

Group

(Abelian Group)

w.r.t

“ Subtraction ”

&

“ Division ”

By # Prof: Fazal Abbas Sajid

- Many Students consider that there is no group w.r.t (Subtraction and Division)
- Even that **Google Search** shows these wrong informations

Remember Dear Students :

- ❖ Set $\{0\}$ is abelian Group w.r.t “ $-$ ”
- ❖ Set $\{1\}$ is abelian Group w.r.t “ \div ”

Google does not know these important informations

🌸🌸🌸 I say “ Google koi hadees to nhi ”

🌸🌸🌸 I also say “Google is just artificial Storage (USB) ”

ALLAH PAK ka ata kya gya Dimagh (Brain) to nhi

🌸🌸🌸 Google can show just that results only which are uploaded by any person on Google

- 🌸 I am infinity times grateful to

ALLAH ALMIGHTY and MUHAMMAD (ﷺ)

to become me **1st Person** to introduce these important hidden informations **1st time in the World**

Regards: Prof. Fazal Abbas Sajid

Proof of Group

(Abelian Group)

w.r.t

“ Subtraction ”

&

“ Division ”

By # Prof:Fazal Abbas Sajid

Alhamdulillah I am **1st Person in the World** who introduced this
concept **1st Time in the World**

Abelian group w.r.t “ Subtraction ”

Let $A = \{0\}$

G1 # Clouser Law :

As $0 - 0 = 0 \in A$ hence Clouser Law hold

G2 # Associative Law :

$$(0 - 0) - 0 = 0 - (0 - 0)$$

Hence Associative Law hold

G3 # Existence of Identity Element :

“ 0 ” is subtractive identity and $0 \in A$,

$$\text{s.t } 0 - 0 = 0 = 0 - 0$$

Hence subtractive identity exist in A

G4 # Existence of Inverse of Element :

“ 0 ” is subtractive inverse of itself ,

$$\text{s.t } 0 - 0 = 0 = 0 - 0$$

Hence subtractive inverse of each exist in A

G5 # Commutative Law :

$$\text{as } 0 - 0 = 0 - 0$$

Hence commutative law hold

G1 to G4 indicates Set A is group w.r.t “ - ”

G1 to G5 indicates Set A is abelian group w.r.t “ - ”

Abelian group w.r.t “ Division ”

Let $B = \{1\}$

G1 # Clouser Law :

As $1 \div 1 = 1 \in B$ hence Clouser Law hold

G2 # Associative Law :

$$(1 \div 1) \div 1 = 1 \div (1 \div 1)$$

Hence Associative Law hold

G3 # Existence of Identity Element :

“ 1 ” is divisive identity and $1 \in B$,

$$\text{s.t } 1 \div 1 = 1 = 1 \div 1$$

Hence divisive identity exist in B

G4 # Existence of Inverse of Element :

“ 1 ” is divsive inverse of itself ,

$$\text{s.t } 1 \div 1 = 1 = 1 \div 1$$

Hence subtractive inverse of each exist in B

G5 # Commutative Law :

$$\text{as } 1 \div 1 = 1 \div 1$$

hence commutative law hold

G1 to G4 indicates Set B is group w.r.t “ \div ”

G1 to G5 indicates Set B is abelian group w.r.t “ \div ”