

# University of Sargodha

B.A/B. Sc 1<sup>st</sup> Annual Examination 2012.

Applied Math

Paper: A

Available at  
www.mathcity.org

Maximum Marks: 100

Time Allowed: 3 Hours

Note: Attempt any two questions from each section.

### Section-I

- Q.1. a. Solve the initial value problem  $\frac{dy}{dx} = \frac{x(x^2+1)}{4y^3}$   $y(0) = \frac{-1}{\sqrt{2}}$  (8)  
 b. Solve the equation.  $(D^2 + 6D + 9)y = 0$   $y(0) = 2$   $y'(0) = -3$  (9)
- Q.2. a. Solve differential equation.  $\frac{dy}{dx} = \frac{x+3y-5}{x-y-1}$  (8)  
 b. Solve by the method of U.C  $y'' - 4y' + 4y = e^{2x}$  (9)
- Q.3. a. Solve  $(1+x^2)\frac{dy}{dx} + 4xy = \frac{1}{(1+x^2)^2}$  (8)  
 b. Solve  $x^2\frac{d^2y}{dx^2} + 7x\frac{dy}{dx} + 5y = x^5$  (9)
- Q.4. a. Find orthogonal trajectories of family of cardioids.  $r = a(1 + \cos\theta)$  (8)  
 b. Find a series solution of differential equation around indicated point  $y'' - x^2y = 0$  around  $x = 0$  (9)

### Section-II

- Q.5. a. Compute the Laplace transformation of  $\cos^2 at$  (8)  
 b. Compute the inverse Laplace transformation of  $\frac{9s-67}{s^2-16s+49}$  (8)
- Q.6. a. Using Newfon Raphson method find a root of  $f(x) = x^3 - 2x - 5 = 0$  (8)  
 b. Solve the transcendental equation  $f(x) = e^{-x} - \sin\left(\frac{\pi x}{2}\right) = 0$  to a positive real root by Bisection method. (8)
- Q.7. a. Use the trapezoidal rule with  $n = 4$  to approximate.  $I = \int_0^4 \sqrt{x^2 + 1} dx$  (8)  
 b. Use Simpson's rule to approximate the Integral  $\int_1^2 \ln x dx$  with  $n = 4$ . (8)
- Q.8. a. Find the first and second order derivatives of the function from the following data at  $x = 2$ . (8)
- |        |   |    |    |    |     |
|--------|---|----|----|----|-----|
| $x$    | 1 | 2  | 3  | 4  | 5   |
| $f(x)$ | 3 | 10 | 29 | 66 | 127 |
- b. Find a bound on the error in approximating the given integral using:  
 i. Trapezoidal rule      ii. Simpson's rule.  $\int_{-1}^2 x^5 dx$  with  $n = 10$  (8)

### Section-III

- Q.9. a. Minimize  $z = 2x_1 + x_2$  subject to the conditions (9)  
 $x_1 + x_2 \geq 1$   
 $x_1 - x_2 \geq -1$   
 $x_1 + 2x_2 \geq 4$   
 $x_1, x_2 \geq 0$
- b. Use the simplex method to find the maximum value of object function  $z = 10x_1 + 11x_2$  with the condition (8)  
 $3x_1 + 4x_2 \leq 9$   
 $5x_1 + 2x_2 \leq 8$   
 $x_1 + 2x_2 \leq 1$   
 $x_1 \geq 0$  and  $x_2 \geq 0$
- Q.10. a. A set of eight cards contains one joker. A and B are two players and A choose 5 cards at random, B taking the remaining 3 cards. What is the probability that A has the joker? (8)  
 b. A pair of fair dice is thrown. If the two numbers appearing are different, find the probability that sum is (i) 6 (ii) sum is 4 or less. (9)
- Q.11. a. If  $f(x) = \frac{1}{n}(x = 1, 2, 3 \dots \dots \dots n)$  then find  $E(x)$  and  $Var(x)$  (8)  
 b. Suppose that the life length (in hours) of a certain radio tube is continuous random variable  $x$  with probability density function  $f(x) = \frac{100}{x^2}$   $x > 100$  (9)  
 And zero elsewhere. What is the probability that a tube will last less than 200 hours, if it is known that tube is still functioning after 150 hours of service?
- Q.12. a. An event has the probability  $P = 3/8$ , Find the complete Binomial distribution for  $n = 5$  trials? (9)  
 b. Let  $X$  be random variable having a binomial distribution with parameters  $n = 25$  and  $P = 0.2$  evaluate  $P[X < \mu - 2\sigma]$  (8)