

Federal Board HSSC-I Examination  
Mathematics Model Question Paper

**FBISE**  
WE WORK FOR EXCELLENCE

Roll No:

Answer Sheet No: \_\_\_\_\_

Signature of Candidate: \_\_\_\_\_

Signature of Invigilator: \_\_\_\_\_

**SECTION – A**

Time allowed: 20 minutes

Marks: 20

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Note: Section-A is compulsory and comprises pages 1-7. All parts of this section are to be answered on the question paper itself. It should be completed in the first 20 minutes and handed over to the Centre Superintendent. Deleting/overwriting is not allowed. Do not use lead pencil.

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Q.1 Insert the correct option i.e. A/B/C/D in the empty box provided opposite each part. Each part carries one mark.

i. Multiplicative inverse of complex number  $(-2, 3)$  is

A.  $\left(\frac{-2}{\sqrt{13}}, \frac{-3}{\sqrt{13}}\right)$

B.  $\left(\frac{-2}{\sqrt{13}}, \frac{3}{\sqrt{13}}\right)$

C.  $\left(\frac{2}{\sqrt{13}}, \frac{-3}{\sqrt{13}}\right)$

D.  $\left(\frac{2}{\sqrt{13}}, \frac{3}{\sqrt{13}}\right)$

ii. Consider the circle relation “C” define for all  $(x,y) \in \mathbb{R} \times \mathbb{R}$  such that  $-1 \leq x, y \leq 1, (x,y) \in C \leftrightarrow x^2 + y^2 = 1$  then  $C(x, y)$  is:

A. 1 – 1 function

B. onto function

C. bijective function

D. not function

**DO NOT WRITE ANYTHING HERE**

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iii. If the application of elementary row operation on  $[A : I]$  in succession reduces A to I then the resulting matrix is

A.  $[A^{-1} : I]$

B.  $[I : A^{-1}]$

C.  $\begin{bmatrix} A^{-1} \\ \vdots \\ I \end{bmatrix}$

D.  $[A : A^{-1}]$

iv. If  $\alpha$  and  $\beta$  be the roots of  $ax^2 + bx + c = 0$ , then  $\alpha + \beta + \frac{1}{\alpha\beta}$  is

A.  $\frac{c-b}{a}$

B.  $\frac{a^2 - bc}{ac}$

C.  $\frac{a^2 + bc}{ac}$

D.  $\frac{ac}{a^2 - bc}$

v.  $\frac{1}{x-1} + \frac{1}{x+1} - \frac{1}{x}$  are the partial fractions of

A.  $\frac{x^2 + 1}{x(x^2 - 1)}$

B.  $\frac{x^2 - 1}{x(x^2 - 1)}$

C.  $\frac{1}{x(x^2 - 1)}$

D.  $\frac{x^2 + 1}{x^2 - 1}$

vi. Which of the following is sum of n AMs between a and b?

A.  $\frac{(a + b)^n}{2}$

B.  $\frac{na + nb}{2}$

C.  $\frac{a^n + b^n}{2}$

D.  $n\sqrt{ab}$

vii. 8 beads of different colours can be arranged in a necklace in

A. 8 ! ways

B. 5040 ways

C. 2520 ways

D. 2 x 7 ! ways

viii.  ${}^nC_2$  exist when n is

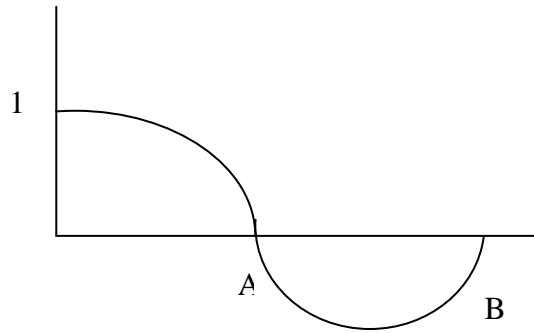
A.  $n < 2$

B.  $n = 1$

C.  $n \geq 2$

D.  $n \leq 1$

ix. If  $f(x) = \cos 2x$  the value of  $x$  at point B is



A.  $\frac{3\pi}{4}$

B.  $\pi$

C.  $\frac{3\pi}{2}$

D.  $2\pi$

x.  $2 \cos^2\left(\frac{3}{8}\pi\right) - 1$  is

A.  $\frac{1}{\sqrt{2}}$

B.  $-\frac{1}{\sqrt{2}}$

C.  $\frac{\sqrt{3}}{2}$

D.  $-\frac{\sqrt{3}}{2}$

xi. An Arc  $\widehat{PQ}$  subtends an angle of  $60^\circ$  at the center of a circle of radius 1 cm. The length  $\widehat{PQ}$  is:

A. 60 cm

B. 30 cm

C.  $\frac{\pi}{6}$  cm

D.  $\frac{\pi}{3}$  cm

xii. If in a triangle  $b = 37$ ,  $c = 45$ ,  $\alpha = 30^\circ 50'$  Then the area of the triangle is

- A. 426.69 sq unit
- B. 246.69 sq unit
- C. 624.96 sq unit
- D. 924.69 sq unit

xiii. The graph of  $y = \tan x$  is along  $x$ -axis. The graph of  $y = \tan^{-1}x$  would be along

- A.  $x$  - axis
- B.  $y$  - axis
- C. origin
- D.  $z$  - axis

xiv. If  $\sin x = \frac{1}{2}$  then  $x$  has values

- A.  $\frac{\pi}{6}, \frac{\pi}{3}$
- B.  $\frac{\pi}{6}, \frac{5\pi}{6}$
- C.  $\frac{\pi}{2}, \frac{\pi}{6}$
- D.  $\frac{\pi}{6}, \frac{-5\pi}{6}$

xv.  $(P(A), *)$  where  $*$  stands for intersection and  $A$  is a non empty set then  $(P(A), *)$  is

- A. monoid group
- B. abelian group
- C. Group
- D. bijective function

xvi. The product of all 4<sup>th</sup> roots of unity is

- A. 1
- B. -1
- C.  $i$
- D.  $-i$

xvii. If  $\frac{1}{a}, \frac{1}{H}, \frac{1}{b}$  are in H.P then H is

A.  $\frac{2ab}{a+b}$

B.  $\frac{a+b}{2ab}$

C.  $\frac{a-b}{2ab}$

D.  $\frac{2ab}{a-b}$

xviii. Probability of a child being born on Friday is

A.  $\frac{1}{3}$

B.  $\frac{1}{2}$

C.  $\frac{1}{7}$

D.  $\frac{1}{4}$

xix.  $\cos^{-1} x + \cos^{-1}(-x)$

A. 0

B.  $\frac{\pi}{2}$

C.  $\pi$

D.  $2 \cos x$

xx. In a triangle if  $a = 17$ ,  $b = 10$  and  $c = 21$  then circum radius 'R' is

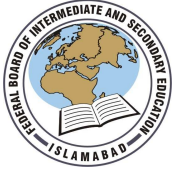
- A. 84
- B. 28
- C. 12
- D.  $\frac{85}{8}$

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For Examiner's use only

Q. No.1: Total Marks:

Marks Obtained:



Federal Board HSSC-I Examination  
Mathematics Model Question Paper

Time allowed: 2.40 hours

Total Marks: 80

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Note: Sections 'B' and 'C' comprise pages 1-3 and questions therein are to be answered on the separately provided answer book. Answer any ten questions from section 'B' and attempt any five questions from section 'C'. Use supplementary answer sheet i.e., sheet B if required. Write your answers neatly and legibly.

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**SECTION-B**  
(Marks: 40)

Note: Attempt any **TEN** questions.

2. Simplify by justifying each step

$$\frac{\frac{1}{a} - \frac{1}{b}}{1 - \frac{1}{a} \cdot \frac{1}{b}} \quad (4)$$

3. If  $p$  and  $q$  are elements of a group  $G$  show that:  $(pq)^{-1} = q^{-1} p^{-1}$  (4)

4. If  $A = \begin{bmatrix} i & 1+i \\ 1 & -i \end{bmatrix}$   
Show that  $A + (\overline{A})^t$  is Hermitian matrix. (4)

5. A wire of length 80 cm is cut into two parts and each part is bent to form squares. If the sum of the areas of the squares is  $300 \text{ cm}^2$ . Find the length of the sides of two squares. (4)

6. Resolve into partial fraction

$$\frac{x^4}{x^3 + 1} \quad (4)$$



7. If  $y = 1 + 2x + 4x^2 + 8x^3 + \dots$   
Then show that  $x = \frac{y-1}{2y}$  (4)
8. The members of a club are 12 boys and 8 girls, in how many ways can a committee of 3 boys and 2 girls be formed. (4)
9. Find  $(2n+1)$ th term from the end in the expansion of  $\left(x - \frac{1}{2x}\right)^{3n}$ . (4)
10. Find the values of remaining trigonometric functions if  $\cot \theta = \sqrt{7}$  and  $\theta$  is not in 1st quadrant. (4)
11. Prove that  
 $\cos 4x = 8 \cos^4 x - 8 \cos^2 x + 1$  (4)
12. If  $r_1, r_2, r_3$  are in A.P then show that  
 $(a-b)(s-c) = (b-c)(s-a)$  (4)
13. Solve for "x"  
 $\cos^{-1}(2x^2 - 2x) = \frac{2\pi}{3}$  (4)
14. Solve  $\frac{1}{\sin^2 \theta} = \frac{4}{3}$  (4)
15. If the roots of the equation  $x^2 - Px + q = 0$  differ by unity, prove that  $P^2 = 4q + 1$ . (4)

**SECTION – C**  
(Marks: 40)

Note: Attempt any **FIVE** questions. Each question carries equal marks.

**(Marks 5x8=40)**

16. Solve the system of following linear equations.  
 $x_1 + 3x_2 + 2x_3 = 3$   
 $4x_1 + 5x_2 - 3x_3 = -3$   
 $3x_1 - 2x_2 + 17x_3 = 42$   
 By reducing its augmented matrix to reduce Echelon form. (8)

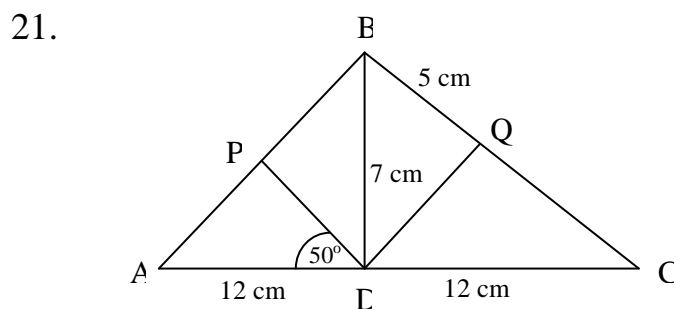
17. Resolve into partial fractions.

$$\frac{1}{x^2(x^2 + a^2)} \quad (8)$$

18. Prove that the sum of all positive integers less than 100 which do not contain the digit 7 is 3762. (8)

19. Write down and simplify the expansion of  $(1-P)^5$ . Use this result to find the expansion of  $(1-x-x^2)^5$  in ascending power of  $x$  as far as the terms in  $x^3$ . Find the value of  $x$  which would enable you to estimate  $(0.9899)^5$  from this expansion. (8)

20. Draw the graph of  $y = \cot x$  for the complete period. (8)

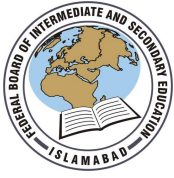


The diagram shows the supports for the roof of a building in which  $\overline{BD} = 7\text{cm}$ ,  $\overline{AD} = \overline{DC} = 12\text{cm}$ ,  $\overline{BQ} = 5\text{cm}$ ,  $\angle P\hat{D}A = 50^\circ$ , then calculate

- (i)  $\angle B\hat{A}D$     (ii)  $\overline{PD}$     (iii)  $\overline{DQ}$     (iv)  $\overline{CQ}$  (8)

22. Solve the given equations.

$$\begin{aligned} x^2 - y^2 &= 5 \\ 4x^2 - 3xy &= 18 \end{aligned} \quad (8)$$



Federal Board HSSC – I Examination  
Mathematics – Mark Scheme

**SECTION A**

**Q.1**

- |       |   |       |   |        |   |
|-------|---|-------|---|--------|---|
| i.    | A | ii.   | D | iii.   | B |
| iv.   | B | v.    | A | vi.    | B |
| vii.  | C | viii. | C | ix.    | C |
| x.    | B | xi.   | D | xii.   | A |
| xiii. | B | xiv.  | B | xv.    | A |
| xvi.  | B | xvii. | B | xviii. | C |
| xix.  | C | xx.   | A |        |   |

**(20×1=20)**

**SECTION B**

**Q.2**

**(4)**

$$\frac{1}{a} - \frac{1}{b}$$

$$1 - \frac{1}{ab}$$

$$= \frac{1}{a} \times \frac{b}{b} - \frac{1}{b} \times \frac{a}{a}$$

Multiplication (1 mark)

$$1 - \frac{ab}{ab} - \frac{1}{ab}$$

$$= \frac{b}{ab} - \frac{a}{ab}$$

Golden rule of fraction (1 mark)

$$= \frac{ab}{ab} - \frac{1}{ab}$$

$$= \frac{1}{ab} (b - a)$$

Distribution property of multiplication over subtraction (1 mark)

$$= \frac{1}{ab} (ab - 1)$$

$$= \frac{1}{ab} (b - a)$$

Cancellation property (1 mark)

$$= \frac{1}{ab} (ab - 1)$$

**Q.3**

**(4)**

Given that  $a, b \in G$  &  $G$  is group so

$$\begin{aligned} (ab) b^{-1} a^{-1} &= a (bb^{-1}) a^{-1} \\ &= a(e) a^{-1} \\ &= a a^{-1} \\ &= e \quad \text{----- I} \end{aligned}$$

(2 marks)

Now let

$$\begin{aligned} (b^{-1} a^{-1}) (ab) &= b (a^{-1} a) b \\ &= b^{-1}(e) b \\ &= b^{-1} b \\ &= e \quad \text{----- II} \end{aligned}$$

(2 marks)

From I & II  $ab$  &  $b^{-1} a^{-1}$  are inverse of each other.

**Q.4**

**(4)**

$$A = \begin{pmatrix} i & 1+i \\ 1 & -i \end{pmatrix}$$

$$\bar{A} = \begin{pmatrix} -i & 1-i \\ 1 & i \end{pmatrix}$$

(1 mark)

$$(\bar{A})^t = \begin{pmatrix} -i & 1 \\ 1-i & i \end{pmatrix}$$

$$A + (\bar{A})^t = \begin{pmatrix} i & 1+i \\ 1 & -i \end{pmatrix} + \begin{pmatrix} -i & 1 \\ 1-i & i \end{pmatrix}$$

$$A + (\bar{A})^t = \begin{pmatrix} 0 & 2+i \\ 2-i & 0 \end{pmatrix}$$

(1 mark)

Let  $B = A + (\bar{A})^t$

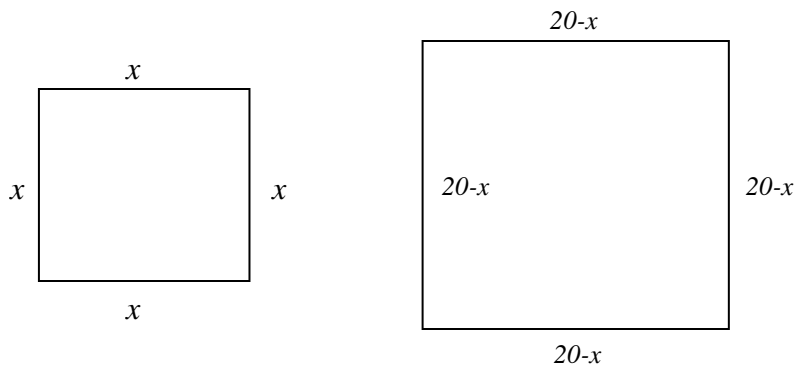
$$\bar{B} = \begin{pmatrix} 0 & 2-i \\ 2+i & 0 \end{pmatrix} \Rightarrow (\bar{B})^t = \begin{pmatrix} 0 & 2+i \\ 2-i & 0 \end{pmatrix}$$

(2 marks)

So  $(\bar{B})^t = B$  Hence  $A + (\bar{A})^t$  Hermitian Matrix

**Q.5**

**(4)**



Let length of each side of one square =  $x$  cm

Remaining Length of wire =  $80 - 4x$  (1 mark)

Length of each side of other square =  $\frac{80-4x}{4}$   
 $= 20 - x$  (1 mark)

By given condition

$$x^2 + (20-x)^2 = 300$$

$$x^2 - 20x + 50 = 0$$

$$x = \frac{-(20) \pm \sqrt{(-20)^2 - 4(1)(50)}}{2}$$
 (1 mark)

$$x = 17.07 \quad x = 2.93$$
 (1 mark)

Hence length of sides of square is 2.93 cm & 17.07 cm.

**Q.6** (4)

$$\frac{x^4}{x^3 + 1} \quad \begin{array}{r} x \\ x^3 + 1 \overline{) x^4} \\ \underline{-x^4 + x} \\ -x \end{array}$$

$$= x - \frac{x}{x^3 + 1}$$
 (1 mark)

For partial fraction Let

$$\frac{x}{x^3 + 1} = \frac{x}{(x+1)(x^2 - x + 1)}$$

$$\frac{x}{(x+1)(x^2 - x + 1)} = \frac{A}{x+1} + \frac{Bx + C}{x^2 - x + 1} \quad \rightarrow \quad I$$

Multiplying with  $(x+1)(x^2-x-1)$

$$x = A(x^2 - x + 1) + (Bx + c)(x+1) \quad \rightarrow \quad II$$

Put  $x+1=0 \Rightarrow x=-1$

$$1 = A(1 + 1 - 1) \Rightarrow \boxed{A = -1}$$
 (1 mark)

Comparing the coefficient of  $x^2$  on both sides

$$0 = A + B \Rightarrow \boxed{B = +1}$$

Comparing the coefficient of  $x$

$$1 = -A + B + C$$

$$1 = 1 + 1 + C$$

$$\boxed{C = -1}$$
 So putting A, B, C in I (1 mark)

$$\frac{x}{(x+1)(x^2 - x + 1)} = \frac{-1}{x+1} + \frac{x-1}{x^2 - x + 1}$$

Hence complete Partial fraction is

$$\frac{x^4}{x^3 + 1} = x + \frac{1}{x+1} - \frac{x-1}{x^2 - x + 1}$$
 (1 mark)

**Q.7** **(4)**

$$y = 1 + 2x + 4x^2 + 8x^3 + \dots \infty$$

$a = 1, r = 2x$  than (1 mark)

$$S_{\infty} = \frac{a}{1-r}$$

$$y = \frac{a}{1-r} \quad (1 \text{ mark})$$

$$y = \frac{1}{1-2x}$$

$$y - 2xy = 1 \quad (1 \text{ mark})$$

$$y - 1 = 2x$$

$$2xy = y - 1 \quad (1 \text{ mark})$$

$$x = \frac{y-1}{2y}$$

**Q.8** **(4)**

Total members of the club = 20

No of boys = 12

No. of Girls = 8 (1 mark)

No. of ways of selecting 3 boys =  ${}^{12}C_3$   
= 220 (1 mark)

No. of ways of selecting 2 girls =  ${}^8C_2$   
= 28 (1 mark)

Total No. of ways =  ${}^{12}C_3 \times {}^8C_2$   
=  $220 \times 28$   
= 6160 (1 mark)

**Q.9** **(4)**

According to the problem

$$a = -\frac{1}{2x}, \quad b = x, \quad n = 3n$$

Total No. of terms =  $3n+1$ , Required term =  $2x + 1$

So  $r = 2n$  (1 mark)

$$T_{r+1} = \binom{n}{r} a^{n-r} b^r \quad (1 \text{ mark})$$

$$T_{r+1} = \binom{3n}{2n} \left(-\frac{1}{2x}\right)^{3n-2n} \cdot (x)^{2n}$$
$$= \frac{(3n)!}{x^1 (2^n)!} \cdot \frac{(-1)^n}{2^n} \cdot x^n$$

$$= \frac{(-1)^n}{2^n} \cdot \frac{(3n)!}{n!(2n)!} \cdot x^n \quad (2 \text{ marks})$$

**Q.10** **(4)**

$$\cot \theta = \sqrt{7} \Rightarrow \tan \theta = \frac{1}{\sqrt{7}}$$

$\tan \theta$  is +ve so  $\theta$  lies in IIIrd quad (1 mark)

$$\text{So } y = -1, \quad x = -\sqrt{7}$$

$$r^2 = x^2 + y^2$$

$$r^2 = 1 + 7$$

$$r^2 = 8$$

$$r = \sqrt{8} = 2\sqrt{2}$$

$$\sin \theta = y/r$$

$$\sin \theta = \frac{-1}{2\sqrt{2}}$$

$$\cos \theta = \frac{-\sqrt{7}}{2\sqrt{2}}$$

$$\operatorname{cosec} \theta = -2\sqrt{2}$$

$$\operatorname{cosec} \theta = \frac{-2\sqrt{2}}{\sqrt{7}} \quad (2 \text{ marks})$$

**Q.11** **(4)**

$$\cos 4x = \cos(2(2x))$$

$$= \cos^2 2x - \sin^2 2x \quad (1 \text{ mark})$$

$$= (\cos^2 x - \sin^2 x) - (2 \sin x \cos x)^2$$

$$= (\cos^2 x - \sin^2 x) - 4 \sin^2 x \cos^2 x \quad (1 \text{ mark})$$

$$= (2 \cos^2 x - 1) - 4(1 - \cos^2 x) \cos^2 x$$

$$= 4 \cos^4 x - 4 \cos^2 x + 1 - 4(1 - \cos^2 x) \cos^2 x$$

$$= 8 \cos^4 x - 8 \cos^2 x + 1 \quad (2 \text{ marks})$$

**Q.12** **(4)**

Given that  $r_1, r_2, r_3$  are all in an A.P, so

$$r_2 - r_1 = r_3 - r_2 \quad (1 \text{ mark})$$

$$\frac{\Delta}{s-b} - \frac{\Delta}{s-a} = \frac{\Delta}{s-c} - \frac{\Delta}{s-b}$$

$$\Delta \left( \frac{1}{s-b} - \frac{1}{s-a} \right) = \Delta \left( \frac{1}{s-c} - \frac{1}{s-b} \right) \quad (1 \text{ mark})$$

$$\Delta \left( \frac{s-a-s+b}{(s-a)(s-b)} \right) = \Delta \left( \frac{s-b-s+c}{(s-c)(s-b)} \right)$$

$$\frac{b-a}{s-a} = \frac{c-b}{s-c} \quad (1 \text{ mark})$$

$$\frac{a-b}{s-a} = \frac{b-c}{s-c}$$

$$(a-b)(s-c) = (b-c)(s-a) \quad (1 \text{ mark})$$

**Q.13** **(4)**

$$\cos^{-1}(2x^2 - 2x) = \frac{2\pi}{3}$$

$$(2x^2 - 2x) = \cos \frac{2\pi}{3} \quad (1 \text{ mark})$$

$$(2x^2 - 2x) = \cos 120^\circ$$

$$(2x^2 - 2x) = -\frac{1}{2}$$

$$4x^2 - 4x = 1 \quad (1 \text{ mark})$$

$$4x^2 - 4x + 1 = 0$$

$$a = 4, \quad b = -4, \quad c = 1$$

$$x = \frac{4 \pm \sqrt{16 - 16}}{8} \quad (1 \text{ mark})$$

$$x = \frac{4}{8} = \frac{1}{2}$$

$$\text{Hence } x = \frac{1}{2} \quad (1 \text{ mark})$$

**Q.14** **(4)**

$$\frac{1}{\sin^2 \theta} = \frac{4}{3}$$

$$\frac{1}{\sin \theta} = \pm \frac{2}{\sqrt{3}}$$

$$\sin \theta = \frac{\sqrt{3}}{2}, \quad \sin \theta = \frac{-\sqrt{3}}{2} \quad (1 \text{ mark})$$

Case I

$$\text{If } \sin \theta = \frac{\sqrt{3}}{2}$$

$$\theta = 60^\circ = \frac{\pi}{3} \quad (1 \text{ mark})$$

$\sin \theta$  is +ve so  $\theta$  lies in 1<sup>st</sup> and 2<sup>nd</sup> quadrant.

In 1<sup>st</sup> quadrant

$$\theta_1 = \theta$$

$$\theta_1 = \frac{\pi}{3}$$

In 2<sup>nd</sup> quadrant

$$\theta_2 = \pi - \theta$$

$$= \pi - \frac{\pi}{3}$$

$$\theta_2 = \frac{2\pi}{3} \quad (1 \text{ mark})$$



Case II

$$\sin \theta = \frac{-\sqrt{3}}{2}$$

$\sin \theta$  is -ve so  $\theta$  lies in IIIrd and 4<sup>th</sup> quadrant

In IIIrd quadrant

$$\theta_3 = \pi + \theta$$

$$= \pi + \frac{\pi}{3}$$

$$\theta_3 = \frac{4\pi}{3}$$

In 4th quadrant

$$\theta_4 = 2\pi - \theta$$

$$= 2\pi - \frac{\pi}{3}$$

$$\theta_4 = \frac{5\pi}{3}$$

(1 marks)

**Q.15**

**(4)**

Let  $\alpha, \beta$  be the roots of equation

$$x^2 - Px + q = 0 \quad \text{then}$$

(1 mark)

$$\alpha + \beta = -\frac{b}{a}$$

$$\boxed{\alpha + \beta = P}$$

$$\alpha \beta = \frac{c}{a}$$

$$\boxed{\alpha \beta = q}$$

(1 mark)

According to given problem

$$\alpha - \beta = 1$$

$$(\alpha - \beta)^2 = (1)^2$$

$$(\alpha - \beta)^2 = 1$$

(1 mark)

$$(\alpha + \beta)^2 - 4\alpha \beta = 1$$

$$P^2 - 4q = 1$$

$$\boxed{P^2 = 4q + 1}$$

(1 mark)

**SECTION C**

**Q.16**

**(8)**

$$x_1 + 3x_2 + 2x_3 = 3$$

$$4x_1 + 5x_2 - 3x_3 = -3$$

$$3x_1 - 2x_2 + 17x_3 = 42$$

$$A = \begin{pmatrix} 1 & 3 & 2 & : & 3 \\ 4 & 5 & -3 & : & -3 \\ 3 & -2 & 17 & : & 42 \end{pmatrix} \begin{matrix} R_2 - 4R_1 \\ R_3 - 3R_1 \end{matrix}$$

(1 mark)

$$= \begin{pmatrix} 1 & 3 & 2 & : & 3 \\ 0 & -7 & -11 & : & -15 \\ 0 & -8 & 11 & : & 33 \end{pmatrix} R_2 + R_3$$

(1 mark)

$$= \begin{pmatrix} 1 & 3 & 2 & : & 3 \\ 0 & 1 & 0 & : & -\frac{6}{5} \\ 0 & 0 & -\frac{11}{8} & : & -\frac{33}{8} \end{pmatrix} \quad \begin{array}{l} R_2 \\ -15 \\ -8 \end{array} \quad \begin{array}{l} R_3 \\ -8 \end{array} \quad (1 \text{ mark})$$

$$= \begin{pmatrix} 1 & 3 & 2 & : & 3 \\ 0 & 1 & 1 & : & -\frac{6}{5} \\ 0 & 0 & 0 & : & 3 \end{pmatrix} \quad R_3 \times \frac{-8}{11} \quad (1 \text{ mark})$$

$$= \begin{pmatrix} 1 & 0 & 2 & : & \frac{33}{5} \\ 0 & 1 & 0 & : & -\frac{6}{5} \\ 0 & 0 & 1 & : & 3 \end{pmatrix} \quad R_1 - 3R_2 \quad (1 \text{ mark})$$

$$= \begin{pmatrix} 1 & 0 & 0 & : & \frac{3}{5} \\ 0 & 1 & 0 & : & -\frac{6}{5} \\ 0 & 0 & 1 & : & 3 \end{pmatrix} \quad R_1 - 2R_3 \quad (1 \text{ mark})$$

Equations are (1 mark)

$$x_1 = \frac{3}{5}$$

$$x_2 = -\frac{6}{5}$$

$$x_3 = 3 \quad \text{S.S. } \left\{ \left( \frac{3}{5}, -\frac{6}{5}, 3 \right) \right\} \quad (1 \text{ mark})$$

**Q.17** (8)

$$\frac{1}{x^2(x^2+a^2)} = \frac{A}{x} + \frac{B}{x^2} + \frac{Cx+D}{x^2+a^2}$$

$$1 = Ax(x^2+a^2) + B(x^2+a^2) + (Cx+D)(x^2) \quad \text{-----I}$$

$$1 = A(x^3+a^2x) + B(x^2+a^2) + C(x^3) + D(x^2) \quad \text{-----II}$$

Put  $x = 0$  in equation I (2 marks)

$$1 = B(0+a^2)$$

$$1 = a^2B \quad \Rightarrow \quad B = \frac{1}{a^2} \quad (1 \text{ mark})$$

Comparing the co-efficients of like powers of 'x'

$$0 = A+C \quad \text{-----III}$$

$$0 = B+D \quad \text{-----IV}$$

$$0 = a^2A \quad \text{-----V}$$

$$\text{Eq -V} \Rightarrow A = 0$$

$$\text{Put } A = 0 \text{ in III} \Rightarrow 0 = 0 + C$$

$$C = 0$$

$$\text{Put } B = \frac{1}{a^2} \text{ in IV}$$

$$0 = \frac{1}{a^2} + D \quad D = \frac{-1}{a^2} \quad (3 \text{ marks})$$

$$\frac{1}{x^2(x^2+a^2)} = \frac{0}{x} + \frac{1}{a^2x^2} + \frac{0x - \frac{1}{a^2}}{x^2+a^2}$$

$$= \frac{1}{a^2x^2} - \frac{1}{a^2(x^2+a^2)} \quad (2 \text{ marks})$$

**Q.18** **(8)**

First '99' positive integers are 1, 2, 3, .....99

$$S_n = \frac{n}{2}[2a + (n-1)d]$$

$$S_{99} = \frac{99}{2}[2 \times 1 + (99-1) \times 1]$$

$$S_{99} = \frac{99}{2}[2 + 98]$$

$$S_{99} = \frac{99}{2} \times 100$$

$$S_{99} = 99 \times 50$$

$$S_{99} = 4950$$

(3 marks)

Now, sum of numbers like 7+17+27+37.....97

$$S_n = \frac{n}{2}[2a + (n-1)d]$$

$$S_{10} = \frac{10}{2}[2 \times 7 + (10-1) \times 10]$$

$$S_{10} = 5[14 + 90]$$

$$S_{10} = 5 \times 104$$

$$S_{10} = 520$$

(3 marks)

Also sum of the numbers like 70+71+72+73+74+75+76+78+79

$$= 668$$

(1 mark)

$$\text{Required sum} = 4950 - 520 - 668$$

$$= 3762$$

(1 mark)

**Q.19** **(8)**

We have

$$(1+x)^n = 1 + nx + \frac{n(n-1)}{2!}x^2 + \frac{n(n-1)(n-2)}{3!}x^3 + \dots$$

$$(1-P)^5 = 1 + 5(-P) + \frac{5(4)}{2!}(-P)^2 + \frac{5(4)(3)}{3!}(-P)^3 + \dots$$

$$= 1 - 5P + 10P^2 - 10P^3 + \dots$$

(3 marks)

Put  $P = x+x^2$  in above expression

$$\begin{aligned}
 [1 - (x + x^2)]^5 &= 1 - 5(x + x^2) + 10(x + x^2)^2 + \dots \\
 &= 1 - 5x - 5x^2 + 10(x^2 + 2x^3 + \dots) \\
 &= 1 - 5x - 5x^2 + 10x^2 + 20x^3 + \dots \\
 &= 1 - 5x + 5x^2 + 20x^3 + \dots
 \end{aligned}$$

(3 marks)

New  $(0.9899)^5 = (1 - 0.0101)^5$

$$\begin{aligned}
 &= 1 - 5(+0.0101) + 10(-0.0101)^2 \\
 &= 1 - 0.0505 + 0.00102 \\
 &= 0.9495
 \end{aligned}$$

(2 marks)

**Q.20** **(8)**

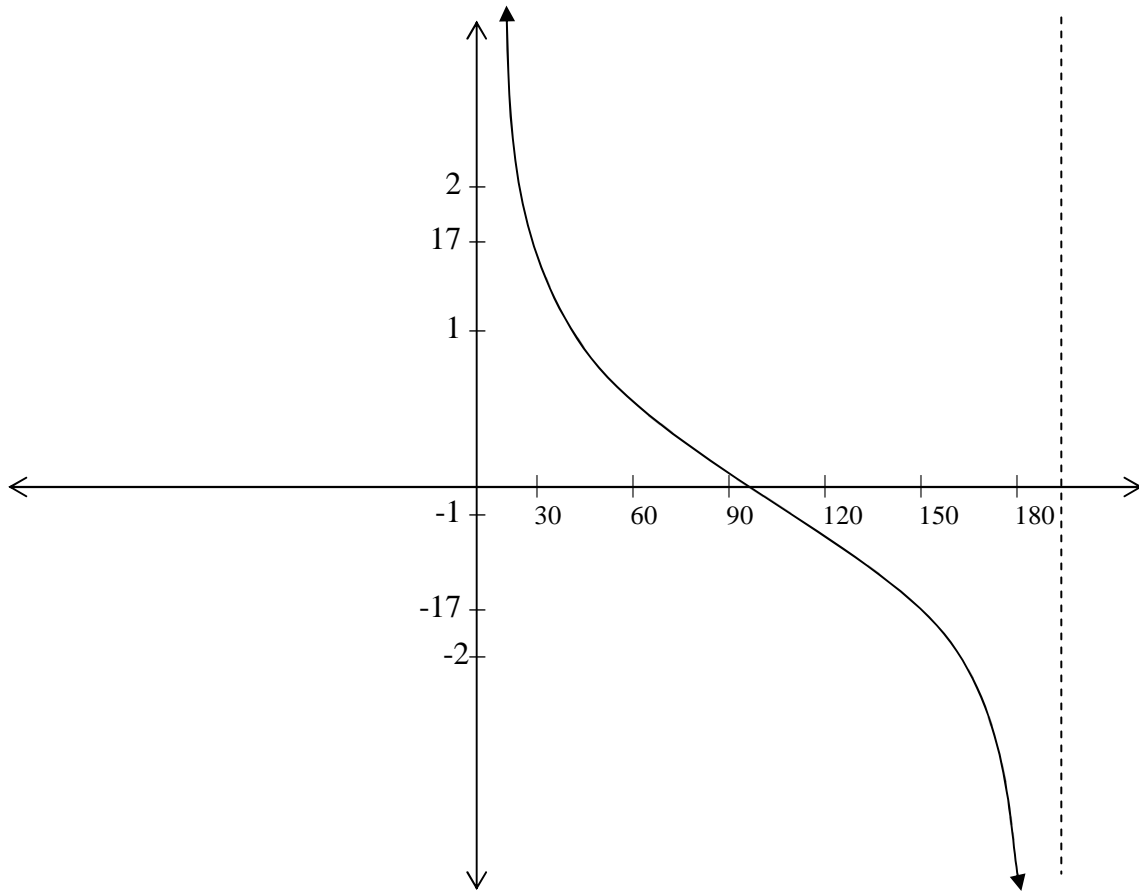
$$y = \cot x \quad x \in [0, \pi]$$

Period of  $\cot x$  is  $\pi$  so complete period

Is 0 to  $\pi$  (2 marks)

$x$	0	$\frac{\pi}{6}$	$\frac{\pi}{3}$	$\frac{\pi}{3}$	$\frac{\pi}{2} - 0$	$\frac{2\pi}{2} + 0$	$\frac{5\pi}{3}$	$\pi$
$y$	$\pm\infty$	1.73	0.58	$\infty$	$-\infty$	-0.58	1.73	$+\infty$

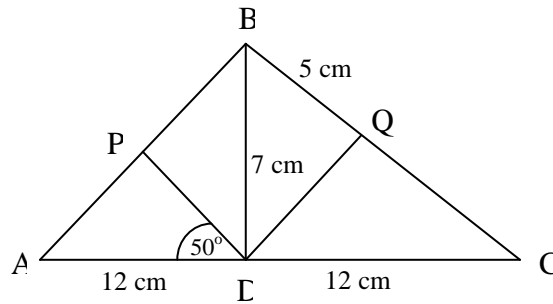
(2 marks)



(4 marks)

Q.21

(8)



I. In  $\triangle APD$

$$\angle \hat{P}AD + 50^\circ + 90^\circ = 180^\circ$$

$$\angle \hat{P}AD = 40^\circ$$

$$\angle \hat{P}AD = \angle \hat{B}AD = 40^\circ$$

(2 marks)

II.

$$\angle \hat{P}AB = 40^\circ$$

In  $\triangle BPD$

$$\cos 40^\circ = \frac{PD}{7}$$

$$PD = 7 \cos 40^\circ$$

$$PD =$$

(2 marks)

III.

$$DQ = ?$$

In  $\triangle BDQ$

$$(BD)^2 = (BQ)^2 + (DQ)^2$$

$$49 = 25 + (DQ)^2$$

$$DQ = \sqrt{24}$$

(2 marks)

IV.

$$CQ = ?$$

In  $\triangle DQC$

$$(DC)^2 = (DQ)^2 + (CQ)^2$$

$$(12)^2 = (\sqrt{24})^2 + (CQ)^2$$

$$(CQ)^2 = 144 - 24$$

$$(CQ)^2 = 120$$

$$(CQ) = \sqrt{120}$$

(2 marks)

Q.22

(8)

Solve the given equations.

$$x^2 - y^2 = 5 \text{ -----I} \qquad 4x^2 - 3xy = 18 \text{ -----II} \qquad (1 \text{ mark})$$

Multiply eq 1 by 18 and eq 2 by 5 and then subtracting

$$\begin{array}{r} 18x^2 - 18y^2 = 90 \\ -20x^2 \pm 15xy = -90 \\ \hline -2x^2 \pm 15xy - 18y^2 = 0 \end{array}$$

(1 mark)

$$2x^2 - 15xy + 18y^2 = 0$$

$$2x^2 - 12xy - 3xy + 18y^2 = 0$$

$$2x(x - 6y) - 3y(x - 6y) = 0$$

$$(x - 6y)(2x - 3y) = 0$$

$$x - 6y = 0 \qquad 2x - 3y = 0$$

$$x = 6y \qquad 2x = 3y$$

$$x = 6y \text{ ----- III} \qquad x = \frac{3}{2}y \text{ ----- IV}$$

(1 mark)

Put  $x = 6y$  in eq ----- I

$$(6y)^2 - y^2 = 5$$

$$36y^2 - y^2 = 5$$

$$35y^2 = 5$$

$$y^2 = \frac{1}{7}$$

$$y = \pm \frac{1}{\sqrt{7}}$$

Put  $y = \pm \frac{1}{\sqrt{7}}$  in eq III

$$x = 6\left(\pm \frac{1}{\sqrt{7}}\right)$$

$$x = \pm \frac{6}{\sqrt{7}}$$

Put  $x = \frac{3}{2}y$  in

eq ----- I

$$\left(\frac{3}{2}y\right)^2 - y^2 = 5$$

$$\frac{9}{4}y^2 - y^2 = 5$$

$$9y^2 - 4y^2 = 20$$

$$5y^2 = 20$$

$$y^2 = 4$$

$$y = \pm 2$$

Put  $y = \pm 2$  in eq IV

$$x = \frac{3}{2}(\pm 2)$$

$$x = (\pm 3)$$

(4 marks)

$$S.S. = \left\{ \left( \frac{6}{\sqrt{7}}, \frac{1}{\sqrt{7}} \right), \left( \frac{-6}{\sqrt{7}}, \frac{-1}{\sqrt{7}} \right), (3, 2), (-3, -2) \right\}$$

(1 mark)

The End