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Exercise 7.5 (Solutions)

Textbook of Algebra and Trigonometry for Class XI Available online @ http://www.mathcity.org, Version: 3.0

For the following experiments, find the probability in each case:

Question # 1

Experiment:

From a box containing orange-flavoured sweets, Bilal takes out one sweet without looking.

Events happening:

- the sweet is orange-flavoured the sweet is lemon-flavoured (ii) Total possible outcomes = n(S) = 1Solution
- Suppose A is the event that sweet is orange flavoured. Since box only contained orange flavoured sweets So favourable outcomes = n(A) = 1

Probability =
$$P(A) = \frac{n(A)}{n(S)} = \frac{1}{1} = 1$$

(ii) Let B be the event that the sweet is lemon-flavoured. Since box only contained orange-flavoured sweet So favourable outcomes = n(B) = 0

Probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{0}{1} = 0$$

Question #2

Experiment:

Pakistan and India play a cricket match. The result is:

Pakistan wins (ii) India does not lose.

Solution Since there are three possibilities that Pakistan wins, loses or the match tied.

Therefore possible outcomes = n(S) = 3

Let A be the event that Pakistan wins (i) Favourable outcomes = n(A) = 1

$$n(A) = n(A)$$

Required probability = $P(A) = \frac{n(A)}{n(S)} = \frac{1}{3}$

(ii) Let B be the event that India does not lose.

If India does not lose then India may win or the match tied

Therefore favourable outcomes = n(B) = 2

Required probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{2}{3}$$

Question #3

Experiment:

There are 5 green and 3 red balls in a box, one ball is taken out.

Event happening

(i) the ball is green

(ii) the ball is red

Solution Total number of balls = 5 + 3 = 8

Therefore possible outcomes = n(S) = 8

(i) Let A be event that the ball is green Then favourable outcomes = n(A) = 5

So probability = $P(A) = \frac{n(A)}{n(S)} = \frac{5}{8}$

(ii) Let B be the event that the ball is red Then favourable outcomes = n(B) = 3

So probability = $P(A) = \frac{n(B)}{n(S)} = \frac{3}{8}$

Question #4

Experiment:

A fair coin is tossed three times. It shows

Event happening

(i) One tail

(ii) atleast one head

Solution When a fair coin is tossed three times, the possible outcomes are HHH, HHT, HTH, THH, HTT, THT, TTH, TTT.

So total possible outcomes = n(S) = 8

(i) Let *A* be the event that the coin shows one tail then favourable outcomes are HHT, HTH, THH,

i.e.
$$n(A) = 3$$

So required probability = $P(A) = \frac{n(A)}{n(S)} = \frac{3}{8}$

(ii) Let *B* be the event that coin shows at least one head then favourable outcomes are

HHH, HHT, HTH, THH, HTT, THT, TTH.

i.e.
$$n(B) = 7$$

So required probability = $P(B) = \frac{n(B)}{n(S)} = \frac{7}{8}$

Question # 5

Experiment:

A die is rolled. The top shows

Event happening

(i) 3 or 4 dots

(ii) dots less than 5

Solution The possible outcomes are that die show 1, 2, 3, 4, 5, 6. So possible outcomes = n(S) = 6

(i) Let A be the event that die show 3 or 4.

Then favourable outcomes = n(A) = 2

So required probability =
$$P(A) = \frac{n(A)}{n(S)} = \frac{2}{6} = \frac{1}{3}$$

(ii) Let *B* be the event that top of the die show dots less than 5 then Favourable outcomes = n(B) = 4

So required probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{4}{6} = \frac{2}{3}$$

Question #6

Experiment:

From a box containing slips numbered 1,2,3,...,5 one slip is picked up Event happening

- (i) The number on the slip is a prime number
- (ii) The number on the slip is a multiple of 3.

Solution Since the box contain 5 slips So possible outcomes = n(S) = 5

(i) Let A be the event that the number on the slip are prime numbers 2, 3 or 5 Then favourable outcomes = n(A) = 3

So required probability =
$$P(A) = \frac{n(A)}{n(S)} = \frac{3}{5}$$

(ii) Let *B* be the event that number on the slips are multiple of 3 then Favourable outcomes = n(B) = 1

So probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{1}{5}$$

Question #7

Experiment:

Two dice, one red and the other is blue, are rolled simultaneously. The numbers of dots on the tops are added. The total of the two scores is:

Event happening

(i) 5 (ii) 7 (iii) 11

Solution When two dice are rolled, the possible outcomes are
$$(1, 1) \quad (1, 2) \quad (1, 3) \quad (1, 4) \quad (1, 5) \quad (1, 6)$$

$$(2, 1) \quad (2, 2) \quad (2, 3) \quad (2, 4) \quad (2, 5) \quad (2, 6)$$

$$(3, 1) \quad (3, 2) \quad (3, 3) \quad (3, 4) \quad (3, 5) \quad (3, 6)$$

$$(4, 1) \quad (4, 2) \quad (4, 3) \quad (4, 4) \quad (4, 5) \quad (4, 6)$$

$$(5, 1) \quad (5, 2) \quad (5, 3) \quad (5, 4) \quad (5, 5) \quad (5, 6)$$

$$(6, 1) \quad (6, 2) \quad (6, 3) \quad (6, 4) \quad (6, 5) \quad (6, 6)$$
This show possible outcomes = $n(S) = 36$

(i) Let A be the event that the total of two scores is 5 then favourable outcome are (1, 4), (2, 3), (3, 2), (4, 1)

i.e. favourable outcomes = n(A) = 4

So required probability =
$$P(A) = \frac{n(A)}{n(S)} = \frac{4}{36} = \frac{1}{9}$$

(ii) Let B be the event that the total of two scores is 7 then favourable outcomes are

$$(1, 6), (2, 5), (3, 4), (4, 3), (5, 2), (6, 1)$$

i.e. favourable outcomes = n(B) = 6

So probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{6}{36} = \frac{1}{6}$$

(iii) Let C be the event that the total of two score is 11 then favourable outcomes are (5, 6), (6, 5) i.e. n(C) = 2

So probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{2}{36} = \frac{1}{18}$$

Question #8

Experiment:

A bag contain 40 balls out of which 5 are green, 15 are black and the remaining are yellow, A ball is taken out of the bag.

Event happening

(i) The ball is black (ii) The ball is green (iii) The ball is not green.

Solution Total number of balls = 40 i.e. n(S) = 40Black balls = 15, Green balls = 5, Yellow balls = 40 - (15+5) = 20

(i) Let A be the event that the ball is black then n(A) = 15

So required probability =
$$P(A) = \frac{n(A)}{n(S)} = \frac{15}{40} = \frac{3}{8}$$

(ii) Let B denotes the event that the ball is green then n(B) = 5

So required probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{5}{40} = \frac{1}{8}$$

Let C denotes the event that the ball is not green then ball is either black or yellow therefore favourable outcomes = n(C) = 15 + 20 = 35

So required probability =
$$P(C) = \frac{n(C)}{n(S)} = \frac{35}{40} = \frac{7}{8}$$

Question #9

Experiment:

One chit out of 30 containing the names of 30 students of a class of 18 boys and 12 girls is taken out at random, for nomination as the monitor of the class. Event happening

- (i) The monitor is the boy (ii) The monitor is the girl.
- **Solution** Number of students = 30 Then possible outcomes = n(S) = 30

(i) Now if A be the event that the monitor is the boy then Favourable outcomes = n(A) = 18

So probability =
$$P(A) = \frac{n(A)}{n(S)} = \frac{18}{30} = \frac{3}{5}$$

(ii) Now if *B* be the event that the monitor is the girl then Favourable outcomes = n(B) = 12

So probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{12}{30} = \frac{2}{5}$$

Question # 10

Experiment:

A coin is tossed four times. The top show

Event happening

(i) All heads

(ii) 2 head and 2 tails.

Solution When the coin is tossed four times the possible outcomes are

HHHT	HHTH	HTHH	THHH
HHTT	HTTH	TTHH	THHT
HTTT	TTTH	TTHT	THTT
TTTT	HHHH	THTH	HTHT

i.e. n(S) = 16

(i) Let A be the event that the top shows all head then favourable outcome is HHHH i.e. n(A) = 1

Now probability =
$$P(A) = \frac{n(A)}{n(S)} = \frac{1}{16}$$

(ii) Let *B* be the event that the top shows 2 head and two tails the favourable outcomes are HHTT, HTTH, TTHH, THHT, THTH, HTHT

i.e.
$$n(B) = 6$$

Now probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{6}{16} = \frac{3}{8}$$

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