

### **The Law of Cosine**

$$\begin{array}{l} \circ a^2 = b^2 + c^2 - 2bc \cos \alpha \\ \circ \cos \alpha = \frac{b^2 + c^2 - a^2}{2bc} \end{array} \quad \begin{array}{l} \circ b^2 = c^2 + a^2 - 2ca \cos \beta \\ \circ \cos \beta = \frac{c^2 + a^2 - b^2}{2ca} \end{array} \quad \begin{array}{l} \circ c^2 = a^2 + b^2 - 2ab \cos \gamma \\ \circ \cos \gamma = \frac{a^2 + b^2 - c^2}{2ab} \end{array}$$

### **The Law of Sine**

$$\circ \frac{a}{\sin \alpha} = \frac{b}{\sin \beta} = \frac{c}{\sin \gamma}$$

### **The Law of Tangent**

$$\circ \frac{a-b}{a+b} = \frac{\tan\left(\frac{\alpha-\beta}{2}\right)}{\tan\left(\frac{\alpha+\beta}{2}\right)} \quad \circ \frac{b-c}{b+c} = \frac{\tan\left(\frac{\beta-\gamma}{2}\right)}{\tan\left(\frac{\beta+\gamma}{2}\right)} \quad \circ \frac{c-a}{c+a} = \frac{\tan\left(\frac{\gamma-\alpha}{2}\right)}{\tan\left(\frac{\gamma+\alpha}{2}\right)}$$

### **Half Angles Formulas**

$$\begin{array}{lll} \circ \sin \frac{\alpha}{2} = \sqrt{\frac{(s-b)(s-c)}{bc}} & \circ \sin \frac{\beta}{2} = \sqrt{\frac{(s-c)(s-a)}{ca}} & \circ \sin \frac{\gamma}{2} = \sqrt{\frac{(s-a)(s-b)}{ab}} \\ \circ \cos \frac{\alpha}{2} = \sqrt{\frac{s(s-a)}{bc}} & \circ \cos \frac{\beta}{2} = \sqrt{\frac{s(s-b)}{ca}} & \circ \cos \frac{\gamma}{2} = \sqrt{\frac{s(s-c)}{ab}} \\ \circ \tan \frac{\alpha}{2} = \sqrt{\frac{(s-b)(s-c)}{s(s-a)}} & \circ \tan \frac{\beta}{2} = \sqrt{\frac{(s-c)(s-a)}{s(s-b)}} & \circ \tan \frac{\gamma}{2} = \sqrt{\frac{(s-a)(s-b)}{s(s-c)}} \end{array}$$

where  $s = \frac{a+b+c}{2}$

### **Area of Triangle ( $= \Delta$ )**

$$\begin{array}{l} \circ \Delta = \frac{1}{2}bc \sin \alpha = \frac{1}{2}ca \sin \beta = \frac{1}{2}ab \sin \gamma \\ \circ \Delta = \frac{a^2 \sin \beta \sin \gamma}{2 \sin \alpha} = \frac{b^2 \sin \gamma \sin \alpha}{2 \sin \beta} = \frac{c^2 \sin \alpha \sin \beta}{2 \sin \gamma} \\ \circ \Delta = \sqrt{s(s-a)(s-b)(s-c)} \quad (\text{Hero's Formula}) \end{array}$$

### **Circum Radius ( $= R$ )**

$$\circ R = \frac{a}{2 \sin \alpha} = \frac{b}{2 \sin \beta} = \frac{c}{2 \sin \gamma} \quad \circ R = \frac{abc}{4\Delta}$$

### **In Radius ( $= r$ )**

$$\circ r = \frac{\Delta}{s}$$

### **Escribed Circle**

$$\circ r_1 = \frac{\Delta}{s-a} \quad \circ r_2 = \frac{\Delta}{s-b} \quad \circ r_3 = \frac{\Delta}{s-c}$$