

Chapter 6 (Objectives)

SEQUENCE AND SERIES

TEXTBOOK OF ALGEBRA AND TRIGONOMETRY FOR CLASS XI

Item 1: Fill in the blanks (Completion Items)

1. Sequences are also called _____.
2. Sequence is denoted by _____.
3. An _____ sequence has no last term.
4. The difference between two consecutive terms in A.P. is called the _____.
5. If $\{a_n\}$ is an _____ then $a_n - a_{n-1} = d$ for $n > 0$.
6. $a_n = a + (n-1)d$ is called _____ or general term of an A.P.
7. If a, A, b are in A.P then $A - a =$ _____.
8. A.M between a_{n-1} and a_{n+1} is _____.
9. If all terms of the sequence are real number then it is called _____ sequence.
10. Finite series has _____ number of terms.
11. $S_{2n} = n(a_1 + a_{2n})$ denotes the sum of _____ terms in A.P.
12. Infinite series has _____ number of terms.
13. If a_n is the A.M. between a_{n-1} and a_{n+1} then $a_n =$ _____.
14. _____ can not be terms in G.P.
15. The common ratio $\frac{a_n}{a_{n-1}}$ exists if $a_{n-1} \neq$ _____.
16. $a_n = ar^{n-1}$ is called general term of a _____.
17. If a, G, b are in G.P. then $\frac{G}{a} =$ _____.
18. If a, G, b are in G.P. then $G^2 =$ _____.
19. If $\{a_n\}$ is a G.P. then $S_n = \frac{a(1-r^n)}{1-r}$ when $r \neq$ _____.
20. If G_1, G_2, \dots, G_n are n G.P. between a and b then $\sqrt[n]{G_1 \cdot G_2 \cdot \dots \cdot G_n} =$ _____.
21. When $\lim_{n \rightarrow \infty} S_n$ does not exist, the series is said to be _____.
22. If S_n exists when $n \rightarrow \infty$ then the series is said to be _____.
23. Middle term of three consecutive terms in A.P. is the _____ between the extreme terms.
24. _____ can not be the term of H.P.
25. If a, H, b are in H.P. then $H =$ _____.
26. $1^3 + 2^3 + 3^3 + \dots + n^3 =$ _____.
27. The next term of the sequence 7, 9, 12, 16, is _____.
28. The 5th term of G.P. 3, 6, 12, is _____.
29. G.M. between $\frac{1}{-2i}$ and $\frac{1}{8i}$ is _____.
30. The sum of infinite geometric series $2, \sqrt{2}, 1, \dots$ is _____.
31. The general term of the series $1^2 + 3^2 + 5^2 + \dots$ is _____.
32. The 12th term of $\frac{1}{2}, \frac{1}{5}, \frac{1}{8}, \dots$ is _____.
33. The G.M. between $-2i$ and $8i$ is _____.
34. $1 + 3 + 5 + \dots$ to n terms, can be written as $\sum_{k=1}^n$ _____.
35. If $a_n = (-1)^{n+1}$ then its 21st term is _____.
36. If A_1, A_2, A_3 are in H.P. then $\frac{1}{A_1}, \frac{1}{A_2}, \frac{1}{A_3}$ are in _____.

37. $\frac{ab(n+1)}{b+na}$ is the n th _____ between a and b .
38. For any two distinct _____ real numbers $A > G > H$.
39. The infinite Geometric series converges if $|r|$ _____.
40. The n th term of the sequence $\left(\frac{1}{3}\right)^2, \left(\frac{2}{3}\right)^2, \left(\frac{3}{3}\right)^2, \dots$, is _____.
41. If $S_n \rightarrow a$ limit as $n \rightarrow \infty$ then the series is said to be _____.

Item 2: True or False

- A sequence is a special type of a function from a subset of \mathbb{N} to \mathbb{N} or \mathbb{C} .
- In real sequence, all the terms must be real numbers.
- Sequence is denoted by a_n .
- Finite sequence has limited number of terms.
- An infinite sequence has no last term.
- The first four terms of the sequence $\{2n-3\}$ are -1, 1, 3, 4.
- A sequence $\{a_n\}$ is an A.P. if $a_n - a_{n-1} = d$ for all $n \in \mathbb{N}$ and $n > 0$.
- $a_n = a + (n+1)d$ is n th term of G.P.
- If $a = 3, d = 7$ in the A.P. then $a_n = 10 + 7n$.
- If a, A, b are in A.P. then $A = \frac{a+b}{2}$.
- A.M. between -1 and 1 is 0.
- $a + (a+d) + (a+2d) + \dots + a + (n-1)d$ is an A.P.
- A finite series has infinite number of terms.
- Infinite series has unlimited number of terms.
- For any sequence $\{a_n\}$, $S_n = a_1 + a_2 + a_3 + \dots + a_{n-1}$.
- If $\{a_n\}$ is an A.P. then $S_n = \frac{n}{2}(a_1 + a_n)$.
- n (number of term) can not be negative.
- Geometric sequence and Geometric progression are two types of sequence.
- In G.P. $\frac{a_n}{a_{n-1}} = r$ for all $n \in \mathbb{N}$ and $n > 0$.
- $r = \frac{a_n}{a_{n-1}}$ exists when $a_{n-1} \neq 0$.
- No term of G.P is zero.
- 6th term of G.P. 3, 6, 12, 24, is 96.
- If a, G, b are in G.P then $G^2 = \pm \sqrt{ab}$.
- 0, 2, 4, 8, is a G.P.
- G.M. between 4 and 16 is ± 8 .
- $S_\infty = \frac{a}{1-r}$ exists when $|r| < 1$.
- $\lim_{n \rightarrow \infty} r^n = 0$ when $|r| < 1$.
- Infinite geometric series converges for $|r| < 1$.
- The sequence $1, \frac{1}{2}, \frac{1}{3}, \frac{1}{4}, \dots$ is a H.P.
- If a, H, b are in H.P. then $H = \frac{2ab}{a+b}$.
- $\sqrt{a} - \sqrt{b}$ is a real number where $a, b \in \mathbb{R}$.

32. $1+2+3+\dots+n = \frac{n(n+1)}{6}$
33. $1^2+2^2+3^2+\dots+n^2 = \frac{n(n+1)(n+2)}{6}$.
34. Term of the sequence are in definite order.
35. A sequence is said to be a function from set \mathbb{R} to set \mathbb{N} .
36. Domain of the sequence is some time taken as the set of whole numbers.
37. There are one-one correspondence between the set of natural numbers and the terms of a sequence.
38. If $1,3,5,\dots$ is the sequence then $a_n = 2n + 1$.
39. In an A.P. ratio of any two consecutive terms is same.
40. $G_n = a \left(\frac{b}{a} \right)^{\frac{n}{n+1}}$ is the n th G.Ms between a and b .
41. If a, b, c and d are in G.P. then $b^2 = ac$ and $c^2 = bd$.
42. If the population of village increase geometrically at the rate of 4% annually then $r = 1 + 0.004$.
43. For any two distinct negative real numbers a and b , $A > G > H$.
44. $a_1 - a_1 + a_1 - a_1 + a_1 - a_1 + \dots$ is called an oscillatory series.

ANSWERS

Item I: Fill in the Blanks

- 1.** Progressions **2.** $\{a_n\}$ **3.** Infinite **4.** Common difference **5.** A.P.
- 6.** n th term **7.** $b - A$ **8.** $\frac{a_{n-1} + a_{n+1}}{2}$ **9.** Real **10.** Finite **11.** $2n$
- 12.** Infinite **13.** $\frac{a_{n-1} + a_{n+1}}{2}$ **14.** Zero **15.** Zero **16.** G.P. **17.** $\frac{b}{G}$
- 18.** ab **19.** 1 (One) **20.** \sqrt{ab} **21.** Divergent **22.** Convergent **23.** A.M.
- 24.** Zero **25.** $\frac{2ab}{a+b}$ **26.** $\frac{n^2(n+1)^2}{4}$ **27.** 21 **28.** 48 **29.** $\frac{1}{4}$
- 30.** $4 + 2\sqrt{2}$ **31.** $(2n-1)^2$ **32.** $\frac{1}{35}$ **33.** 4 **34.** $(2k-1)$ **35.** 1
- 36.** A.P. **37.** H.M. **38.** positive **39.** less than 1 **40.** $\left(\frac{n}{3}\right)^2$ **41.** Convergent

Item 2: True or False

- 1.** False **2.** True **3.** False **4.** True **5.** True **6.** False
- 7.** True **8.** False **9.** False **10.** True **11.** True **12.** False
- 13.** False **14.** True **15.** False **16.** True **17.** True **18.** False
- 19.** True **20.** False **21.** True **22.** True **23.** False **24.** False
- 25.** True **26.** False **27.** False **28.** True **29.** True **30.** True
- 31.** True **32.** False **33.** True **34.** True **35.** False **36.** True
- 37.** True **38.** False **39.** False **40.** True **41.** True **42.** False
- 43.** False **44.** True

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