\dots$
- (a)  $1/(x^2 + 1)$  (b)  $1/\sqrt{x^2 + 1}$  (c)  $-1/(x^2 + 1)$  (d)  $1/(x^2 - 1)$
18.  $1 + ax + a^2 x^2/2! + a^3 x^3/3! + \dots\dots\dots$  is the expansion of .....
- (a)  $e^{ax}$  (b)  $e^{a/x}$  (c)  $e^{x/a}$  (d)  $ae^x$
19.  $-x - x^2/2 - x^3/3 - \dots\dots\dots$  is the..... of .....
- (a)  $\log(-x-1)$  (b)  $\log(x-1)$  (c)  $\log(1-x)$  (d)  $\log(x+1)$
20. Hundredth derivative of  $e^{-x}$  is .....
- (a)  $1/100 e^{-x}$  (b)  $100 e^{-x}$  (c)  $e^{-x}$  (d)  $e^{-100x}$
21.  $d/dx \operatorname{Cot}^{-1} x$  is.....
- (a)  $(1/(x^2 + 1))$  (b)  $-1/(x^2 + 1)$  (c)  $1/(x^2 - 1)$  (d)  $1/(1-x^2)$
22.  $d/dx \operatorname{Sin hx} = \dots\dots\dots$
- (a)  $(e^x + e^{-x})/2$  (b)  $(e^x - e^{-x})/2$  (c)  $(e^{-x} - e^x)/2$  (d) None
23.  $d/dx (x^x) = \dots\dots\dots$
- (a)  $x \ln x$  (b)  $x^x \ln x$  (c)  $x^x$  (d) None
24.  $d/dx (\sqrt{x + \sqrt{x}}) = \dots\dots\dots$
- (a)  $(1/2) \sqrt{x + \sqrt{x}}$  (b)  $(1/2) (x + \sqrt{x})$   
 (c)  $1/2 (\sqrt{x + x})$  (d) None
25.  $d/dt (1/t) = \dots\dots\dots$
- (a)  $-1/t$  (b)  $1/t^2$  (c)  $1$  (d)  $-1/t^2$

## SHORT QUESTIONS

1. Find the derivative of  $x^n$  by ab – initial method
2. Find  $dy / dx$  from first Principle's if  $y = 1 / (\sqrt{x + a})$
3. If  $y = x^4 + 2x^2 + 2$ , Prove that  $dy / dx = 4x \sqrt{y - 1}$
4. Differentiate  $\frac{x^2 + 1}{x^2 - 1}$  w.r.t  $\frac{x - 1}{x + 1}$
6. Show that  $d / dx (\operatorname{Cosec}^{-1} x) = 1 / (x \sqrt{x^2 - 1})$
7. If  $x = a \cos^3 \theta$ ;  $y = b \sin^3 \theta$ , show that  $a \cdot dy / dx + b \tan \theta = 0$
8. Find  $dy / dx$  if  $y = x \cos y$ .
9. Find the derivative of  $a^{\sqrt{x}}$  w. r . t  $x$
10. Show that  $\operatorname{Sin}^{-1} x = \ln (x + \sqrt{x^2 + 1})$
11. Prove that  $e^{x+h} = e^x \left\{ 1 + h + \frac{h^2}{2!} + \frac{h^3}{3!} + \dots \right\}$
12. Show that  $2^{x+h} = 2^x \{ 1 + (\ln 2) h + (\ln 2)^2 h^2 + \dots \}$
13. Show that  $y = \ln x / x$  has maximum value at  $x = 1/e$
14. Show that  $y = x^x$  has minimum value at  $x = 1/e$ .
15. Divide 20 into two parts so that the sum of their squares will be minimum.
16. Use differentials to approximate the value of  $\operatorname{Sin} 61^\circ$ . X.

## UNIT # 3 INTEGRATION

1.  $\int \ln x \, dx = \dots\dots\dots$   
 (a)  $1/x$  (b)  $1/x \ln x$  (c)  $1/x \log_{10} x$  (d) None
2.  $\int e^{ax+b} \, dx = \dots\dots\dots$   
 (a)  $(1/a) e^{ax+b}$  (b)  $(1/b) e^{ax+b}$  (c)  $ae^{ax+b} + c$  (d)  $e^{ax+b}$
3.  $\int 3^{dx+\mu} \, dx = \dots\dots\dots$   
 (a)  $3^{dx+\mu}$  (b)  $1/d 3^{dx+\mu}$  (c)  $\frac{3^{dx+\mu}}{d \ln 3} + c$  (d)  $3^{dx+\mu} \ln 3$
4.  $\int \tan x \, dx = \dots\dots\dots$   
 (a)  $\ln \sin x$  (b)  $\ln \cos x$  (c)  $\sec^2 x$  (d)  $\ln \sec x + c$
5.  $\int \cot x \, dx = \dots\dots\dots$   
 (a)  $\ln \cos x + c$  (b)  $\ln \sin x + c$  (c)  $\operatorname{CoSec}^2 x + c$  (d) None
6.  $\int \sin^{-1} x \, dx = \dots\dots\dots$   
 (a)  $\cos^{-1} x + c$  (b)  $1/\sqrt{1-x^2} + c$   
 (c)  $-1/\sqrt{1-x^2} + c$  (d)  $1/\sqrt{x^2-1} + c$
7.  $\int_a^b \ln x \, dx = \dots\dots\dots$   
 (a)  $\ln a - \ln b$  (b)  $\ln b - \ln a$  (c)  $\ln a + \ln b$  (d) None
8.  $\int e^x (\sin x + \cos x) \, dx = \dots\dots\dots$   
 (a)  $e^x \sin x + c$  (b)  $e^x \cos x + c$  (c)  $e^x \ln \sin x + c$  (d) None

9.  $\int \frac{dx}{x^2+4} = \dots\dots\dots$

- (a)  $\tan^{-1}(x/4) + c$       (b)  $\tan^{-1}(x/2) + c$   
 (c)  $\frac{1}{4} \tan^{-1}(x/4)$       (d)  $\frac{1}{2} \tan^{-1}(x/2) + c$

10.  $\int (ax + b) / \sqrt{ax^2 + 2bx + c} dx = \dots\dots\dots$

- (a)  $\frac{1}{2} \sqrt{ax^2 + 2bx + c}$       (b)  $\sqrt{ax^2 + 2bx + c} + d$   
 (c)  $\ln \sqrt{ax^2 + 2bx + c}$       (d)  $\frac{1}{2} \ln \sqrt{ax^2 + 2bx + c} + d$

11.  $\int \cos h k x dx = \dots\dots\dots$

- (a)  $\sin h k x + c$       (b)  $-\sin h k x + c$   
 (c)  $\frac{\sin h k x}{h k}$       (d)  $\frac{\sin h k x}{k} + c$

12.  $\int \sin h k x dx = \dots\dots\dots$

- (a)  $\cos h k x + c$       (b)  $-\cos h k x + c$   
 (c)  $\frac{\cos h k x}{h k}$       (d)  $\frac{\cos h k x}{k} + c$

13.  $\int 1/x dx = \dots\dots\dots$

- (a)  $\ln x + c$       (b)  $-1/x + c$       (c)  $-1/x^2 + c$       (d) None

14.  $\int k \cdot dx = \dots\dots\dots$

- (a)  $k + c$       (b)  $kx + c$       (c) Zero      (d)  $k$

15.  $\int dx / (x \ln x) = \dots\dots\dots$

- (a)  $1/x + c$       (b)  $1 / \ln x + c$       (c)  $\ln (\ln x) + c$       (d)  $\ln x + c$

16.  $\int e^{\sin x} \cdot \cos x \, dx = \dots\dots\dots$   
 (a)  $e^{\cos x} + c$       (b)  $e^{\sin x} + c$   
 (c)  $\frac{e^{\cos x}}{\sin x} + c$       (d)  $\frac{e^{\sin x}}{\cos x} + c$
17.  $\int \sqrt{e^x} \, dx = \dots\dots\dots$   
 (a)  $\sqrt{e^x} + c$       (b)  $e^x + c$       (c)  $\frac{1}{2} \sqrt{e^x} + c$       (d)  $2 \sqrt{e^x} + c$
18.  $\int dx / (x^2 - a^2) = \dots\dots\dots$   
 (a)  $\frac{1}{2} a \cdot \ln(x + a / x - a) + c$       (b)  $-1/2a \cdot \ln(x - a / x + a) + c$   
 (c)  $1/2a \cdot \ln(x - a / x + a) + c$       (d)  $+ 1/2a \ln(a - x / a + x) + c$
19.  $\int dx / (a^2 - x^2)$   
 (a)  $1/2a \ln(a - x / a + x) + c$       (b)  $1/2a \ln(a + x / a - x) + c$   
 (c)  $-1/2a \ln(a + x / a - x)$       (d) None
20.  $\int dx / (x^2 + a^2) = \dots\dots\dots$   
 (a)  $\tan^{-1}(x/a) + c$       (b)  $\tan^{-1}(a/x) + c$   
 (c)  $1/a \tan^{-1}(x/a)$       (d) None
21.  $\int dx / \sqrt{x^2 + a^2} = \dots\dots\dots$   
 (a)  $1/a \operatorname{Sin h}^{-1} x$       (b)  $1/a \operatorname{Sinh}^{-1}(x/a)$   
 (c)  $\operatorname{Sinh}^{-1}(x/a) + c$       (d)  $\operatorname{Cosh}^{-1}(x/a) + c$
22.  $\int dx / \sqrt{x^2 - a^2} = \dots\dots\dots$   
 (a)  $1/a \operatorname{Cosh}^{-1}(x/a) + c$       (b)  $\operatorname{Cosh}^{-1}(x/a) + c$   
 (c)  $\operatorname{Cosh}^{-1}(a/x) + c$       (d)  $\operatorname{Sinh}^{-1}(x/a)$

23.  $\int dx / \sqrt{a^2 - x^2} = \dots\dots\dots$
- (a)  $1/a \sin^{-1}x + c$       (b)  $1/a \sin^{-1}(x/a)$
- (c)  $1/a \sin^{-1}(a/x)$       (d)  $\sin^{-1}(x/a) + c$
24.  $\int \ln ax / x dx = \dots\dots\dots$
- (a)  $\ln ax + c$       (b)  $\ln ax / a + c$
- (c)  $(\ln ax)^2 / 2 + c$       (d)  $(\ln ax)^2 + c$
25.  $\int_a^b 1/x dx = \dots\dots\dots$
- (a)  $\ln a - \ln b$       (b)  $\ln b - \ln a$
- (c)  $1/b - 1/a$       (d)  $1/a - 1/b$
26. Solution of diff: equation.  $dy / dx = 1$  is:
- (a)  $x - y = c$       (b)  $y / x = c$
- (c)  $x / y = c$       (d)  $x + y = c$

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## SHORT QUESTION

1. Use differential to approximate the value of  $\sin 61^\circ$

2. Evaluate  $\int \frac{dx}{\sqrt{3}(\sqrt{x+1})}$ .

3. Evaluate  $\int \frac{ax+b}{ax^2+2bx+c}$

4. Evaluate  $\int \operatorname{Cosec} x \, dx$

5. Evaluate  $\int \frac{\operatorname{Cot} \sqrt{x}}{\sqrt{x}} \, dx$

6. Find  $\int ax^2 \cdot x \, dx$ .

7. Evaluate  $\int \frac{x+b}{\sqrt{x^2+2bx+c}} \, dx$

8. Evaluate  $\int \frac{\cos x \cdot \ln \sin x}{\sin x} \, dx$ .

9. Evaluate  $\int \frac{2a}{x^2-a^2} \, dx$ .

10. Evaluate  $\int \frac{2a}{a^2-x^2} \, dx$ .

11. Evaluate  $\int_{-1}^2 (x+|x|) \, dx$ .

12.  $\int_{-1}^5 |x-3| dx.$

13. Evaluate  $\int_{1/8}^1 \left( \frac{x^{1/3} + 2}{x^{2/3}} \right) dx$

14. Find the area bounded by Cos function from  $x = -\pi / 2$  to  $x = \pi / 2$

15. Solve the differential equation  $\frac{dy}{dx} + \frac{2xy}{2y+1}$

16. Solve the differential equation  $\sec x + \tan y \frac{dy}{dx}$

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## UNIT # 4

### ANALYTIC GEOMETRY

1. Slope of vertical line is .....
  - (a) Zero (b) Undefined (c) One (d) None
2. Gradient of horizontal line is.....
  - (a) Zero (b) Undefined (c) One (d) None
3. Slope of the line  $2y + x + 3 = 0$  is .....
  - (a) 2 (b) -2 (c)  $\frac{1}{2}$  (d)  $-\frac{1}{2}$
4. Y- intercept of the line  $5x + \sqrt{5}y + \sqrt{5} = 0$  is .....
  - (a)  $\sqrt{5}$  (b)  $-\sqrt{5}$  (c) 5 (d) -1
5. L, is horizontal iff  $m = \dots\dots\dots$ 
  - (a) 0 (b) 1 (c) -1 (d)  $\infty$
6. L, is vertical iff  $m = \dots\dots\dots$ 
  - (a) 0 (b) 1 (c) -1 (d)  $\infty$
7. If slope of AB = Slope o BC then A, B and C are.....
  - (a) Concurrent (b) Collinear (c) Coplanar (d) None
8. Two lines  $l_1$  and  $l_2$  with slopes  $m_1$  and  $m_2$  are parallel if  $m_1 - m_2 = \dots\dots\dots$ 
  - (a) 0 (b) 1 (c) -1 (d)  $\infty$
9. Two lines are perpendicular If  $1 + m_1m_2 = \dots\dots\dots$ 
  - (a) -1 (b) +1 (c) 0 (d)  $\infty$

10. Equation of x – axis is .....
- (a)  $x = 0$  (b)  $y = 0$  (c)  $x - y = 0$  (d)  $x + y = 0$
11. Equation of y – axis is .....
- (a)  $x = 0$  (b)  $y = 0$  (c)  $x + y = 0$  (d)  $x - y = 0$
12. If a line intersects x – axis at  $(a, 0)$  then a is called .....
- (a) a – intercept (b) x – intercept  
(c) y – intercept (d) None
13. P lies above the line if  $ax_1 + by_1 + c \dots\dots\dots 0$
- (a)  $>$  (b)  $<$  (c)  $=$  (d)  $\leq$
14. P lies below the line if  $ax_1 + by_1 + c \dots\dots\dots 0$
- (a)  $=$  (b)  $>$  (c)  $<$  (d)  $\geq$
15. P  $(2, -1)$  line ....., the line  $3x + 7y + 15 = 0$
- (a) Above (b) Below (c) On (d) None
16. Three lines  $l_1, l_2$  and  $l_3$  are .....if  $\begin{vmatrix} x_1 & y_1 & 1 \\ x_2 & y_2 & 1 \\ x_3 & y_3 & 1 \end{vmatrix} = 0$
- (a) Collinear (b) Concurrent (c) Coplanar (d) None
17. The lines are real and distinct if  $h^2 \dots\dots\dots ab$
- (a)  $>$  (b)  $<$  (c)  $=$  (d)  $\leq$
18. Three points P, Q, R are collinear if  $\Delta \dots\dots\dots 0$
- (a)  $=$  (b)  $>$  (c)  $<$  (d) None

19. The angle between two lines  $ax^2 + 2hxy - by^2 = 0$  is .....
- (a)  $\pi/3$  (b)  $\pi/2$  (c)  $\pi/4$  (d)  $\pi/6$
20. Slope of the line bisecting I and III. A quadrant is .....
- (a) 0 (b) 1 (c)  $\infty$  (d) None of these

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**SHORT QUESTION**

1. Find the point three – fifth of the way along the line segment from A (-5, 8) to B (5, 3)?
2. Find K so that the line joining A (7, 3); B (k, -6) and the line joining C (-4, 5), D (-6, 4) are Perpendicular?
3. Find an equation of the vertical line through (-5, 3)?
4. Find an equation of the horizontal line through (7, -9)?
5. Find an equation of the line through (-4, 7) and parallel to the line  $2x-7y+4 = 0$ ?
6. Find the area of the triangular region whose vertices are A (5, 3), B (-2, 2), C (4, 2)?
7. Find the equation of the line through (5, -8) and perpendicular to the join of A (-15, -8), B (10, 7)?
8. Find an equation of the line through (-8, 5) having slope undefined?
9. By means of slopes show that the points (-1, -3), (1, 5) and (2, 9) are Collinear.
10. Transform the equation  $5x - 12y + 39 = 0$  into Symmetric form.

## UNIT # 5

# LINEAR INEQUALITIES

1. An expression involving any one of the four symbols  $>$ ,  $<$ ,  $\geq$ ,  $\leq$  is called:
  - (a) An equation
  - (b) An identity
  - (c) An inequality
  - (d) A linear equality
  
2.  $ax + by > 2$  is an:
  - (a) Equation
  - (b) In-equation
  - (c) Identity
  - (d) A linear equality
  
3. The inequality  $x > 0$  shows:
  - (a) Right half-plane
  - (b) Left half-plane
  - (c) Upper half-plane
  - (d) lower half-plane
  
4.  $ax + by > c$  is a linear inequality in:
  - (a) One variable
  - (b) Two variables
  - (c) Three variables
  - (d) Four variables
  
5. Associated equation of  $ax + by > c$  is:
  - (a)  $ax + by = 0$
  - (b)  $ax + by < c$
  - (c)  $ax + by = c$
  - (d)  $ax + by > c$
  
6. The solution of  $ax + by < c$  is:
  - (a) Closed half-plane
  - (b) Open half –plane
  - (c) Circle
  - (d) Parabola

7. If the line segment obtained by joining any two points of a region lies entirely within the region then the region is called:
- (a) Feasible (b) Convex  
(c) Non-convex (d) Optimal
8. A function which is to be maximized or minimized is called:
- (a) Subjective function (b) Objective function  
(c) Qualitative function (d) Quantitative function
9. The feasible solution which maximizes or minimizes the objective function is called:
- (a) Exact solution (b) Optimal solution  
(c) Objective solution (d) Final solution
10. The point where two boundary lines of a shaded region intersect is called:
- (a) Boundary point (b) Corner point  
(c) Stationary point (d) Feasible point
11. If  $x > b$ , then
- (a)  $-x > -b$  (b)  $-x < b$   
(c)  $x < b$  (d)  $-x < -b$
12. A linear inequality contains at least ----- variable:
- (a) One (b) Two  
(c) Three (d) More than three
13. The graph of a linear equation of the form  $ax + by = c$  is a line which divides the whole plane into----- disjoint parts.
- (a) Two (b) Four  
(c) More than four (d) Infinitely many

14. The graph of corresponding linear equation of the linear inequality is a line called-----.
- (a) Boundary line                      (b) Horizontal line  
(c) Vertical line                        (d) Inclined line
15. The graph of the inequality  $x \leq b$  is:
- (a) Upper half plane                      (b) Lower half plane  
(c) Left half plane                        (d) Right half plane
16. The graph of the inequality  $y \leq b$  is:
- (a) Upper half plane                      (b) Lower half plane  
(c) Left half plane                        (d) Right half plane
17. Associated equation of  $x + 2y \leq 6$  or  $x + 2y \geq 6$  is the:
- (a) Same                                      (b) Not same  
(c) Sometimes same                        (d) None of these
18. The non-negative constraints;  $x \geq 0, y \geq 0$  indicate the:
- (a) Quadrant I                                (b) Quadrant II  
(c) Quadrant III                              (d) Quadrant IV
19.  $x = 0$  is the solution of the inequality:
- (a)  $2x + 1 > 0$                               (b)  $2x + 1 < 0$   
(c)  $2x + 1 \leq 0$                               (d) None of these

## SHORT QUESTIONS

1. Graph the solution of each of the following linear in equality in xy-plane.
  - (i)  $2x + y \leq 6$
  - (ii)  $2x + 1 \geq 0$
  - (iii)  $3y - 4 \leq 0$
  
2. Indicate the solution set of the following system of linear inequality by shading.
  - (i)  $2x - 3y \leq 6$
  - (ii)  $x - y \leq 1$
  - (iii)  $4x - 3y \leq 12, \quad x \geq 3/2.$
  
3. Graph the solution region of the following system of linear inequalities by shading.
  - (i)  $3x - 4y \leq 12$  and  $3x + 2y \geq 3$
  - (ii)  $2x + y \leq 4$  and  $2x - 3y \geq 12$

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## UNIT # 6

### Conic section

1. If radius of the Circle is Zero, then the Circle is called.....
  - (a) Zero circle (b) Point circle
  - (c) Concentric circle (d) In circle
  
2. A line may be a tangent to the parabola if  $C = \dots\dots\dots$ 
  - (a)  $am$  (b)  $a/m$  (c)  $m/a$  (d) Zero
  
3. The point (2, 2) lies ..... the circle  $x^2 + y^2 = 1$ 
  - (a) Outside (b) inside (c) On (d) None
  
4. An angle in a Semi circle is a/an ..... angle
  - (a) Right (b) Acute (c) Obtuse (d) None
  
5. The point where the axes meet, the parabola, is called..... of the parabola.
  - (a) Focus (b) Vertex
  - (c) Directrix (d) Centre
  
6. Latus rectum of the parabola  $x^2 = y$  is.....
  - (a) 1 (b) 2 (c) 3 (d) 4
  
7. Directrix of the parabola  $x^2 = 4y$  is.....
  - (a)  $y + 1 = 0$  (b)  $y - 1 = 0$  (c)  $y - 4 = 0$  (d)  $y + 4 = 0$
  
8. The Conic is a parabola if  $e \dots\dots\dots$ 
  - (a)  $=$  (b)  $>$  (c)  $<$  (d)  $\geq$

9. The Conic is an ellipse if  $e$ ..... |  
 (a) = (b) > (c) < (d)  $\geq$
10. The mid point of the hypotenuse of a right triangle is the ..... Centre of the triangle.  
 (a) In (b) Circum (c) e (d) None
11. Directrices of the ellipse  $x^2/b^2 + y^2/a^2 = 1$  are -----  
 (a)  $x = a/e$  (b)  $x = -a/e$  (c)  $y = \pm e/a$  (d)  $\pm a/e$
12. The Conic is a hyperbola if  $e$  ..... |  
 (a) = (b) > (c) < (d)  $\geq$
13. The focal chord perpendicular to the axis of the parabola is  $X =$  .....  
 (a)  $b$  (b)  $a$  (c)  $a$  (d) None
14. Axis of the parabola  $y^2 = -x$  is .....  
 (a)  $x = 0$  (b)  $y = 0$  (c)  $x = 1$  (d)  $x = -1$
15. Vertex of the parabola  $x^2 = 2y$  is .....  
 (a) (0, 0) (b) (0, 2) (c) (2, 0) (d) (1, 2)
16. Eccentricity of the ellipse is.....  
 (a)  $a/c$  (b)  $c/a$  (c)  $ac$  (d) None
17. Centre of the ellipse:  $\frac{(x+1)^2}{4} + \frac{(y+1)^2}{2} = 1$  is ----  
 (a) (1, 1) (b) (-1, 1) (c) (-1, -1) (d) (1, -1)

18. With usual notation: the points A and A' are called..... of the ellipse  
 $x^2/a^2 + y^2/b^2 = 1$   
 (a) Vertices (b) Co-vertices (c) Transverse (d) Conjugate
19. Length of Latus rectum of the ellipse is .....  
 (a)  $2a^2/b$  (b)  $2a/b^2$  (c)  $2b^2/a$  (d)  $2b/a^2$
20. In hyperbola  $x^2/a^2 - y^2/b^2 = 1$ ;  $c^2 = \dots\dots\dots$   
 (a)  $a^2 - b^2$  (b)  $a^2 + b^2$  (c)  $b^2 - a^2$  (d)  $\sqrt{a^2 - b^2}$
21. A conic is hyperbola if  $h^2 - ab \dots\dots 0$   
 (a) = (b) > (c) < (d)  $\geq$
22. The mid point C of the foci F and F' is called the ..... of the ellipse  
 (a) Vertex (b) Centre (c) Focus (d) Directrix

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## SHORT QUESTIONS

1. Find the centre and radius of the circle  $4x^2 + 4y^2 - 8x + 12y - 25 = 0$ .
2. Find the length of the tangent drawn from the point  $(-5, 4)$  to the Circle  $5x^2 + 5y^2 - 10x + 15y - 131 = 0$
3. Find an equation of the parabola having its focus at the origin and Directrix Parallel to  $y - \text{axis}$ .
4. Find an equation of the ellipse with foci  $(\pm 3, 0)$  and minor axis of length 10.
5. Prove that latus rectum of the ellipse is  $2b^2 / a$
6. Find an equation of the ellipse with vertices  $(0, \pm 6)$  and  $e = 2$  and  $e = 3 / 5$
7. Find an equation of the hyperbola with foci  $(0, \pm 6)$  and  $e = 2$ .
8. Find an equation of the hyperbola with foci  $(\pm 5, 0)$ ; vertex  $(3, 0)$ .

## CHAPTER # 7 VECTORS

1. A unit vector is a vector whose magnitude is .....  
(a) Zero (b) unity (c) -1 (d) None
2. If P is the mid point of AB then  $k_1 : k_2 = \dots\dots\dots$   
(a) 1 : 2 (b) 2 : 1 (c) 1 : 1 (d)  $\frac{1}{2} : 2$
3.  $\cos^2\alpha + \cos^2\beta + \cos^2\gamma = \dots\dots\dots$   
(a) 0 (b) 1 (c) -1 (d)  $\pm 1$
4.  $\hat{j} \cdot \hat{i} = \dots\dots\dots$   
(a) 0 (b) 1 (c)  $\hat{k}$  (d)  $-\hat{k}$
5.  $\hat{i} \times \hat{j} = \dots\dots\dots$   
(a) 0 (b) 1 (c)  $\hat{k}$  (d)  $-\hat{k}$
6.  $\hat{i} \times \hat{j} = \dots\dots\dots$   
(a)  $\hat{j}$  (b)  $-\hat{j}$  (c) 1 (d) 0
7. U and V are orthogonal if  $\theta = \dots\dots\dots$   
(a)  $\pi/6$  (b)  $\pi/4$  (c)  $\pi/3$  (d)  $\pi/2$
8. U and V are parallel if  $U \times V = \dots\dots\dots$   
(a) 0 (b)  $-V \times U$  (c) 1 (d) -1
9. Two vectors U And V are Collinear if  $\theta = \dots\dots\dots$

10. (a) 0 (b)  $\pi$  (c)  $\pi/2$  (d) a and b  
 If  $\underline{V} = ai + bi + ck$  then projection of  $\underline{V}$  along  $j = \dots\dots\dots$
- (a) b (b) a (c) j (d) k
11. If  $\underline{V} = ai + bj + ck$  then projection of  $V$  along  $k = \dots\dots\dots$
- (a) c (b) a (c) b (d) k
12. In any triangle ABC  $a = b \cos C + \dots\dots\dots$
- (a)  $c \cos B$  (b)  $a \cos B$  (c)  $b \cos A$  (d)  $b \cos B$
13.  $\underline{U} \times \underline{V} = \dots\dots\dots$
- (a)  $\underline{V} \times \underline{W}$  (b)  $-\underline{V} \times \underline{U}$  (c)  $\underline{W} \times \underline{U}$  (d)  $-\underline{W} \times \underline{V}$
14. Projection of  $\underline{U}$  along  $\underline{V} = \dots\dots\dots$
- (a)  $\frac{\underline{U} \cdot \underline{V}}{|\underline{V}|}$  (b)  $\frac{\underline{U} \cdot \underline{V}}{|\underline{U}|}$  (c)  $\frac{|\underline{U} \cdot \underline{V}|}{\underline{V}}$  (d)  $\frac{|\underline{U} \cdot \underline{V}|}{\underline{U}}$
15. Work Done =  $\dots\dots\dots$
- (a)  $F \cdot d$  (b)  $F \cdot r$  (c)  $r \cdot d$  (d) None of these
16.  $\underline{U}, \underline{V}$  and  $\underline{W}$  are Coplanar if  $(\underline{U} \times \underline{V}) \cdot \underline{w} = \dots\dots\dots$
- (a) 0 (b)  $\pi/3$  (c)  $\pi/2$  (d)  $\pi/4$
17. Volume of tetrahedron =  $\dots\dots\dots$
- (a)  $\frac{1}{2} (\underline{u} \times \underline{v}) \cdot \underline{w}$  (b)  $\frac{1}{4} (\underline{u} \times \underline{v}) \cdot \underline{w}$
- (c)  $\frac{1}{3} (\underline{u} \times \underline{v}) \cdot \underline{w}$  (d)  $\frac{1}{6} (\underline{u} \times \underline{v}) \cdot \underline{w}$
18. If  $K$  is +ve, then  $\underline{V}$  and  $k\underline{v}$  are in the  $\dots\dots$  Direction
- (a) Opposite (b) Same (c) Upward (d) downward.

19. The vector whose initial point is the origin  $O$  and terminal point is  $P$  is called the ----- vector.
- (a) Unit (b) Position (c) Zero vector (d) None
20.  $U \times U = \dots\dots\dots$
- (a)  $-U$  (b)  $U$  (c)  $0$  (d)  $1$

## SHORT QUESTIONS

1. Find a unit vector in the direction of the vector  $\underline{\gamma} = -\frac{\sqrt{3}}{2} \underline{i} - \frac{1}{2} \underline{j}$
2. Find the direction cosines for the vector  $\overrightarrow{PQ}$  where  $P = (2, 1, 5)$  and  $Q = (1, 3, 1)$ .
3. By means of vector prove that  $a^2 = b^2 + c^2 - 2bc \cos A$ .
4. By means of vector prove that  $a = b \cos C + c \cos B$ .
5. Prove that  $\cos(\alpha - \beta) = \cos \alpha \cos \beta + \sin \alpha \sin \beta$  (by use of vectors)
6. Prove that  $\cos(\alpha + \beta) = \cos \alpha \cos \beta - \sin \alpha \sin \beta$  (by use of vectors)
7. Prove that  $\sin(\alpha + \beta) = \sin \alpha \cos \beta + \cos \alpha \sin \beta$  ( // )
8. Prove that  $\sin(\alpha - \beta) = \sin \alpha \cos \beta - \cos \alpha \sin \beta$  ( // )
9. Prove that in any triangle.  
(i)  $b = c \cos A + a \cos C$  (ii)  $c = a \cos B + b \cos A$ .
10. Find the volume of the tetrahedron whose vertices are  $A(2, 1, 8)$ ,  $B(3, 2, 9)$ ,  $C(2, 1, 4)$ ,  $D(3, 3, 10)$ .
11. Prove that the vertices  $\underline{i} - 2\underline{j} + 3\underline{k}$ ,  $-2\underline{i} + 3\underline{j} - 4\underline{k}$  and  $\underline{i} - 3\underline{j} + 5\underline{k}$  are Coplanar.
12. If  $\underline{a} + \underline{b} + \underline{c} = 0$  then prove that  $\underline{b} \times \underline{c} = \underline{c} \times \underline{a}$ .

# ANSWERS

## UNIT # 1

- |    |   |     |   |     |   |     |   |
|----|---|-----|---|-----|---|-----|---|
| 1. | c | 8.  | d | 15. | a | 22. | a |
| 2. | b | 9.  | a | 16. | b | 23. | d |
| 3. | b | 10. | a | 17. | c | 24. | a |
| 4. | b | 11. | c | 18. | c | 25. | d |
| 5. | d | 12. | c | 19. | b |     |   |
| 6. | d | 13. | b | 20. | b |     |   |
| 7. | d | 14. | a | 21. | d |     |   |

## UNIT # 2

- |    |   |     |   |     |   |     |   |
|----|---|-----|---|-----|---|-----|---|
| 1. | a | 8.  | b | 15. | b | 22. | a |
| 2. | b | 9.  | c | 16. | a | 23. | d |
| 3. | b | 10. | d | 17. | b | 24. | d |
| 4. | c | 11. | b | 18. | a | 25. | d |
| 5. | d | 12. | d | 19. | c |     |   |
| 6. | c | 13. | a | 20. | c |     |   |
| 7. | a | 14. | c | 21. | b |     |   |

## UNIT # 3

- |    |   |     |   |     |   |     |   |
|----|---|-----|---|-----|---|-----|---|
| 1. | d | 8.  | a | 15. | c | 22. | b |
| 2. | a | 9.  | d | 16. | b | 23. | d |
| 3. | c | 10. | b | 17. | d | 24. | c |
| 4. | d | 11. | d | 18. | c | 25. | b |
| 5. | b | 12. | d | 19. | b | 26. | a |
| 6. | b | 13. | a | 20. | c |     |   |
| 7. | c | 14. | b | 21. | c |     |   |

**UNIT # 4**

- |    |   |     |   |     |   |     |   |
|----|---|-----|---|-----|---|-----|---|
| 1. | b | 6.  | d | 11. | a | 16. | a |
| 2. | a | 7.  | b | 12. | b | 17. | c |
| 3. | d | 8.  | a | 13. | a | 18. | a |
| 4. | d | 9.  | a | 14. | c | 19. | b |
| 5. | a | 10. | b | 15. | a | 20. | b |

**UNIT # 5**

- |    |   |     |   |     |   |     |   |
|----|---|-----|---|-----|---|-----|---|
| 1. | c | 6.  | b | 11. | d | 16. | b |
| 2. | b | 7.  | b | 12. | a | 17. | a |
| 3. | a | 8.  | b | 13. | a | 18. | a |
| 4. | b | 9.  | b | 14. | a | 19. | a |
| 5. | a | 10. | b | 15. | c |     |   |

**UNIT # 6**

- |    |   |     |   |     |   |     |   |
|----|---|-----|---|-----|---|-----|---|
| 1. | b | 7.  | a | 13. | b | 19. | c |
| 2. | b | 8.  | a | 14. | b | 20. | b |
| 3. | a | 9.  | a | 15. | a | 21. | b |
| 4. | a | 10. | b | 16. | b | 22. | b |
| 5. | b | 11. | d | 17. | c |     |   |
| 6. | a | 12. | b | 18. | a |     |   |

**UNIT # 7**

- |    |   |     |   |     |   |     |   |
|----|---|-----|---|-----|---|-----|---|
| 1. | b | 6.  | b | 11. | a | 16. | a |
| 2. | c | 7.  | d | 12. | a | 17. | d |
| 3. | b | 8.  | a | 13. | b | 18. | b |
| 4. | a | 9.  | d | 14. | a | 19. | b |
| 5. | c | 10. | a | 15. | a | 20. | c |

Notes, MCQs, model papers, old papers are available at  
<http://www.MathCity.org/FSc>