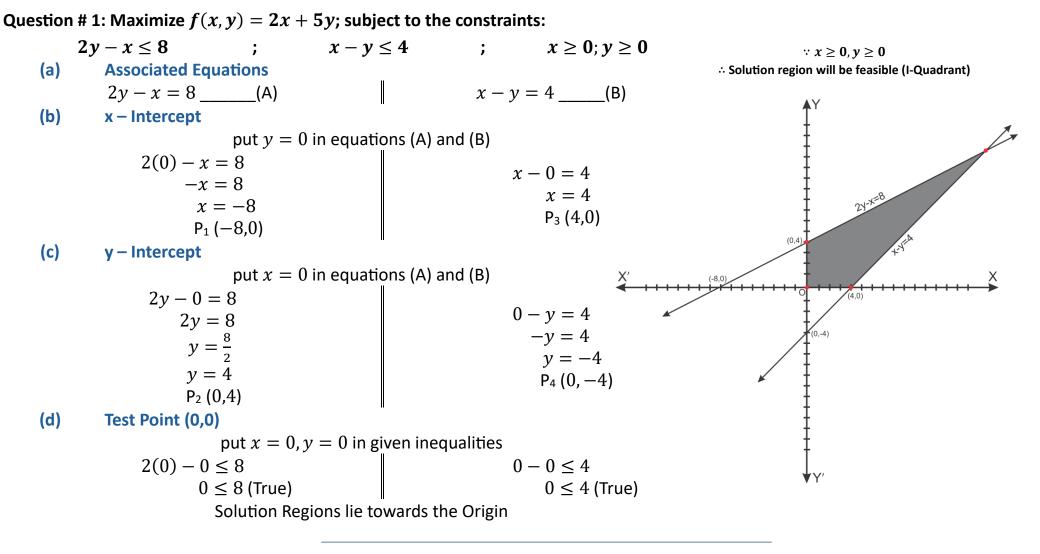
Exercise 5.1 (Solutions) Mathematics 9: PCTB (2025) Author: Sheraz Ansari Available at MathCity.org

Chapter # 5

Linear Equations and Inequalities

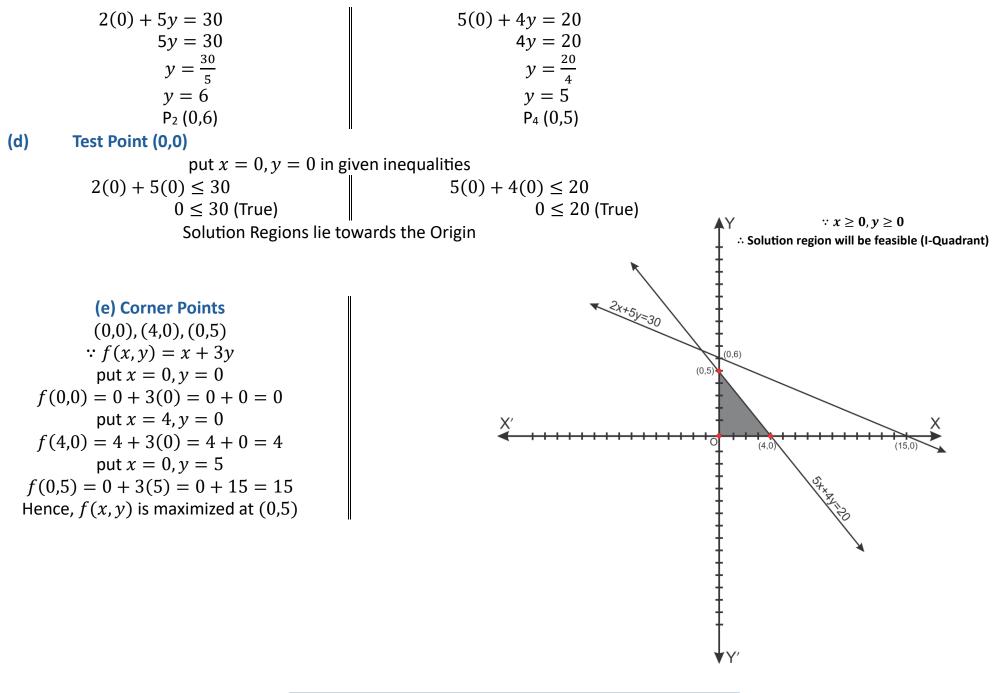
Exercise # 5.2

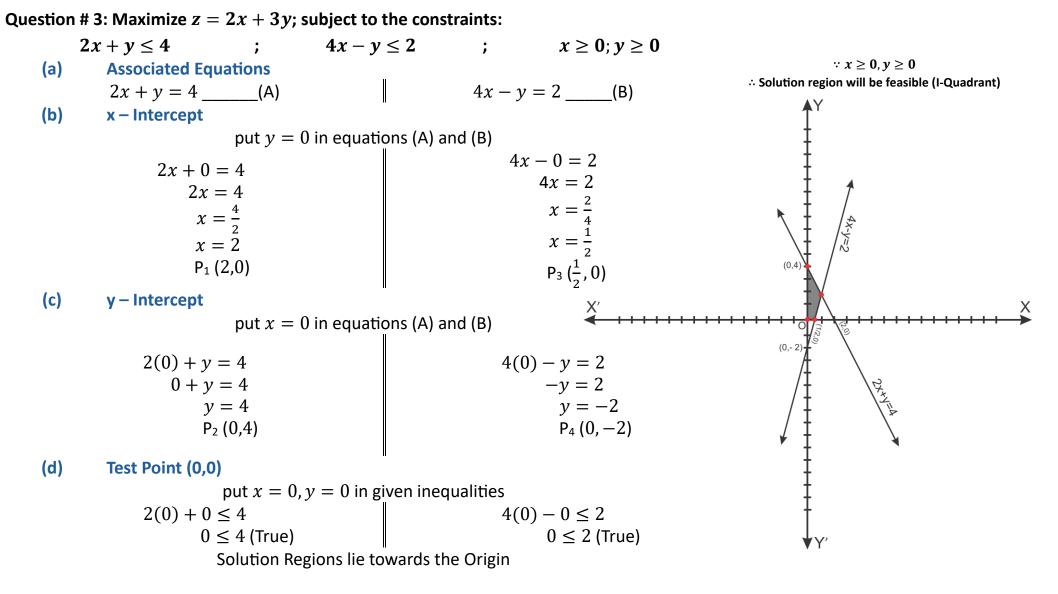


(e) Point of Intersection (f) Corner Points (0,0), (0,4), (4,0), (16,12)2y - x = 8 ____ (A) f(x,y) = 2x + 5yx - y = 4 (B) put x = 0, y = 0(A) + (B) f(0,0) = 2(0) + 5(0) = 0 + 0 = 0-x + 2y = 8put x = 0, y = 4 $\dot{x} - y = 4$ f(0,4) = 2(0) + 5(4) = 0 + 20 = 20v = 12put x = 4, y = 0Put in equation (B) f(4,0) = 2(4) + 5(0) = 8 + 0 = 8x - 12 = 4put x = 16, y = 12x = 4 + 12f(16,12) = 2(16) + 5(12) = 32 + 60 = 92x = 16Hence, f(x, y) is maximized at (16,12) Question # 2: Maximize f(x, y) = x + 3y; subject to the constraints: $2x + 5y \leq 30$; $5x + 4y \le 20$; $x \ge 0; y \ge 0$ (a) **Associated Equations** 5x + 4y = 20 (B) 2x + 5y = 30 (A) (b) x – Intercept put y = 0 in equations (A) and (B) 2x + 5(0) = 305x + 4(0) = 202x = 305x = 20 $x = \frac{20}{5}$ $x = \frac{30}{2}$ x = 4x = 15P₁ (15,0) P₃ (4,0) y – Intercept

put x = 0 in equations (A) and (B)

(c)





(e) Point of Intersection

$$2x + y = 4$$
(A)

$$4x - y = 2$$
(B)
(A) + (B)

$$2x + y = 4$$

$$4x - y = 2$$

$$6x = 6$$

$$x = \frac{6}{6}$$

$$x = 1$$

Put in equation (A)

$$2(1) + y = 4$$

$$2 + y = 4$$

$$y = 4 - 2$$

$$y = 2$$

(f) Corner Points

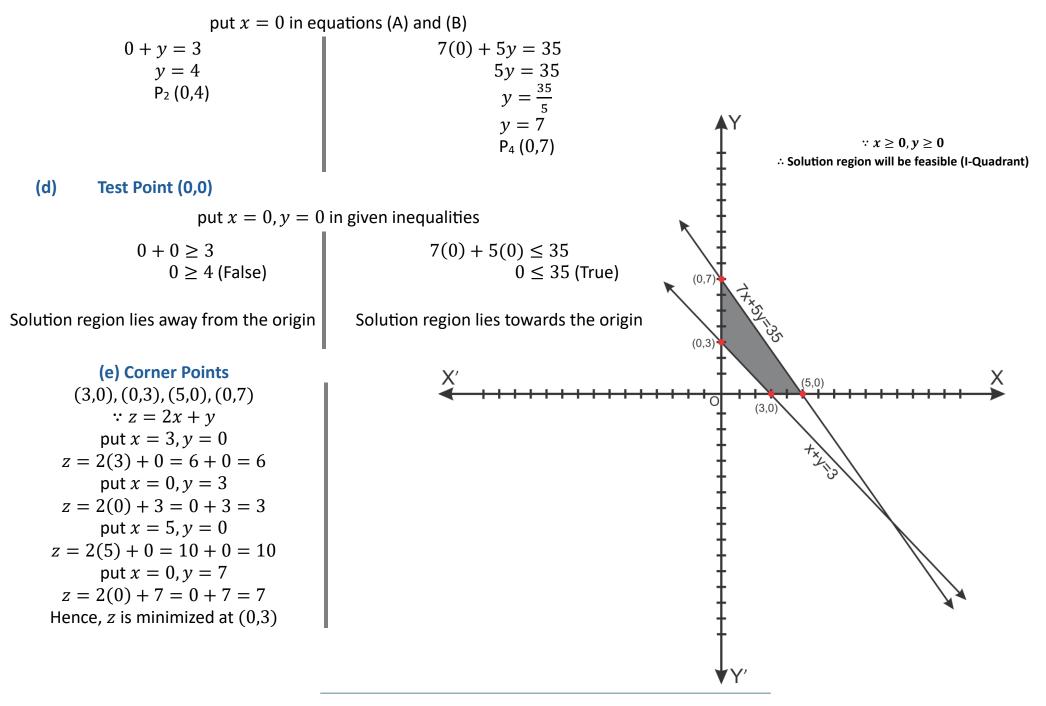
$$(0,0), (0,4), (1,0), (1,2)$$

 $\therefore z = 2x + 3y$
put $x = 0, y = 0$
 $z = 2(0) + 3(0) = 0 + 0 = 0$
put $x = 0, y = 4$
 $z = 2(0) + 3(4) = 0 + 12 = 12$
put $x = 1, y = 0$
 $z = 2(1) + 3(0) = 2 + 0 = 2$
put $x = 16, y = 12$
 $z = 2(1) + 3(2) = 2 + 6 = 8$
Hence, z is maximized at (0,4)

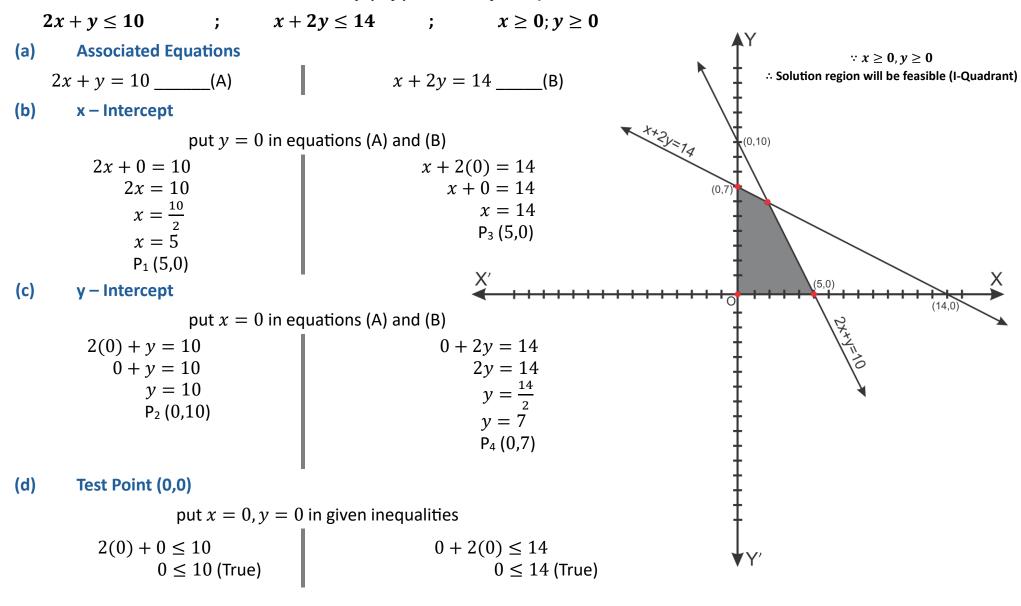
Question # 4: Maximize z = 2x + y; subject to the constraints:

 $x + y \ge 3$; $7x + 5y \le 35$; $x \ge 0$; $y \ge 0$ (a) Associated Equations 7x + 5y = 35 (B) x + y = 3 ____(A) (b) x – Intercept put y = 0 in equations (A) and (B) x + 0 = 37x + 5(0) = 35*x* = 3 7x = 35 $x = \frac{35}{7}$ P₁ (3,0) *x* = 5 P₃ (5,0)

(c) y – Intercept



Question # 5: Maximize the function defined as: f(x, y) = 2x + 3y; subject to the constraints:



Solution Regions lie towards the origin

(e) Point of Intersection

$$2x + y = 10 ; x + 2y = 14$$
Multiply by '2'

$$4x + 2y = 20$$
(C)
(C) - (D)

$$4x + 2y = 20$$

$$\pm x \pm 2y = \pm 14$$

$$3x = 6$$

$$x = \frac{6}{3}$$

$$x = 2$$
Put in equation (D)

$$2 + 2y = 14$$

$$2y = 14 - 2$$

$$2y = 12$$

$$y = \frac{12}{2}$$

$$y = 6$$

(f) Corner Points

$$(0,0), (5,0), (0,7), (2,6)$$

 $\therefore f(x,y) = 2x + 3y$
put $x = 0, y = 0$
 $f(0,0) = 2(0) + 3(0) = 0 + 0 = 0$
put $x = 5, y = 0$
 $f(5,0) = 2(5) + 3(0) = 10 + 0 = 10$
put $x = 0, y = 7$
 $f(0,7) = 2(0) + 3(7) = 0 + 21 = 21$
put $x = 2, y = 6$
 $f(2,6) = 2(2) + 3(6) = 4 + 18 = 22$
Hence, z is maximized at (2,6)

Question # 6: Find minimum and maximum values of z = 3x + y; subject to the constraints:

; $x + 3y \le 9$; $x \ge 0; y \ge 0$ $3x + 5y \ge 15$ (a) **Associated Equations** 3x + 5y = 15 (A) x + 3y = 9 ____(B) (b) x – Intercept put y = 0 in equations (A) and (B) 3x + 5(0) = 15x + 3(0) = 93x = 15x + 0 = 9 $x = \frac{15}{3}$ x = 9P₃ (9,0) *x* = 5 P₁ (5,0)

(c) y – Intercept

