

OBJECTIVE

Q. 7: Some possible answers to each statement are given below. Tick (P) mark the correct answer.

i) $x = at^2$ and $y = 2at$ represents:

- a) Circle b) Ellipse
c) Parabola d) Hyperbola

ii) $\lim_{x \rightarrow 0} \frac{e^x - 1}{x} = \dots\dots\dots$

- a) 0 b) 1c) e d) ∞

iii) If $f(x) = x^{\frac{2}{3}}$ then $f'(8) =$

- a) $\frac{1}{2}$ b) $\frac{2}{3}$ c) $\frac{1}{3}$ d) 3

iv) If $y = \cos^{-1} \frac{x}{a}$, then $\frac{dy}{dx} =$

- a) $\frac{-1}{\sqrt{a^2 - x^2}}$ b) $\frac{1}{\sqrt{a^2 - x^2}}$
c) $\frac{1}{a\sqrt{a^2 - x^2}}$ d) $\frac{1}{\sqrt{a^2 + x^2}}$

v) $f(x) = f(0) + xf'(0) + \frac{x^2}{\underline{2}} f''(0) + \dots + \frac{x^n}{\underline{n}} f^{(n)}(0) + \dots$

- a) Taylor's series b) Binomial series
c) Machlaurin's series d) Power series

vi) $\int \sec 5x \tan 5x \, dx =$

- a) $5 \sec 5x \tan 5x + c$ b) $\frac{1}{5} \sec x + c$
c) $\frac{\sec 5x}{5} + c$ d) $\frac{\tan 5x}{5} + c$

vii) $\int \cos x \left(\frac{\ln \sin x}{\sin x} \right) dx =$

- a) $\ln(\sin x)^2 + c$ b) $\frac{1}{2} \ln(\sin x)^2 + c$
c) $(\ln \sin x)^2 + c$ d) $\frac{1}{2} (\ln \sin x)^2 + c$

viii) $\int x e^x dx =$

- a) $x e^x + e^x + c$ b) $e^x + x + c$
c) $x e^x - e^x + c$ d) $x e^x + c$

ix) $\int_0^{\frac{1}{\sqrt{3}}} \frac{dx}{1+x^2} =$

- a) $\frac{p}{2}$ b) $\frac{p}{6}$ c) $\frac{p}{4}$ d) $\frac{p}{3}$

- x) The solution of $\frac{dy}{dx} = -y$ is
 a) $y = e^x$ b) $y = ce^{-x}$ c) $y = e^{-x}$ d) $y = ce^x$
- xi) If $a = 0$ in the $ax + by + c = 0$ then line is
 a) \parallel to x -axis b) \parallel to y -axis
 c) Inclined d) Passing through origin
- xii) The point of intersection of medians of a triangle is called
 a) Centroid b) Orthocentre
 c) Circumcentre d) In-centre
- xiii) $(0,0)$ is one of the solutions of inequality;
 a) $3x + 5y > 7$ b) $2x - 3y > 4$
 c) $x + 3y > 5$ d) $2x + 3y < 5$
- xiv) Radius r of a circle $x^2 + y^2 + 2gx + 2fy + c = 0$ is
 a) $\sqrt{g^2 + f^2 + c}$ b) $\sqrt{g^2 + f^2 - c}$
 c) $\sqrt{g + f + c}$ d) $\sqrt{g^2 - f^2 - c}$
- xv) The point where the axis meets the parabola is called
 a) Focus b) Directrix c) Centre d) Vertex
- xvi) For the ellipse $\frac{x^2}{b^2} + \frac{y^2}{a^2} = 1$ foci are
 a) $(\pm c, 0)$ b) $(0, \pm c)$ c) $(c, 0)$ d) $(0, c)$
- xvii) For the hyperbola $\frac{x^2}{a^2} - \frac{y^2}{b^2} = 1$ the directrices are
 a) $x = \pm \frac{c}{e}$ b) $x = \pm \frac{c}{e^2}$ c) $x = \pm \frac{c}{2e}$ d) $y = \pm \frac{c}{e^2}$
- xviii) For the equation of tangent to conic x^2 is replaced by
 a) xx_1 b) x c) $\frac{1}{2}(x + x_1)$ d) xx_1^2
- xix) Cosine of the angle between two non-zero vectors \underline{a} and \underline{b} is
 a) $\underline{a} \cdot \underline{b}$ b) $\frac{|\underline{a}||\underline{b}|}{\underline{a} \cdot \underline{b}}$ c) $\frac{\underline{a} \cdot \underline{b}}{|\underline{a}||\underline{b}|}$ d) $\frac{\underline{a} \times \underline{b}}{|\underline{a}||\underline{b}|}$
- xx) If $\underline{a} \times \underline{b} = 0$ and $\underline{a} \cdot \underline{b} = 0$ then
 a) \underline{a} and \underline{b} are parallel b) \underline{a} and \underline{b} are perpendicular
 c) Either $\underline{a} = 0$ or $\underline{b} = 0$ d) Both \underline{a} and \underline{b} are non-zero

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Section – I*Note: All questions are to be attempted on answer book.***Q # 1: Write any TWENTY-FIVE short answers of the following questions:**

- (i) If $f(x) = \sin x$, find $\frac{f(a+h) - f(a)}{h}$
- (ii) Evaluate the limit: $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x^2 + x - 6}$
- (iii) Discuss the continuity of $f(x)$:
- $$f(x) = \begin{cases} 2x+5, & \text{if } x \leq 2 \\ 4x+1, & \text{if } x > 2 \end{cases} \quad \text{at } x = 2.$$
- (iv) Differentiate w.r.t x of $\frac{2x-3}{2x+1}$.
- (v) Differentiate $\sin^2 x$ w.r.t $\cos^4 x$
- (vi) Find $\frac{dy}{dx}$, if $y = \cosh 2x$.
- (vii) If $y = \sin 3x$, find y_2
- (viii) Examine the function defined as $f(x) = 1 + x^3$ for extreme value.
- (ix) Find dy when $y = x^2 - 1$ when 'x' change from 3 to 2.02
- (x) Evaluate: $\int \frac{1-x^2}{1+x^2} dx$
- (xi) Evaluate: $\int \frac{\sec^2 x}{\sqrt{\tan x}} dx$
- (xii) Evaluate: $\int \ln x dx$
- (xiii) Evaluate: $\int \frac{2a}{a^2 - x^2} dx$
- (xiv) Evaluate: $\int a^{x^2} x dx$
- (xv) Find the area bounded by $\sin x$ from $x = -\frac{p}{2}$ to $\frac{p}{2}$.
- (xvi) Show that solution of $\frac{1}{x} \frac{dy}{dx} - 2y = 0$ is $y = ce^{x^2}$.
- (xvii) Find the points trisecting the join of $A(-1, -4)$ and $B(6, 2)$.
- (xviii) Find k so that \overline{AB} is perpendicular to \overline{CD} , where $A(7, 3)$, $B(k, -6)$, $C(-4, 5)$, $D(-6, 4)$ are given vertices.
- (xix) Find equation of line with x -intercept -9 , slope -4 .
- (xx) Find the area of the triangular region whose vertices are $A(-5, 3)$, $B(-2, 2)$, $C(4, 2)$.
- (xxi) Find the interior angle A of the triangle with vertices $A(-2, 11)$, $B(-6, -3)$, $C(4, -9)$.
- (xxii) Find the measure of the angle between the line represented by the homogeneous equation $x^2 - xy - 6y^2 = 0$.
- (xxiii) Define the associated equation of an inequality.

(xxiv)	What is convex region? Define it.
(xxv)	What is linear programming?
(xxvi)	Define circle.
(xxvii)	Find the vertex and directrix of $x^2 = -16y$.
(xxviii)	Find the lengths of semi major axis and semi minor axis of ellipse $\frac{x^2}{9} + \frac{y^2}{4} = 1$.
(xxix)	Define hyperbola.
(xxx)	Determine whether the point $P(-5,6)$ lies outside, on or inside the circle $x^2 + y^2 + 4x - 6y - 12 = 0$.
(xxxi)	Find an equation of circle with ends of diameter at $(-3,2)$ and $(5,-6)$.
(xxxii)	Write the most general equation of second degree of the conic.
(xxxiii)	Find a , so that $ a\mathbf{i} + (a+1)\mathbf{j} + 2\mathbf{k} = 3$.
(xxxiv)	Find a so that the vectors $2\mathbf{i} + a\mathbf{j} + 5\mathbf{k}$ and $3\mathbf{i} + \mathbf{j} + a\mathbf{k}$ are perpendicular.
(xxxv)	Find a vector perpendicular to each of the vectors $\mathbf{a} = 2\mathbf{i} + \mathbf{j} + \mathbf{k}$ and $\mathbf{b} = 4\mathbf{i} + 2\mathbf{j} - \mathbf{k}$.
(xxxvi)	What is scalar triple product?
(xxxvii)	Find the area of the triangle with vertices $A(1,-1,1)$, $B(2,1,-1)$ and $C(-1,1,2)$.

Section - II	
Note: Attempt any <i>THREE</i> questions.	
Q # 2 (a)	Prove that $\lim_{x \rightarrow 0} \frac{a^x - 1}{x} = \log_e a$
(b)	Find the derivative of $(x+4)^{\frac{1}{3}}$ w.r.t x by definition.
Q # 3 (a)	Evaluate: $\int \frac{\sqrt{2} dx}{\sin x + \cos x}$
(b)	Evaluate: $\int_{-1}^2 (x + x) dx$
Q # 4 (a)	The three points $A(7,-1)$, $B(-2,2)$ and $C(1,4)$ are consecutive vertices of a parallelogram. Find the fourth vertex.
(b)	Graph the feasible region subject to constraints $2x - 3y \leq 6$, $2x + y \geq 2$, $x + 2y \leq 8$, $x \geq 0$, $y \geq 0$
Q # 5 (a)	Find the equation of circle passing through points $A(3,-1)$, $B(0,1)$ and having centre at $4x - 3y - 3 = 0$.
(b)	Find the equation of parabola with focus $(-3,1)$ and directrix $x - 2y - 3 = 0$.
Q # 6 (a)	Find a unit vector perpendicular to the plane containing \mathbf{a} and \mathbf{b} , also find sine of angle between them; $\mathbf{a} = 2\mathbf{i} - 2\mathbf{j} + 4\mathbf{k}$, $\mathbf{b} = -\mathbf{i} + \mathbf{j} - 2\mathbf{k}$.
(b)	Find a so that the vectors $\mathbf{i} - \mathbf{j} + \mathbf{k}$, $\mathbf{i} - 2\mathbf{j} - 3\mathbf{k}$ and $3\mathbf{i} - a\mathbf{j} + 5\mathbf{k}$ are coplanar.