

Exc 1.2

Q#1 Plot the graph of the Functions.

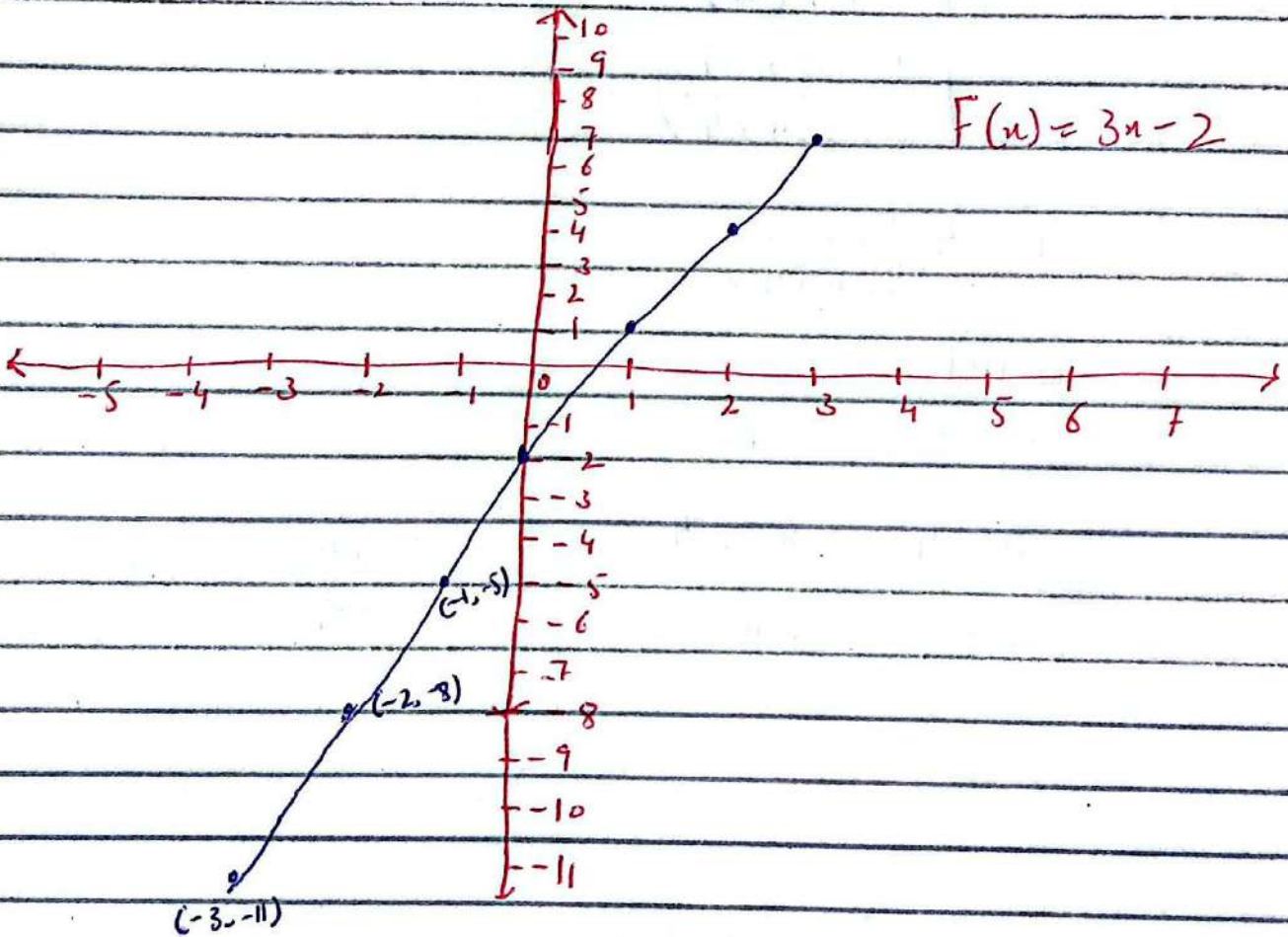
i) $F(x) = 3x - 2$

Sol

Let $y = F(x)$

$y = 3x - 2$ (Linear Function)

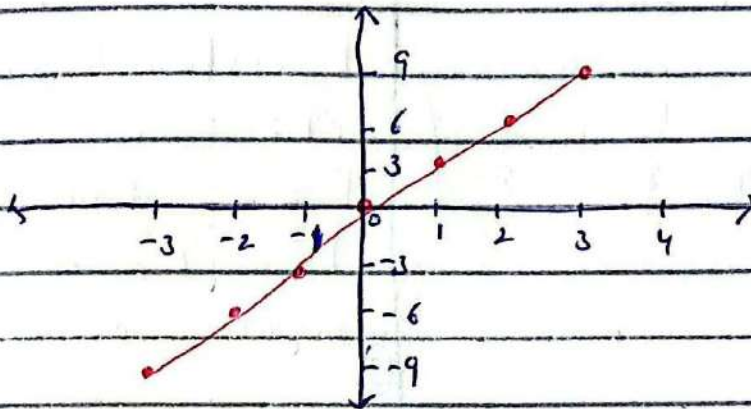
Input	x	-3	-2	-1	0	+1	+2	+3
output	y	-11	-8	-5	-2	1	4	7



(iii) $y = 3x$

Sol Let $y = f(x)$
 $y = 3x$

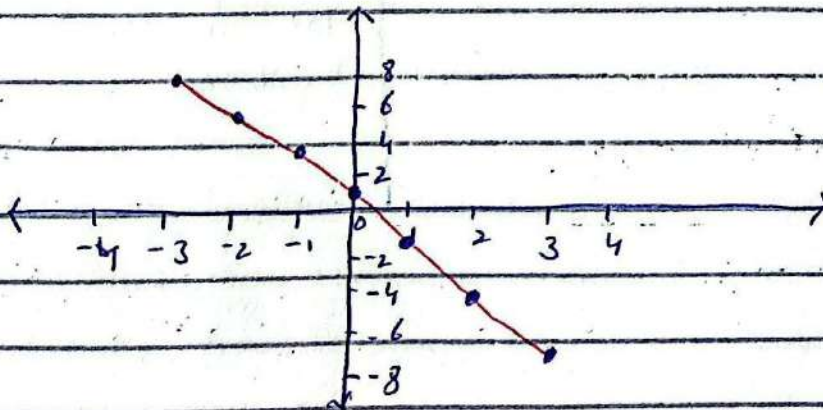
x	-3	-2	-1	0	1	2	3
y	-9	-6	-3	0	3	6	9



(iii) $f(x) = 1 - 2x$

Sol Let $y = f(x)$
 $y = 1 - 2x$

x	-3	-2	-1	0	1	2	3
y	7	5	3	1	-1	-3	-5



Note

(iv) $y = g(x) = x^2 + 4$

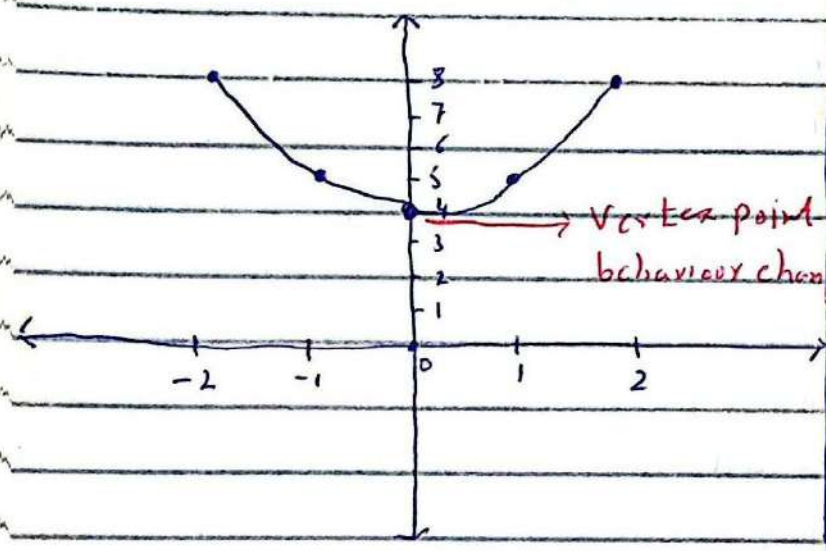
Sol

- i) $a = 1 > 0$ open upward
- ii) $b = 0$ At y-axis
- iii) $c = 4$ (0,4) intercept

iv) $x = \frac{-b}{2a} = \frac{0}{2} = 0$ $x = 0$

is the eq at y-axis.

x	-2	-1	0	1	2
y	8	5	4	5	8



- ① $y = ax^2 + bx + c$
- i) IF $a > 0$ open upward.
 - ii) IF $a < 0$ open downward.
 - iii) IF value of 'a' is large than parabola narrow.

② IF $b > 0$ then position of vertex horizontally left side.

IF $b < 0$ then position of vertex horizontally right side.

③ c : (intercept)
this is y-intercept

$y = mx + c$ $m = \text{slope}$
 $c = \text{intercept}$

So (0,c) is on the parabola

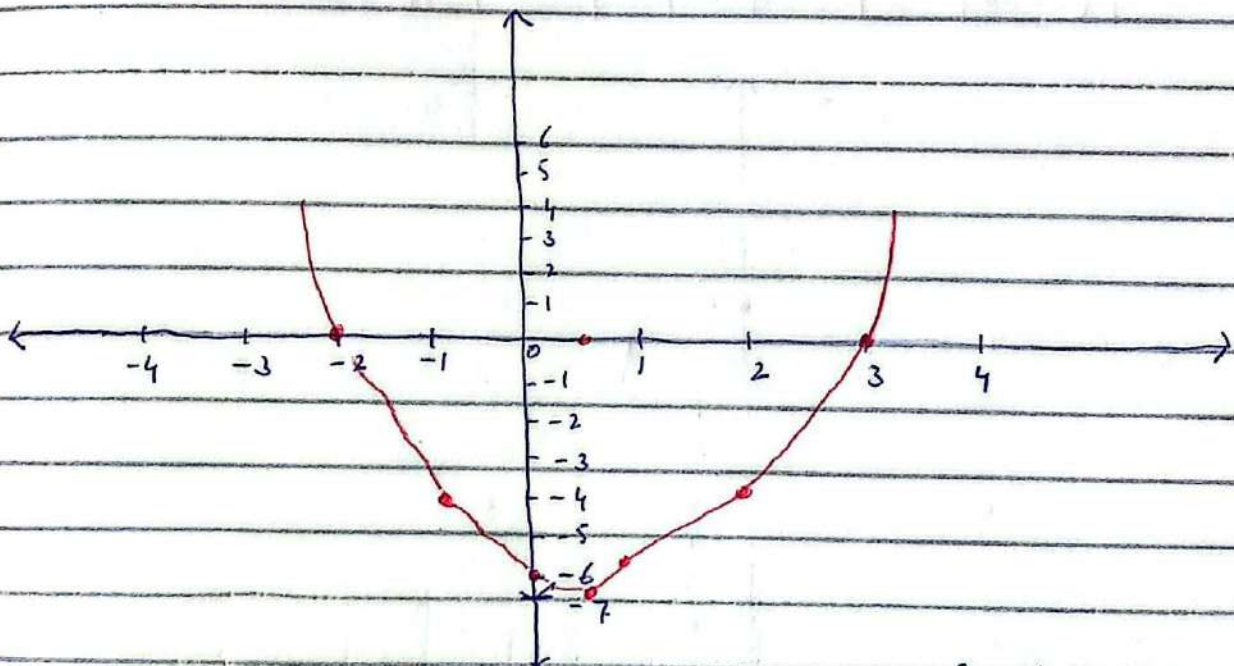
④ $x = \frac{-b}{2a}$ is eq. of axis of symmetry and also x-coordinate the vertex.

(v) $g(x) = x^2 - x - 6$

Sol

- i) $a = 1 > 0$ open upward.
- ii) $b = -1 < 0$ vertex horizontally right side.
- iii) $c = -6 \rightarrow (0, -6)$ intercept (y).
- iv) $x = \frac{-b}{2a} = \frac{-(-1)}{2(1)} = \frac{1}{2} = 0.5$ $x = 0.5$

x	-3	-2	-1	0	1	2	3	0.5
y	6	0	-4	-6	-6	-4	0	-6.25



(vi) $g(x) = \sqrt{2x+1}$

$$2x+1 \geq 0$$

$$2x \geq -1$$

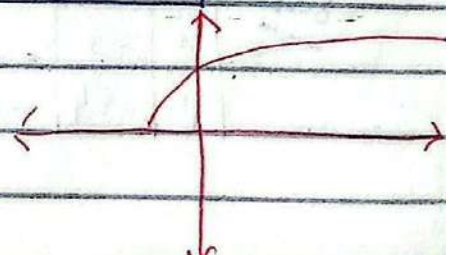
$$x \geq -\frac{1}{2}$$

$$x \geq -0.5$$

Sol

x	0	1	2	3	4	5
y	1	$\sqrt{3} = 1.73$	$\sqrt{5} = 2.23$	$\sqrt{7}$	$\sqrt{9}$	$\sqrt{11}$

Draw yourself.



Q#2 Plot the graph of following functions.

i) $F(x) = -x^2 + 1$

Sol

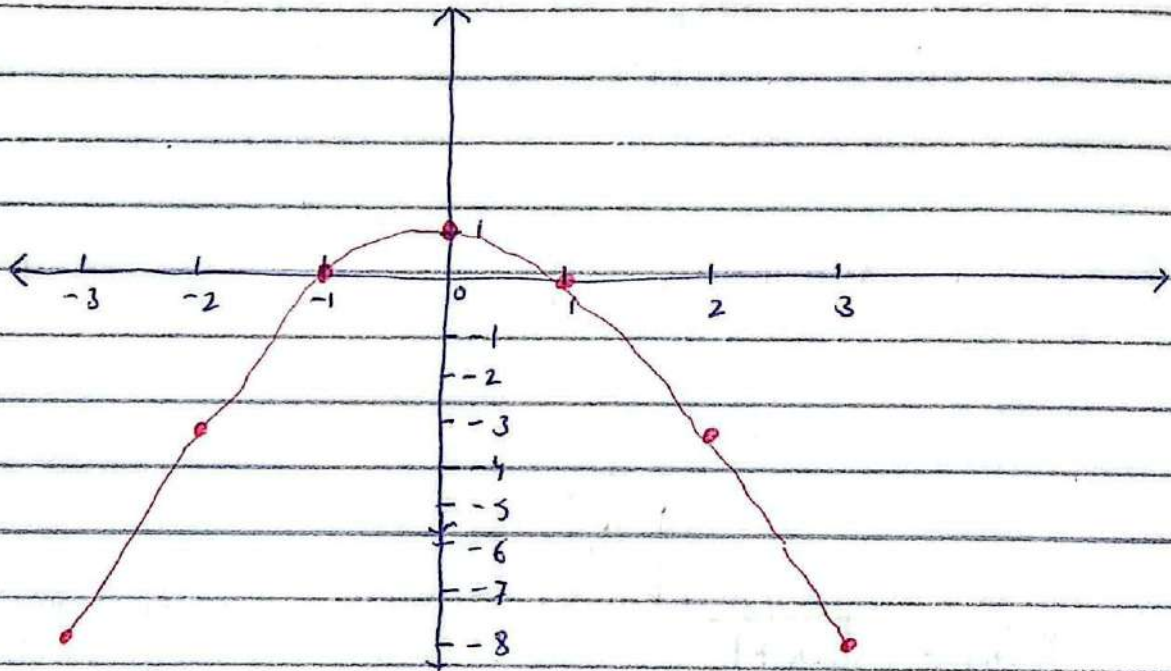
i) $a = -1 < 0$ Open downward

ii) $b = 0$ At y-axis

iii) $c = 1$ (0,1) intercept

iv) $x = -b/2a = \frac{-0}{-2} = 0$ $x = 0$ (eq of symmetry)

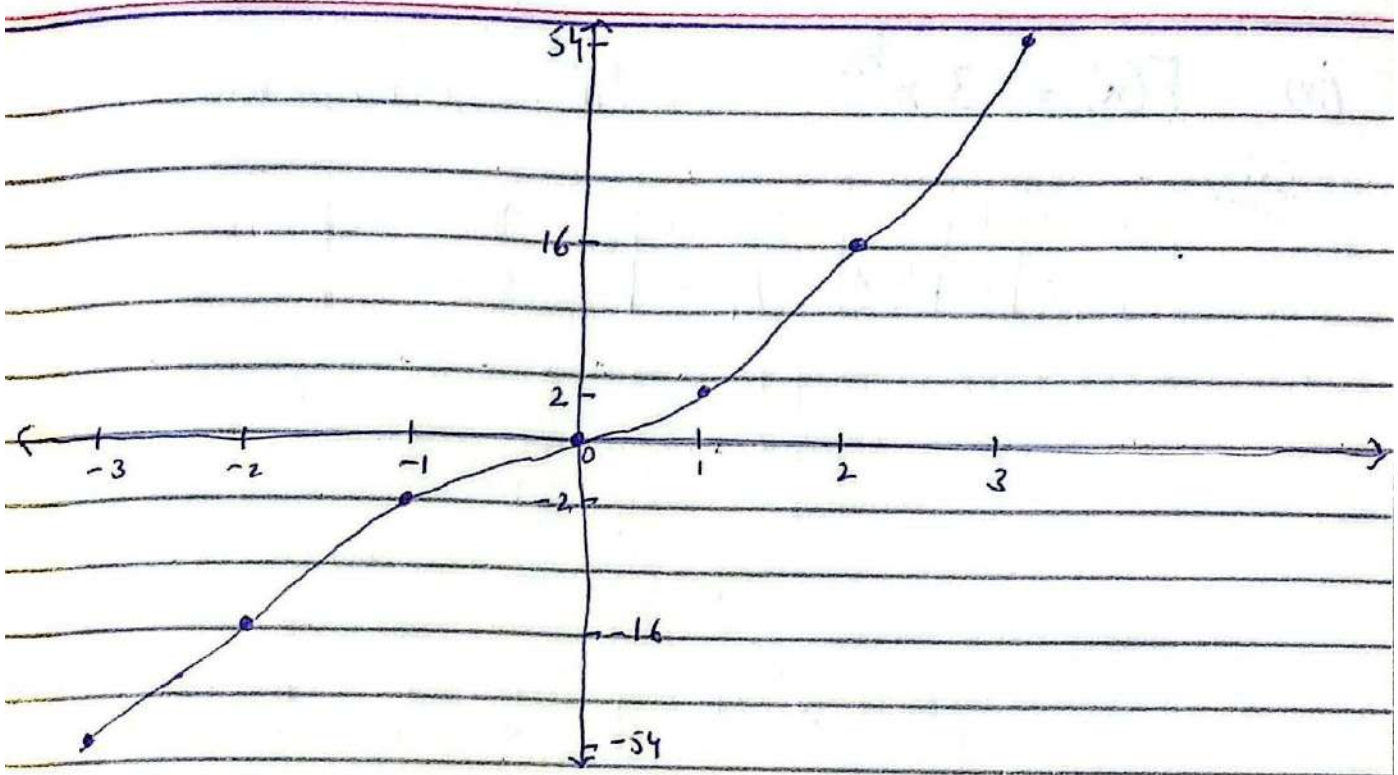
x	-3	-2	-1	0	1	2	3
y	-8	-3	0	1	0	-3	-8



ii) $F(x) = 2x^3$

Sol

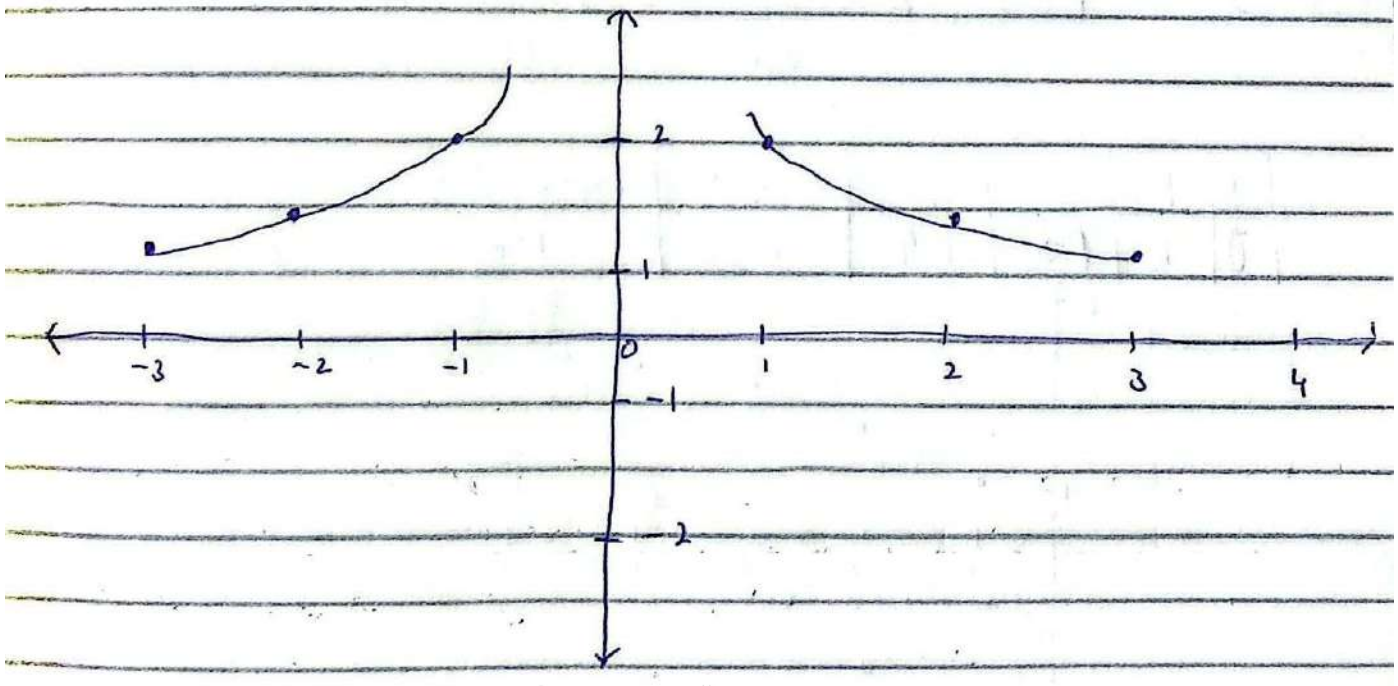
x	-3	-2	-1	0	1	2	3
y	-54	-16	-2	0	2	16	54



iii) $f(x) = 1 + x^{-2}$. x میں (0) Post نہیں کر سکتے .

Sol

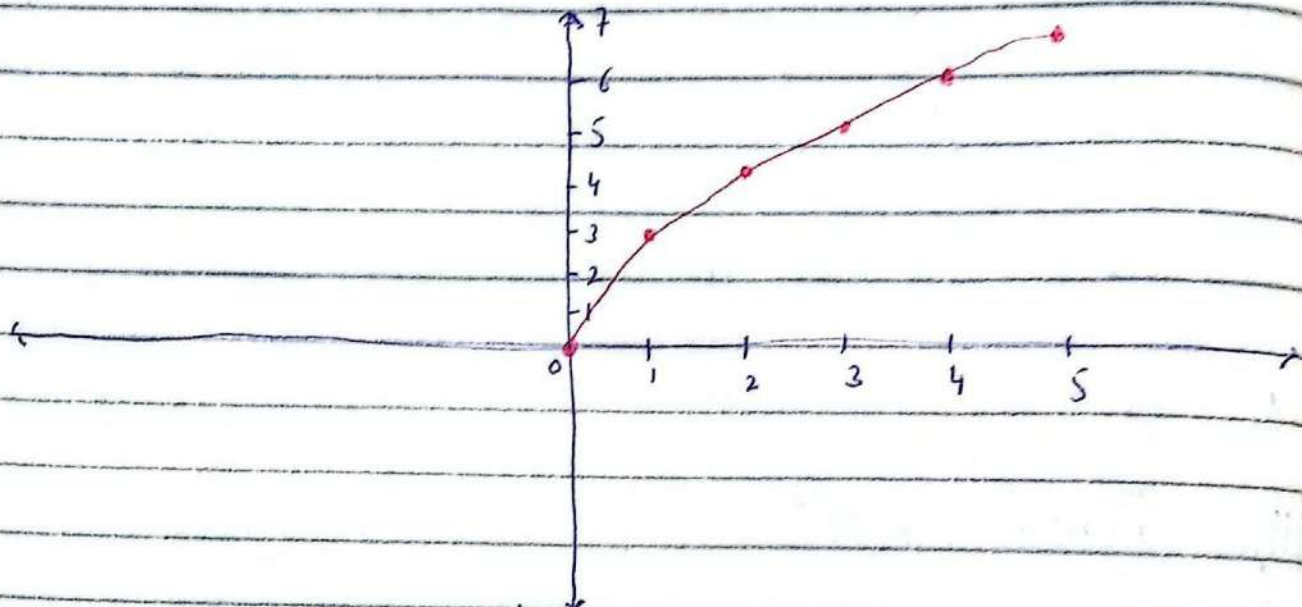
x	-3	-2	-1	1	2	3
y	1.1	1.2	2	2	1.2	1.1



(iv) $F(x) = 3x^{1/2} = 3\sqrt{x}$ (3 تا 5 کے لیے P.T کر سکتے ہیں)

Sol

x	0	1	2	3	4	5
y	0	3	4.2	5.2	6	6.7

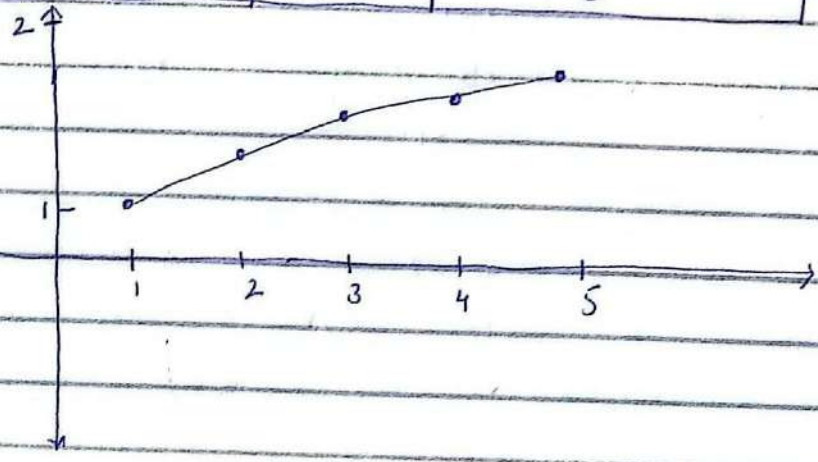


(v) $F(x) = 2 - x^{1/2}$

Sol

$F(x) = 2 - \frac{1}{\sqrt{x}}$

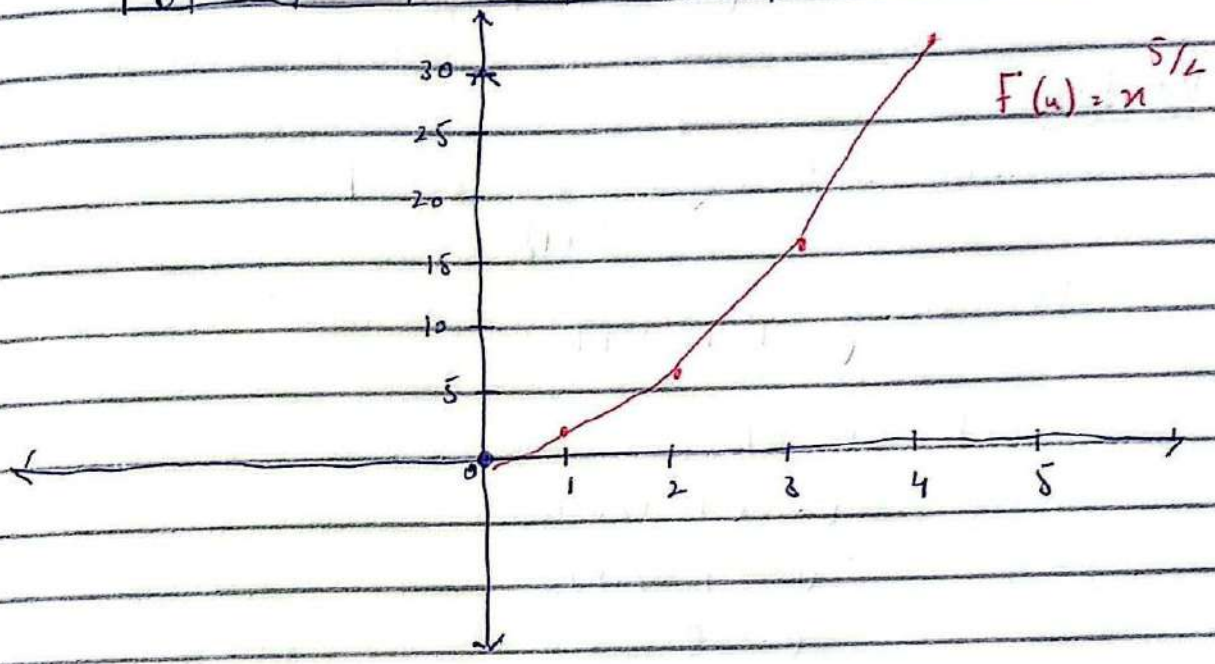
x	1	2	3	4	5
y	1	1.3	1.4	1.5	1.6



vi) $f(x) = x^{5/2}$ $f(x) = \sqrt[5]{x}$

Sol

x	0	1	2	3	4
y	0	1	5.6	15.5	32



Q#3 Find possible x-intercept, y-intercept and vertex of the functions and plot.

i) $f(x) = x^2 + 2x + 1 \Rightarrow y = x^2 + 2x + 1$

Sol

x-intercept

Put $y = 0$

$0 = x^2 + 2x + 1$

$(x+1)^2 = 0$

Taking square root

$\sqrt{(x+1)^2} = \sqrt{0}$

$x+1 = 0 \Rightarrow x = -1$

$(-1, 0)$ is x-intercept.

Y-interceptPut $x=0$

$$y = (0)^2 + 2(0) + 1$$

$$y = 1$$

(0, 1) is y-intercept.

Vertex

$$x = -\frac{b}{2a} = \frac{-2}{2(1)} = -1$$

As

$$y = x^2 + 2x + 1$$

Put $x = -1$

$$y = (-1)^2 + 2(-1) + 1$$

$$y = 1 - 2 + 1$$

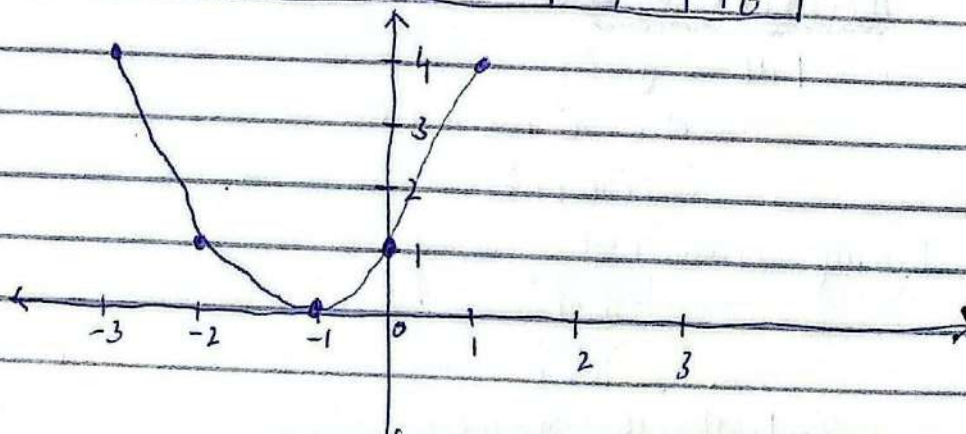
$$y = 0$$

(-1, 0) is vertex.

اس میں vertex اور x-intercept ایک جیسے آتے ہیں لیکن یہ
 ہر سوال میں ایسا جیسے نہیں ہوتا ہے۔

Graph.

x	-3	-2	-1	1	2	3
y	4	1	0	4	9	16



$$(ii) f(x) = -2x^2 + 2x - 1$$

Sol Let $y = -2x^2 + 2x - 1$

x-intercept

Put $y = 0$

$$-2x^2 + 2x - 1 = 0$$

$$a = -2, b = 2, c = -1$$

$$x = \frac{-2 \pm \sqrt{(2)^2 - 4(-2)(-1)}}{2(-2)}$$

$$x = \frac{-2 \pm \sqrt{4 - 8}}{-4}$$

$$x = \frac{-2 \pm \sqrt{-4}}{-4} = \text{Complex}$$

Not Possible

• No x-intercept

y-intercept

Put $x = 0$

$$y = 0 + 0 - 1$$

$$y = -1$$

$(0, -1)$ is y intercept

Vertex

$$x = \frac{-b}{2a} = \frac{-2}{2(-2)} = \frac{-2}{-4} = \frac{1}{2}$$

As $y = -2x^2 + 2x - 1$

$$y = -2\left(\frac{1}{2}\right)^2 + 2\left(\frac{1}{2}\right) - 1$$

$$y = -2 \cdot \frac{1}{4} + 1 - 1$$

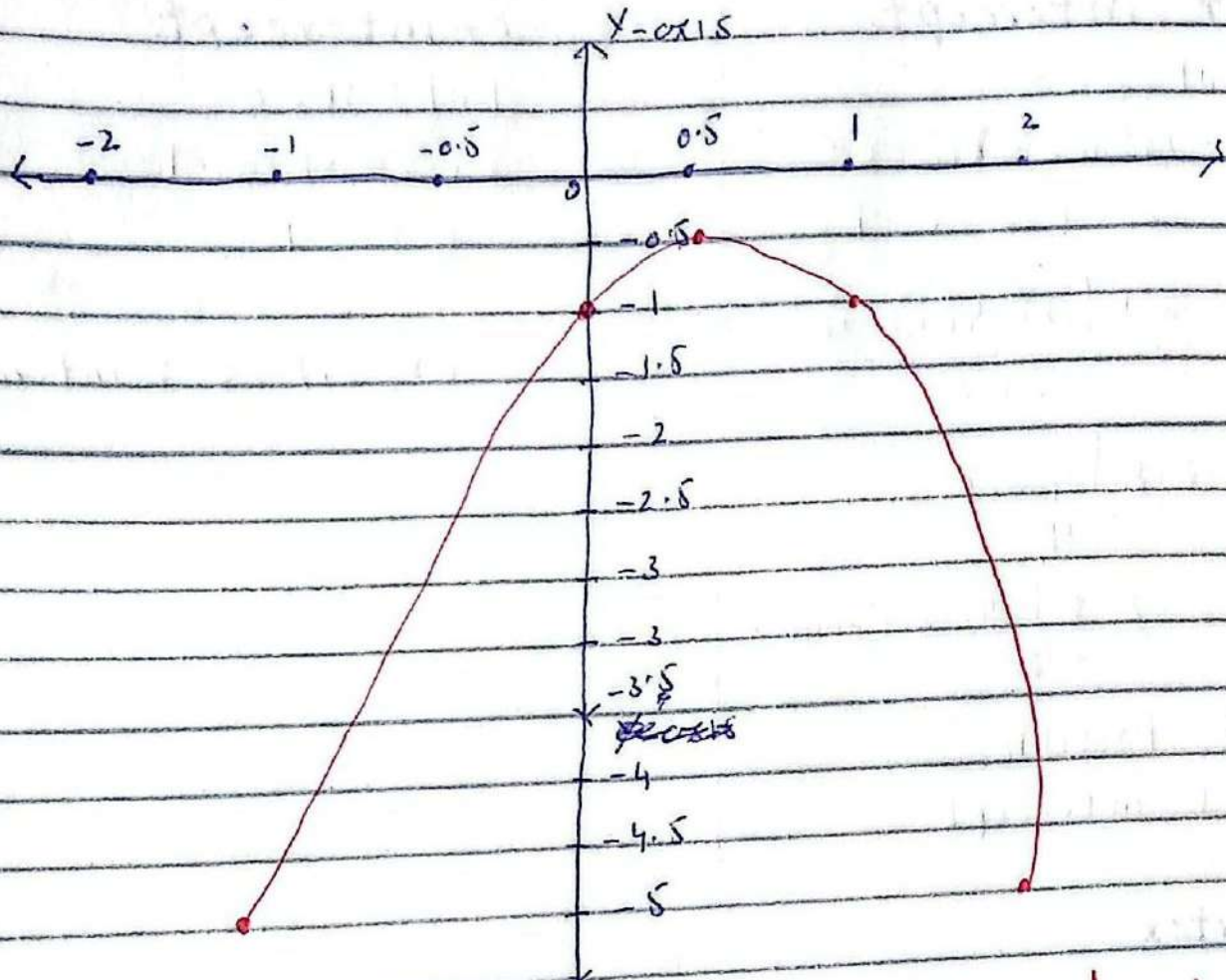
$$y = -\frac{1}{2}$$

$\left(\frac{1}{2}, -\frac{1}{2}\right)$ is Vertex

Graph

Vertex
↑

x	-2	-1	0	$\frac{1}{2}$	1	2
y	-13	-5	-1	$-\frac{1}{2}$	-1	-5



یہ گراف اس کے پاس x -intercept ہے جو کہ Points میں نکالنے کے لئے
 اس کے لئے اس Parabola کے x -axis میں x -intercept نکالیں

(iii) $F(x) = x^2 + 2x$
 $y = x^2 + 2x$
 $a = 1, b = 2, c = 0$

Sol

x -intercept

put $y = 0$
 $x^2 + 2x = 0$
 $x(x+2) = 0$
 $x+2 = 0$

y -intercept
 put $x = 0$

$y = (0)^2 + 2(0)$

$x = 0$ $x = -2$

$y = 0$

$(0,0)$ $(-2,0)$ are
x-intercepts.

$(0,0)$ is the y
intercept.

Vertex

$x = \frac{-b}{2a} = \frac{-2}{2(1)} = -1$

Put $x = -1$ in given function:

$y = (-1)^2 + 2(-1)$

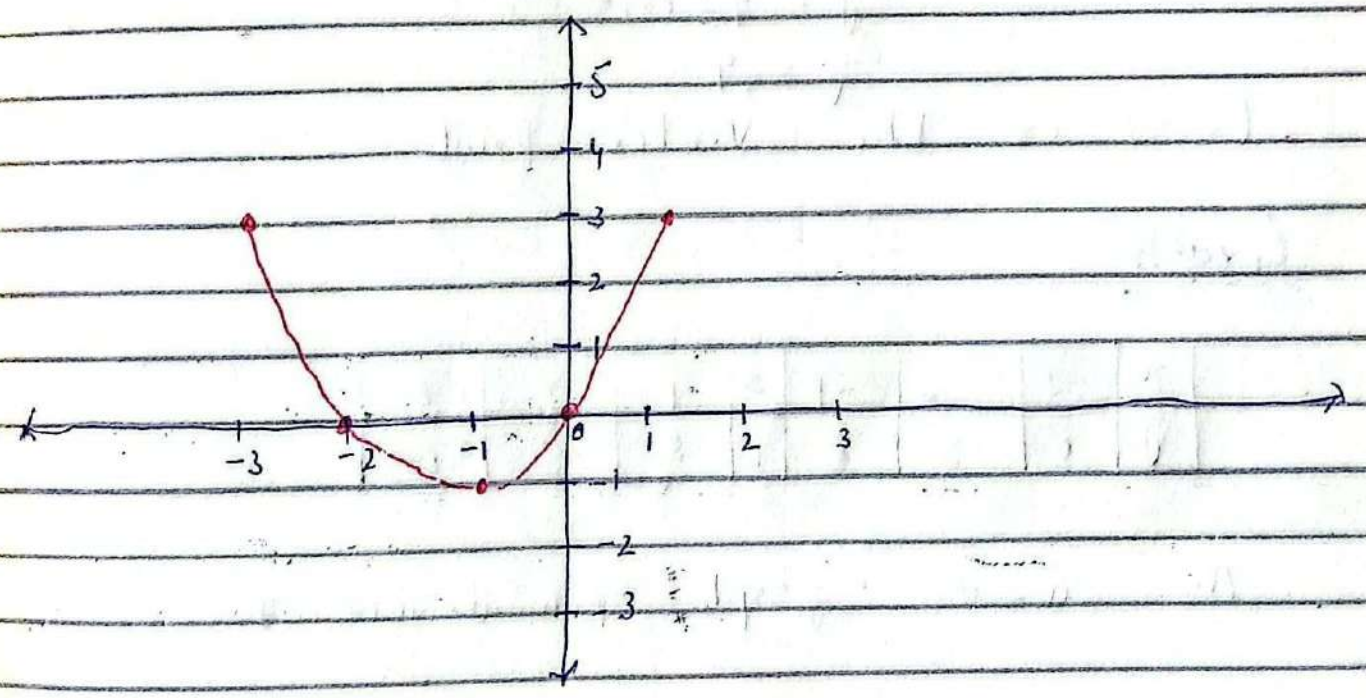
$y = 1 - 2$

$y = -1$

$(-1, -1)$ is the vertex.

Graph

x	-3	-2	-1	0	1	2
y	3	0	-1	0	3	8



Q(iv) $F(x) = 9 - x^2$

Sol Let $y = 9 - x^2$

$a = -1, c = 9, b = 0$

X-intercept

Put $y = 0$

$9 - x^2 = 0$

$x^2 = +9$

$x^2 = 9$

$x = +3$

$(3, 0)$ and $(-3, 0)$ are x-intercept

Y-intercept

Put $x = 0$

$y = 9 - (0)^2$

$y = 9$

$(0, 9)$ is y intercept

Vertex

$x = \frac{-b}{2a} = \frac{0}{2(-1)} = 0$

Put $x = 0$ in given function

$y = 9 - (0)^2$

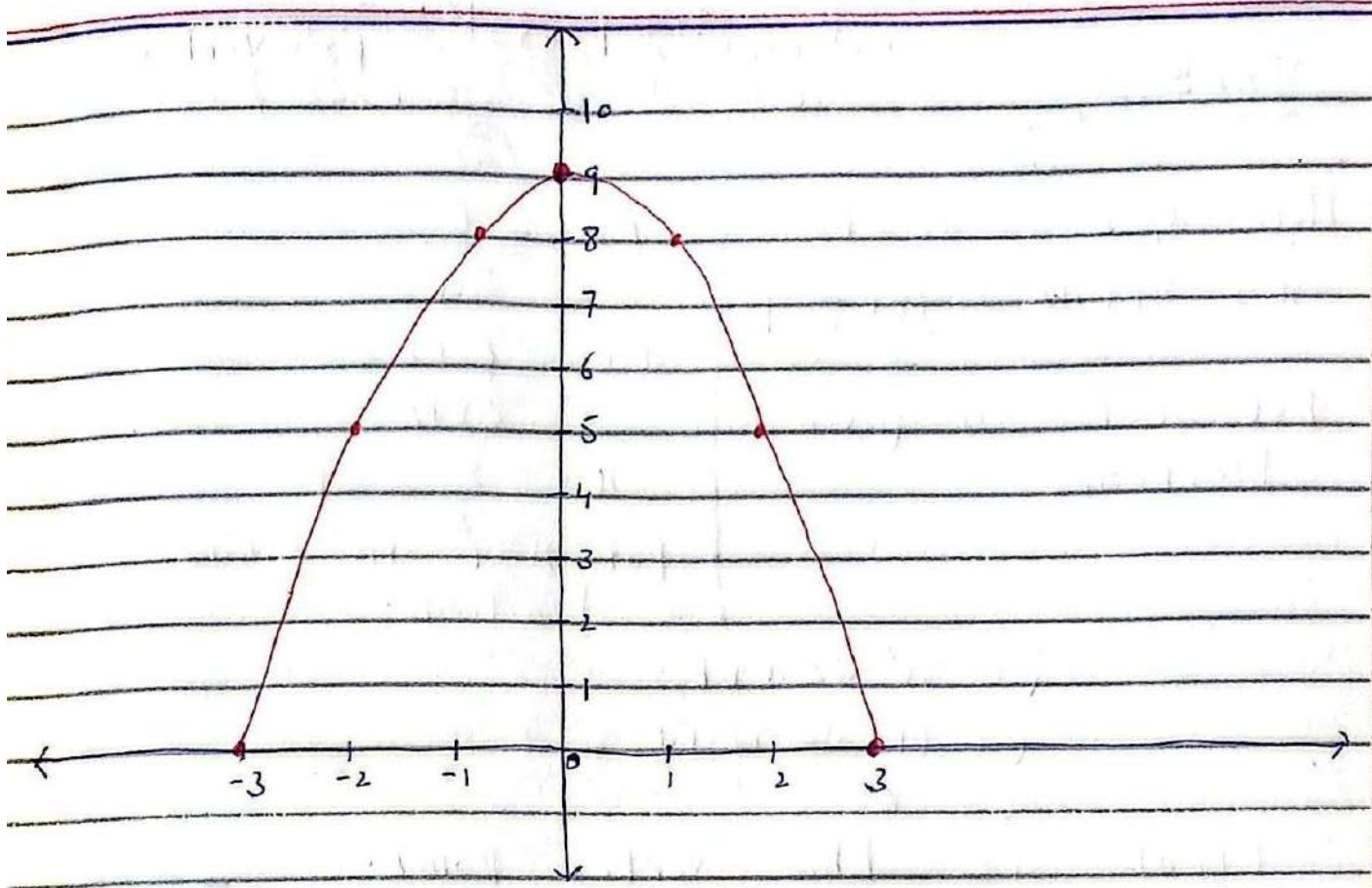
$y = 9$

$(0, 9)$ is the vertex point

Graph

x	-3	-2	-1	0	1	2	3
y	0	5	8	9	8	5	0

As $a < 0$; graph open downwards.



Q #4 Draw the graph of following functions using factors.

i) $F(x) = x^2 - 2x + 1$

Sol
x-intercept
 Put $y = 0$
 $x^2 - 2x + 1 = 0$
 $x^2 - x - x + 1 = 0$
 $x(x-1) - 1(x-1) = 0$
 $(x-1)(x-1) = 0$
 $x-1 = 0$ $x-1 = 0$
 $x = 1$ $x = 1$
 Here (1, 0) is the x-intercept
 $x_1 = 1$ $x_2 = 1$

Here $a = 1, b = -2, c = 1$
y-intercept
 Put $x = 0$
 $y = (0)^2 - 2(0) + 1$
 $y = 1$
 (0, 1) is the y-intercept

ادھر vertex معلوم کرنے کا دوسرا طریقہ بھی ہے، دونوں طریقوں سے کر سکتے ہیں۔

Vertex

①

Here $x_1 = 1$ $x_2 = 1$

$$x = \frac{x_1 + x_2}{2} = \frac{1 + 1}{2} = 1$$

Put $x = 1$ in given Function

②

$$x = \frac{-b}{2a}$$

$$x = \frac{-(-2)}{2(1)}$$

$$x = \frac{2}{2} = 1$$

Put $x = 1$ in given Function

$$y = x^2 - 2x + 1 \qquad 1 + 2 + 1$$

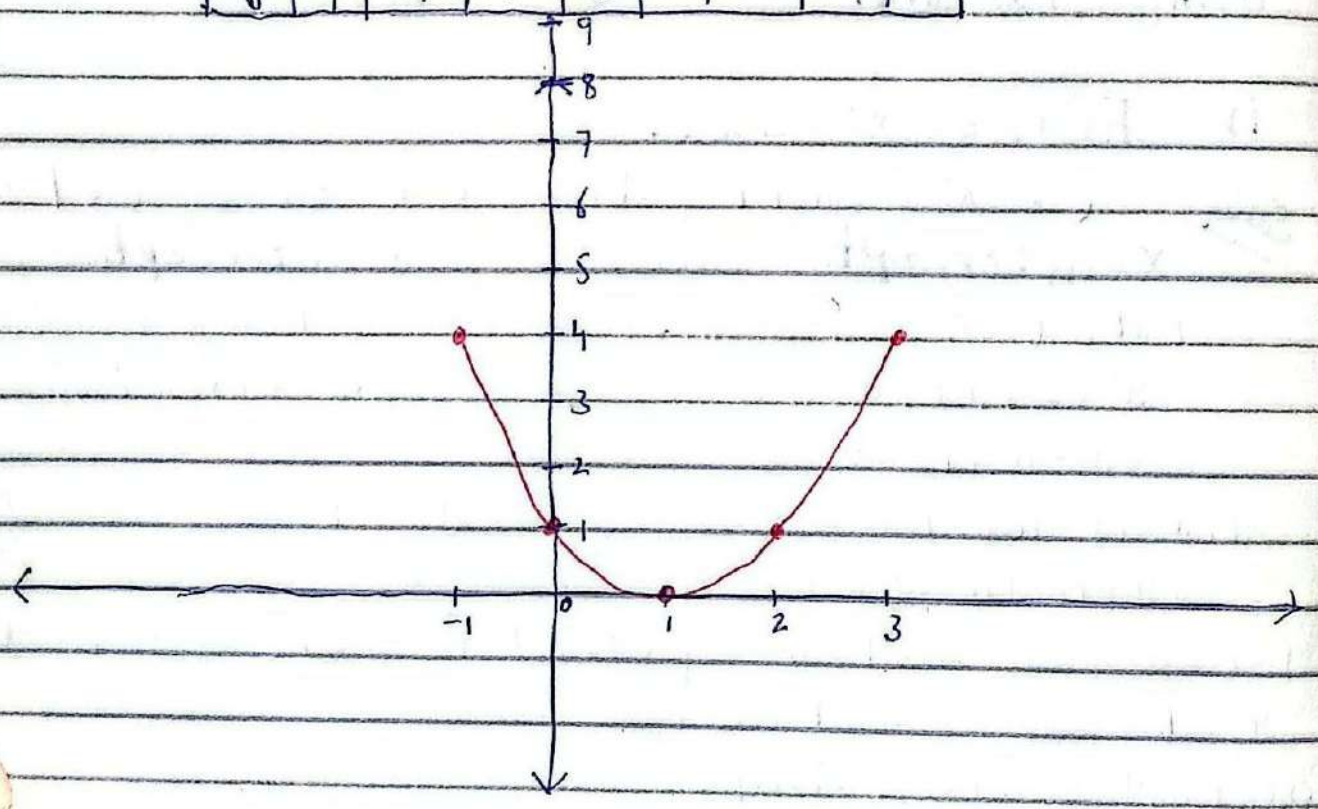
$$y = (1)^2 - 2(1) + 1$$

$$y = 0$$

(1, 0) is the vertex point.

Graph

x	-2	-1	0	1	2	3
y	9	4	1	0	1	4



Q#4 (ii) $y = x^2 - 7x + 12$

X-intercept

Put $y = 0$

$$x^2 - 7x + 12 = 0$$

$$x^2 - 4x - 3x + 12 = 0$$

$$x(x-4) - 3(x-4) = 0$$

$$x-3 = 0 \quad x-4 = 0$$

$$x = 3 \quad x = 4$$

Hence (3,0) and (4,0) are x-intercepts

Y-intercept

Put $x = 0$

$$y = 0 - 7(0) + 12$$

$$y = 12$$

(0,12) is the y-intercept

Vertex

دو تونوں میں سے کوئی ایک method کر لیں

Here $x_1 = 3$ $x_2 = 4$

$$x = \frac{x_1 + x_2}{2} = \frac{3 + 4}{2} = \frac{7}{2}$$

$$x = 3.5$$

$$x = \frac{-b}{2a}$$

$$x = \frac{-(-7)}{2(1)}$$

$$x = \frac{7}{2} \quad x = 3.5$$

Put $x = 3.5$ in given function:

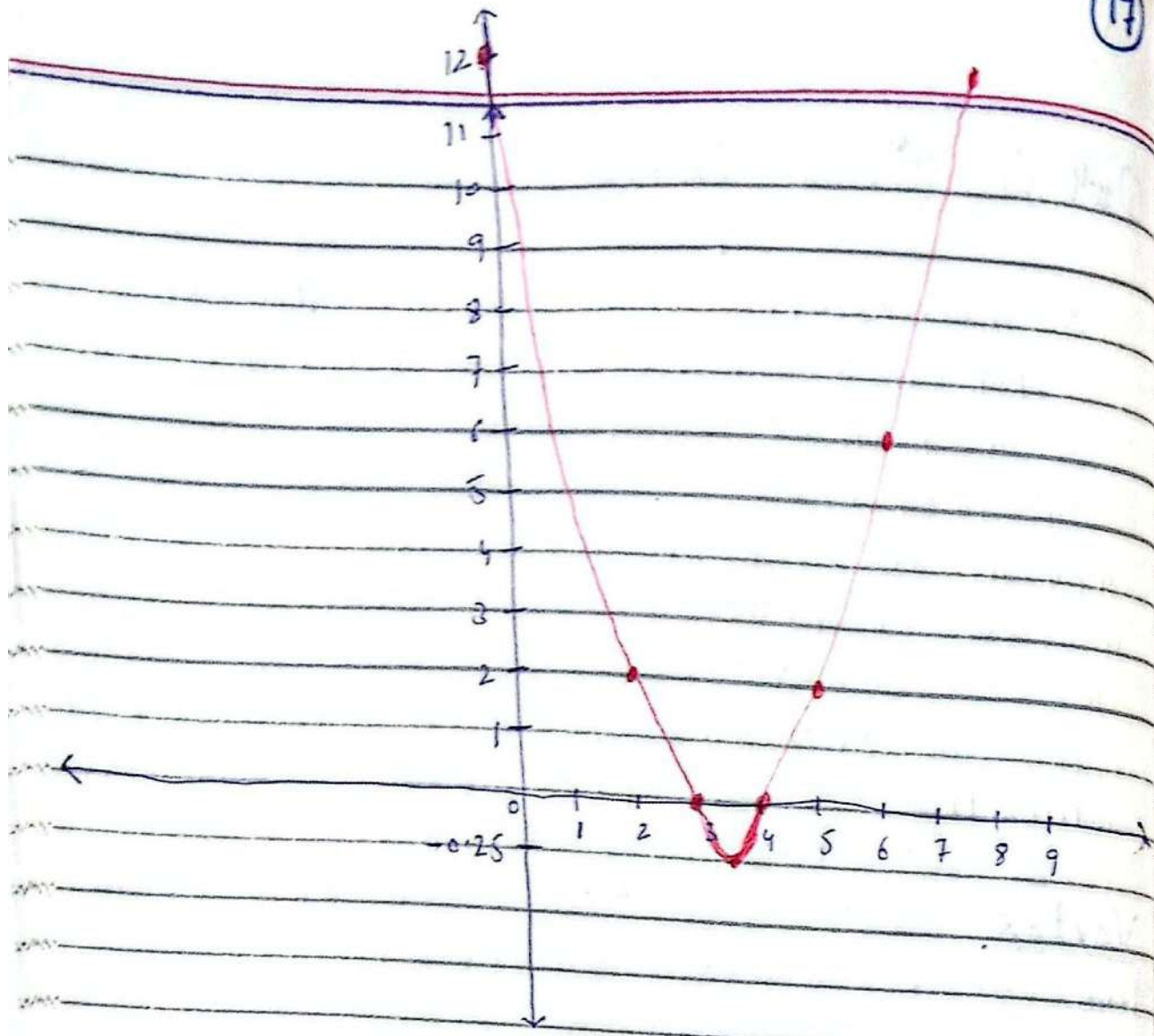
$$y = (3.5)^2 - 7(3.5) + 12$$

$$y = -0.25$$

(3.5, -0.25) is the vertex point.

Graph

x	0	2	3	3.5	4	5	6	7	...
y	12	2	0	-0.25	0	2	6	12	...



(iii) $f(x) = x^2 - 2x$

Sol $y = x^2 - 2x$

x-intercept

y-intercept

Put $y = 0$
 $x^2 - 2x = 0$
 $x(x - 2) = 0$
 $x = 0$ $x = 2$

Put $x = 0$
 $y = 0 - 2(0)$
 $y = 0$

$(0, 0)$ and $(2, 0)$ are the x-intercept

$(0, 0)$ is the y-intercept

Vertex

Here $x_1 = 0$ $x_2 = 2$

$$x = \frac{-b}{2a}$$

$$x = \frac{x_1 + x_2}{2} = \frac{0 + 2}{2} = 1$$

$$x = \frac{-(-2)}{2(1)}$$

$$x = 1$$

Put $x = 1$ in given function.

$$y = (1)^2 - 2(1)$$

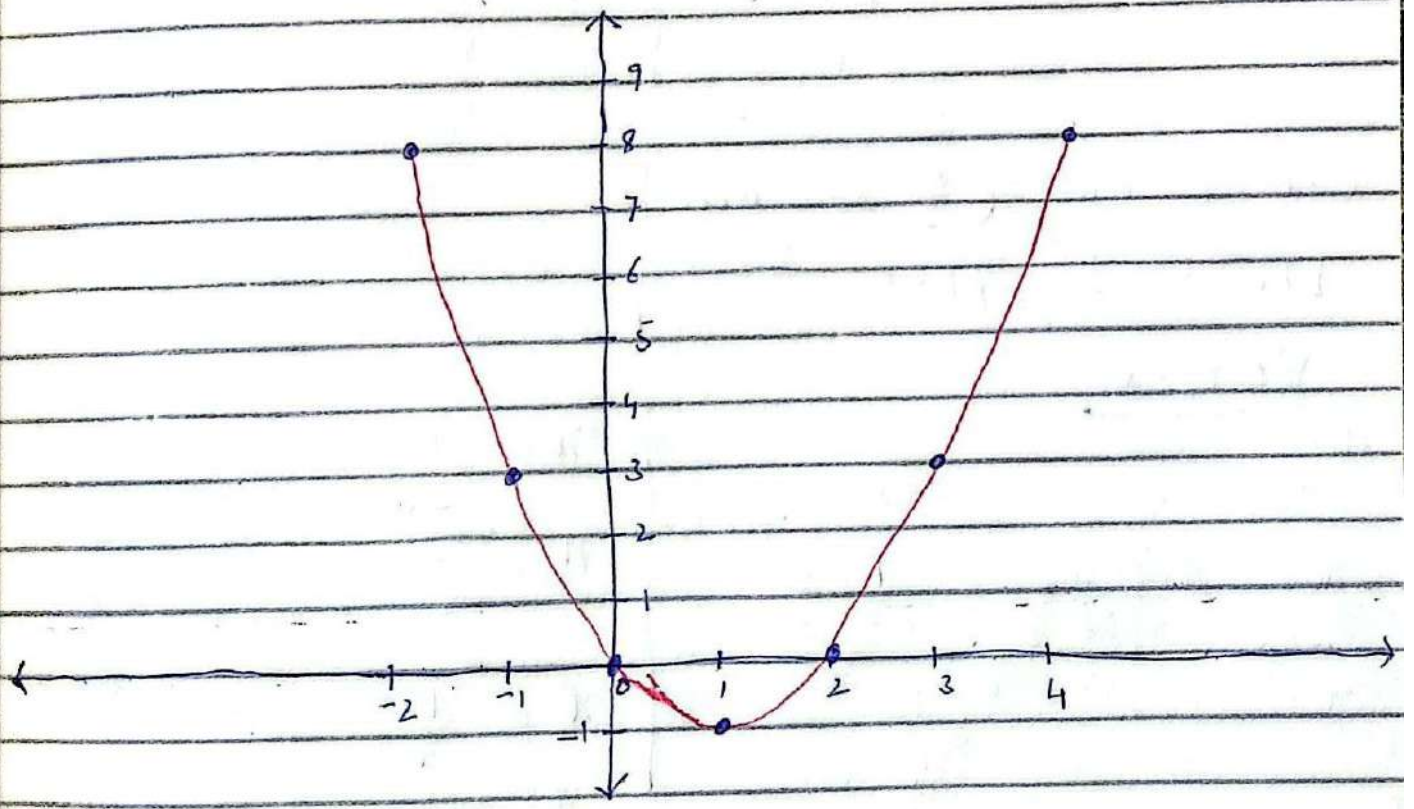
$$y = 1 - 2$$

$$y = -1$$

$(1, -1)$ is the vertex point.

Graph

x	-2	-1	0	1	2	3	4
y	8	3	0	-1	0	3	8



(iv) $F(x) = -2x^2 + x + 3$

Sol

$y = -2x^2 + x + 3$ $a = 2, b = 1, c = 3$

X-intercept

Y-intercept

Put $y = 0$

Put $x = 0$

$-2x^2 + x + 3 = 0$

$y = -2(0) + 0 + 3$

$2x^2 - x - 3 = 0$

$y = 3$

$2x^2 - 3x + 2x - 3 = 0$

$x(2x - 3) + 1(2x - 3)$

$(0, 3)$ is the Y-intercept

$(x + 1)(2x - 3) = 0$

$x + 1 = 0$

$2x - 3 = 0$

$x = -1$

$2x = 3$

$x = \frac{3}{2}$

$(-1, 0)$ and $(\frac{3}{2}, 0)$ are

the X intercepts.

Vertex

Here

$x_1 = -1$

$x_2 = \frac{3}{2}$

$x = \frac{-b}{2a}$

$x = \frac{x_1 + x_2}{2} = \frac{-1 + \frac{3}{2}}{\frac{1}{2}}$

$x = \frac{-1}{2(-2)}$

$x = \frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$

$x = \frac{1}{4}$

$x = 0.25$

$x = 0.25$

Put $x = 0.25$ in given function

$$y = -2(0.25)^2 + (0.25) + 3$$

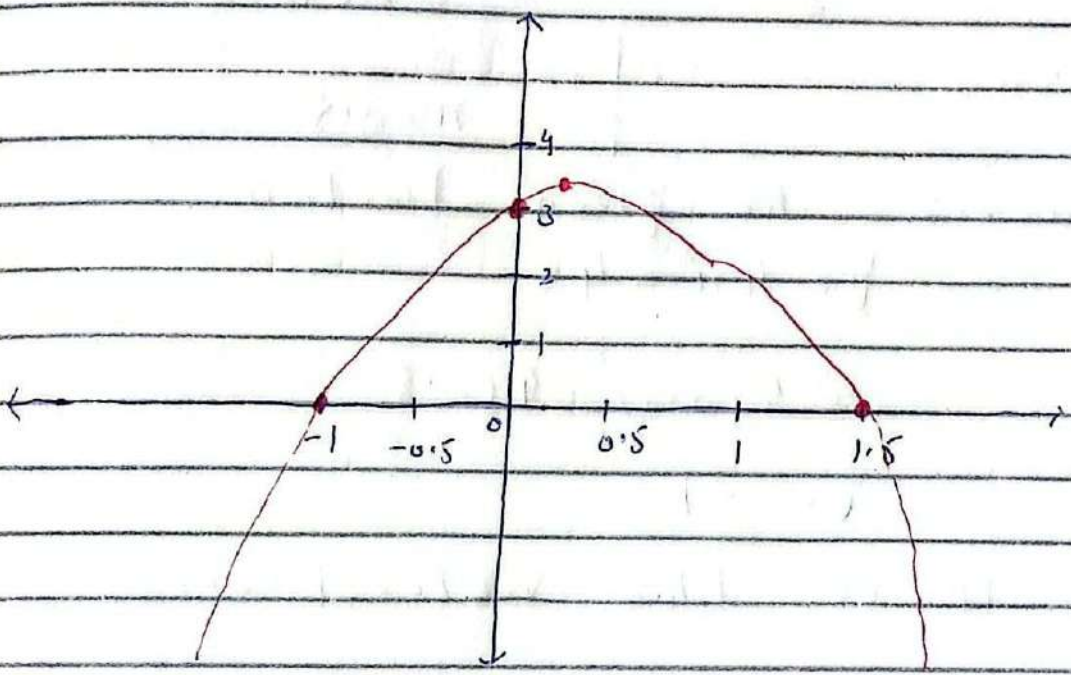
$$y = \frac{25}{8}$$

$$y = 3.125$$

$(0.25, 3.125)$ is the vertex point.

Graph

x	-1	0	0.25	1.5
y	0	3	3.125	0



(V) $f(x) = 4x^2 - 4x$

Sol

$$y = 4x^2 - 4x$$

X-intercept

Put, $y = 0$

$$4x^2 - 4x = 0$$

$$4x(x - 1) = 0$$

Y-intercept

Put $x = 0$

$$y = 4(0)^2 - 4(0)$$

$$4x = 0 \quad x - 1 = 0$$

$$x = 0 \quad x = 1$$

$$y = 0 - 0$$

$$y = 0$$

$(0,0)$ and $(1,0)$ are the
X-intercepts

$(0,0)$ is the
Y-intercept

Vertex

Here $x_1 = 0$, $x_2 = 1$

$$x = \frac{-b}{2a}$$

$$x = \frac{x_1 + x_2}{2} = \frac{0 + 1}{2}$$

$$x = \frac{-(-4)}{2(4)} = \frac{4}{8} = \frac{1}{2}$$

$$x = 0.5$$

$$x = 0.5$$

Put $x = 0.5$ in given function

$$y = 4x^2 - 4x$$

$$y = 4(0.5)^2 - 4(0.5)$$

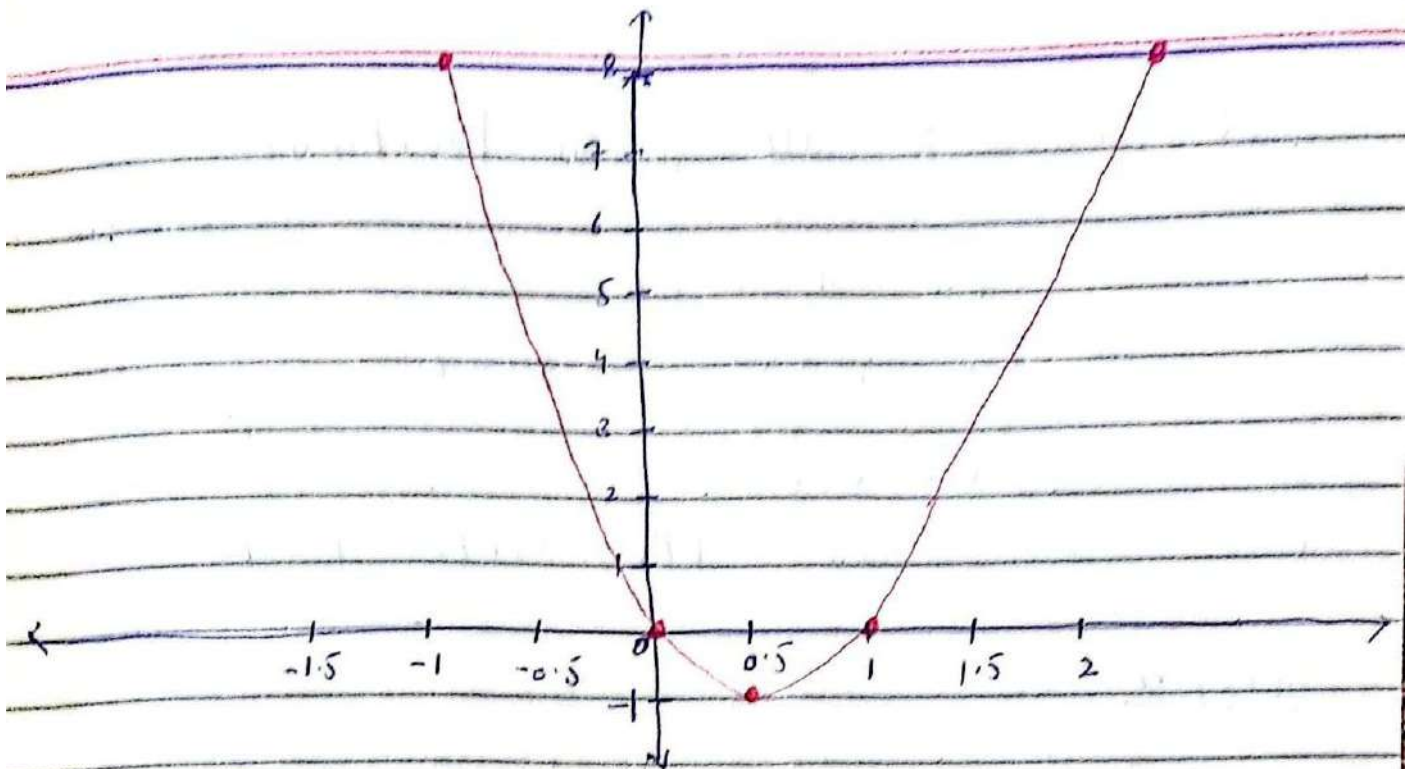
$$y = -1$$

$(0.5, -1)$ is the vertex point.

Graph

Available at MathCity.org

x		-1	0	0.5	1	2
y		8	0	-1	0	8



(VI) $F(x) = 6 - x^2 - x$

Sol

$y = -x^2 - x + 6$

$a = -1, b = -1, c = 6$

X-intercept

Y-intercept

Put $y = 0$

Put $x = 0$

$-x^2 - x + 6 = 0$

$y = 0 - 0 + 6$

$x^2 + x - 6 = 0$

$y = 6$

$x^2 + 3x - 2x - 6 = 0$

$x(x+3) - 2(x+3) = 0$

(0, 6) is the Y-intercept

$(x-2)(x+3) = 0$

$x-2 = 0 \quad x+3 = 0$

$x = 2 \quad x = -3$

(2, 0) and (-3, 0) are the X-intercepts.

Vertex

$x_1 = 2$

$x_2 = -3$

$x = \frac{x_1 + x_2}{2} = \frac{2 - 3}{2}$

$x = \frac{-b}{2a} = \frac{-(-1)}{2(-1)}$

$x = \frac{-1}{2} = -0.5$

$x = \frac{-1}{2} = -0.5$

Put $x = -0.5$ in given function.

$$y = -x^2 - x + 6$$

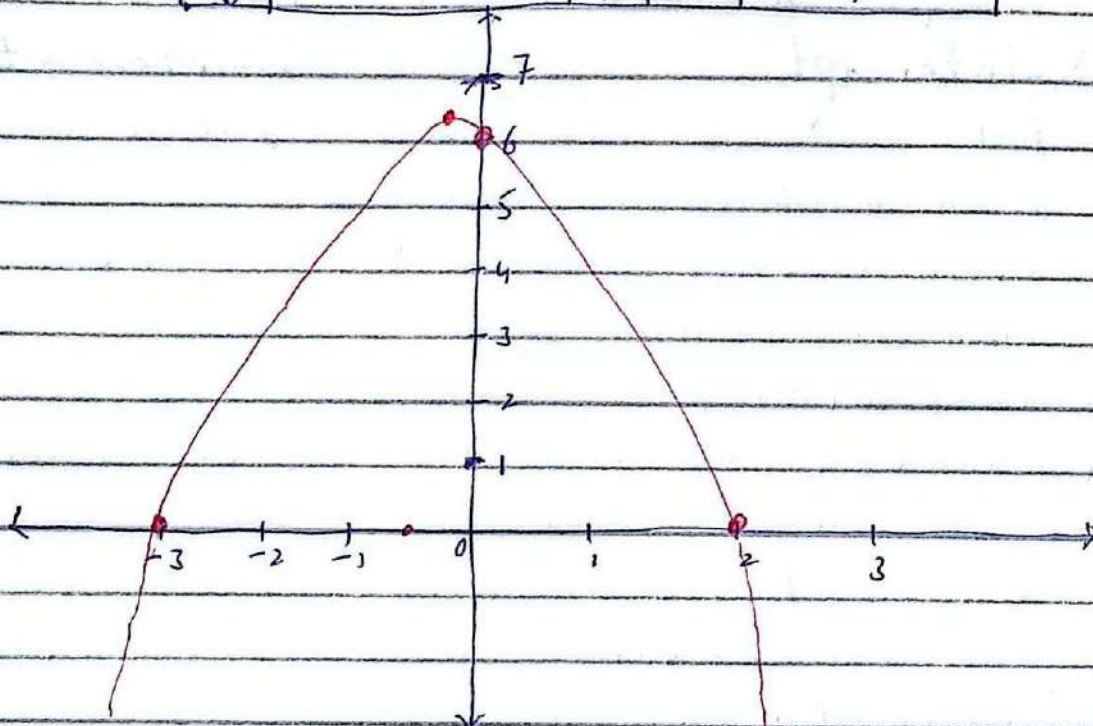
$$y = -(-0.5)^2 - (-0.5) + 6$$

$$y = 6.25$$

$(-0.5, 6.25)$ is the vertex point.

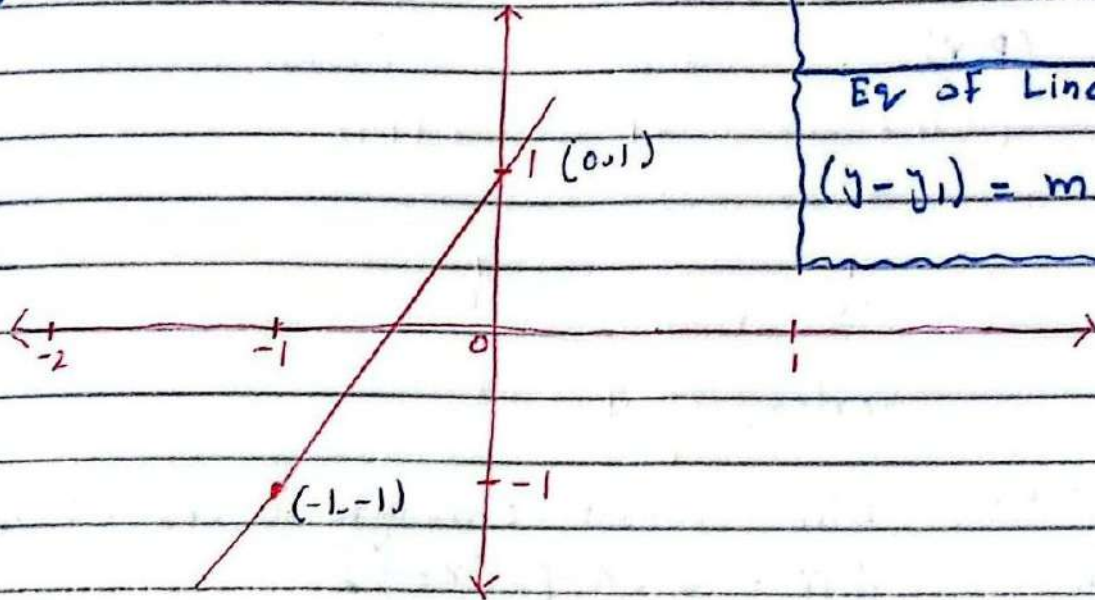
Graph

x	-3	-0.5	0	2	
y	0	6.25	6	0	



Q#5 Predict algebraic function from the Graph.

(ii)



$$\text{Slope} = m = \frac{y_2 - y_1}{x_2 - x_1}$$

Eq of Line

$$(y - y_1) = m(x - x_1)$$

Sol

The graph shows a line passing through points $(0, 1)$ and $(-1, -1)$
 $x_1 \quad y_1$ $x_2 \quad y_2$

Slope of the line is

$$m = \frac{y_2 - y_1}{x_2 - x_1} = \frac{-1 - 1}{-1 - 0} = \frac{-2}{-1}$$

$$m = 2$$

Eq of line is

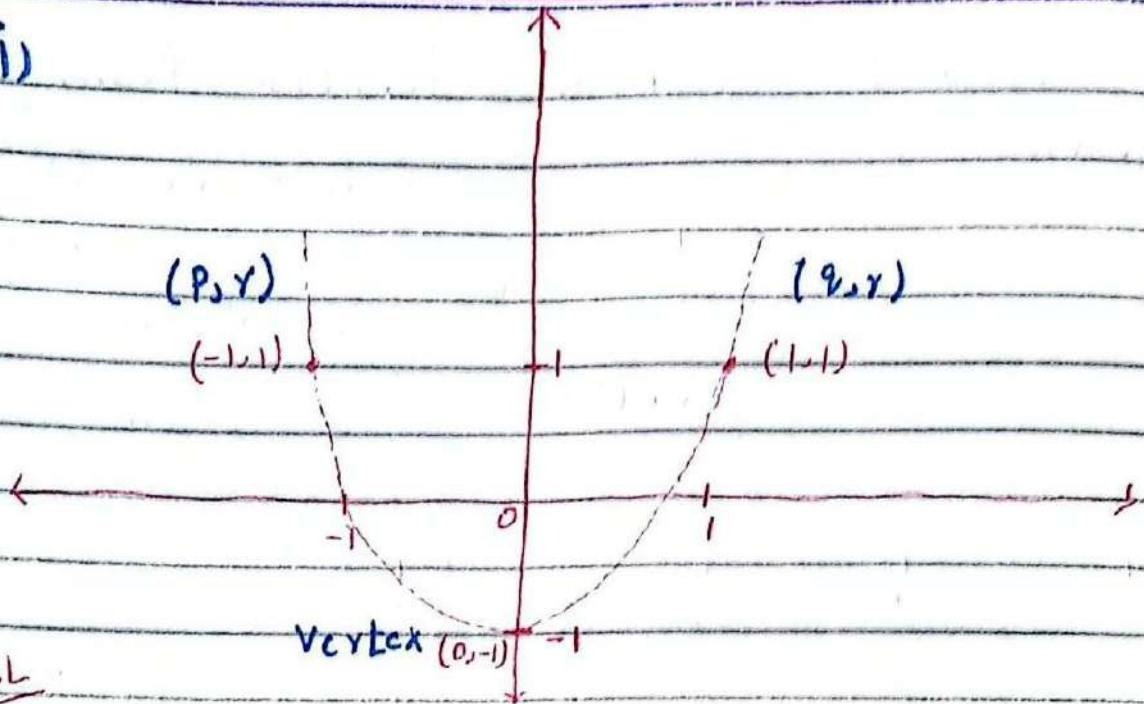
$$(y - y_1) = m(x - x_1)$$

$$(y - 1) = 2(x - 0)$$

$$y - 1 = 2x$$

$$y = 2x + 1 \quad \text{Ans}$$

(ii)



Sol

Note: Line Passes through (p, r) (q, r)
 Then $y - r = a(x - p)(x - q)$

$$(y - 1) = a(x + 1)(x - 1) \quad \text{--- i) 2nd Method}$$

Since $(0, -1)$ at Parabola

Put In (i)

$$x = 0, \quad y = -1$$

$$-1 - 1 = a(0 + 1)(0 - 1)$$

$$-2 = -a$$

$$a = 2$$

Put In (i)

$$y - 1 = 2(x + 1)(x - 1)$$

$$y - 1 = 2(x^2 - 1)$$

$$y = 2x^2 - 2 + 1$$

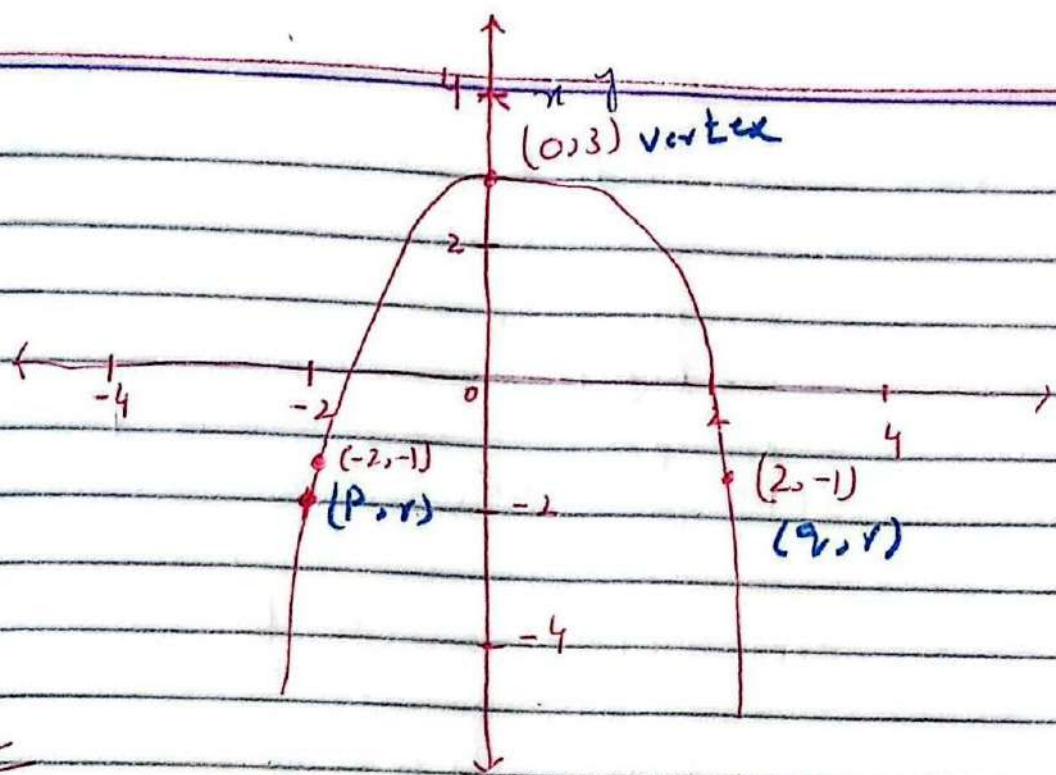
$$y = 2x^2 - 1$$

Ans

Vertex form
 $y = a(x - h)^2 + k$
 Vertex = $(h, k) = (0, -1)$
 $h = 0, k = -1$
 $y = a(x - 0)^2 + (-1)$
 $y = ax^2 - 1$
 As $(1, 1)$
 $1 = a(1)^2 - 1$
 $1 + 1 = a$
 $a = 2$

$$y = 2x^2 - 1 \quad \text{Ans}$$

(iii)



SOL

$$(y - r) = a (x - P) (x - Q) \quad \text{--- (1)}$$

$$(y + 1) = a (x + 2) (x - 2) \quad \text{--- (2) 2nd Method}$$

Since (0, 3) at parabola.

$$x = 0, \quad y = 3$$

$$(3 + 1) = a (0 + 2) (0 - 2)$$

$$4 = a (-4)$$

$$a = -1$$

Put in (2)

$$y + 1 = -1 (x + 2) (x - 2)$$

$$y + 1 = -1 (x^2 - 4)$$

$$y + 1 = -x^2 + 4$$

$$y = -x^2 + 4 - 1$$

$$y = -x^2 + 3$$

$$y = a(x - h)^2 + k$$

Vertex = (h, k) = (0, 3)

$$h = 0, \quad k = 3$$

$$y = a(x - 0)^2 + 3$$

$$y = ax^2 + 3$$

As point (2, -1)

$$-1 = a(2)^2 + 3$$

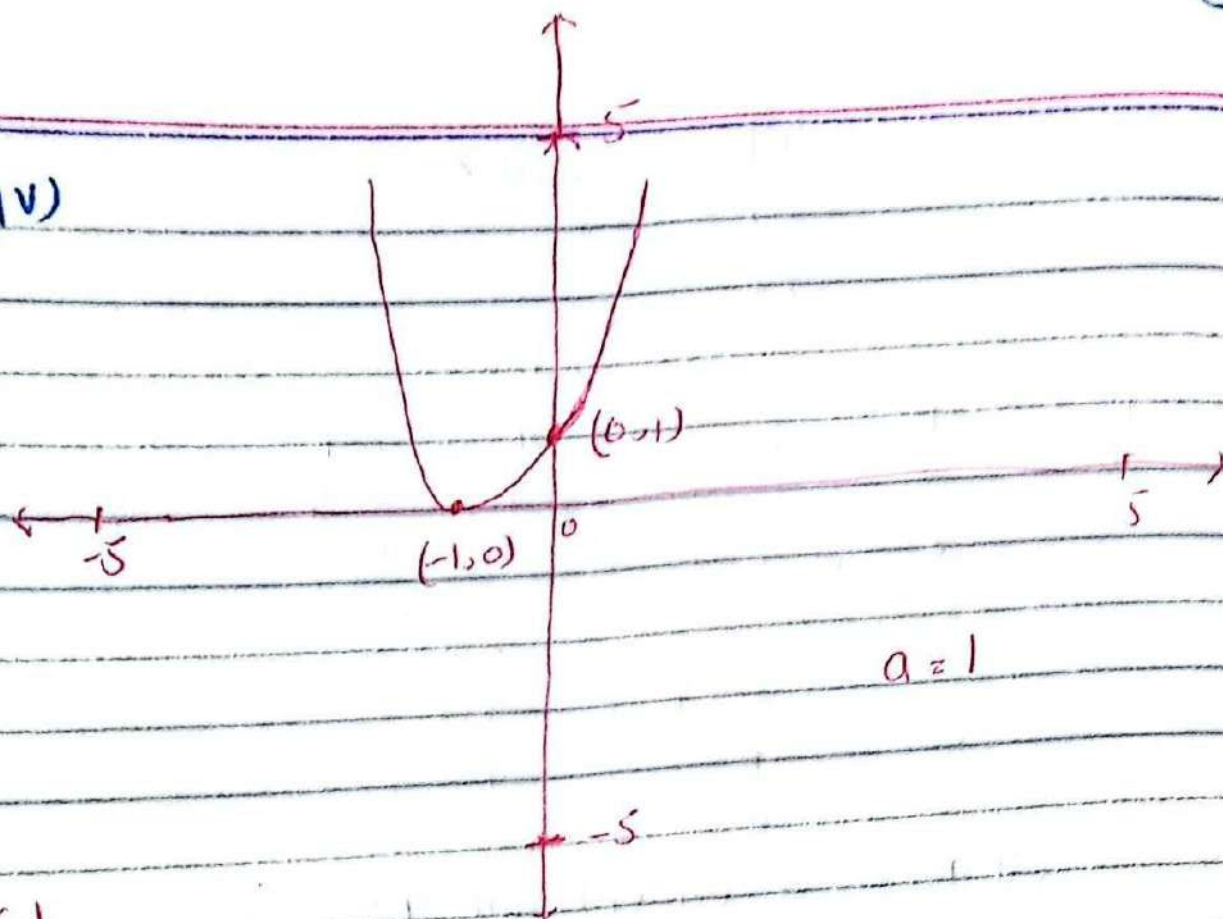
$$-1 - 3 = a \cdot 4$$

$$-4 = a$$

$$a = -1$$

$$y = -x^2 + 3 \quad \text{Ans.}$$

(iv)

Sol

$$y - r = a(x - p)(x - q)$$

$$\text{Vertex } = (h, k) = (-1, 0)$$

$$y = a(x - h)^2 + k$$

$$y = 1(x + 1)^2 + 0$$

$$y = (x + 1)^2 \quad \text{Ans}$$

Q#6 Plot the graph and find Point of intersection with axis.

i) $y = x + 3$

Sol

X-intercept

Put $y = 0$

$$x + 3 = 0$$

$$x = -3$$

$(-3, 0)$ is X-intercept

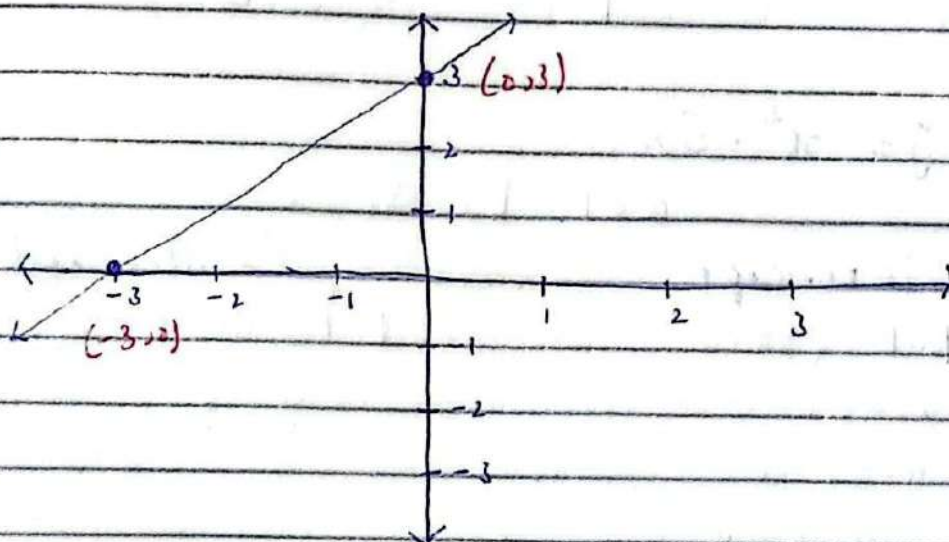
Y-intercept

Put $x = 0$

$$y = 0 + 3$$

$$y = 3$$

$(0, 3)$ is Y-intercept



ii) $y = 6 - 3x$

Sol

X-intercept

Put $y = 0$

$$6 - 3x = 0$$

$$-3x = -6$$

$$x = 2$$

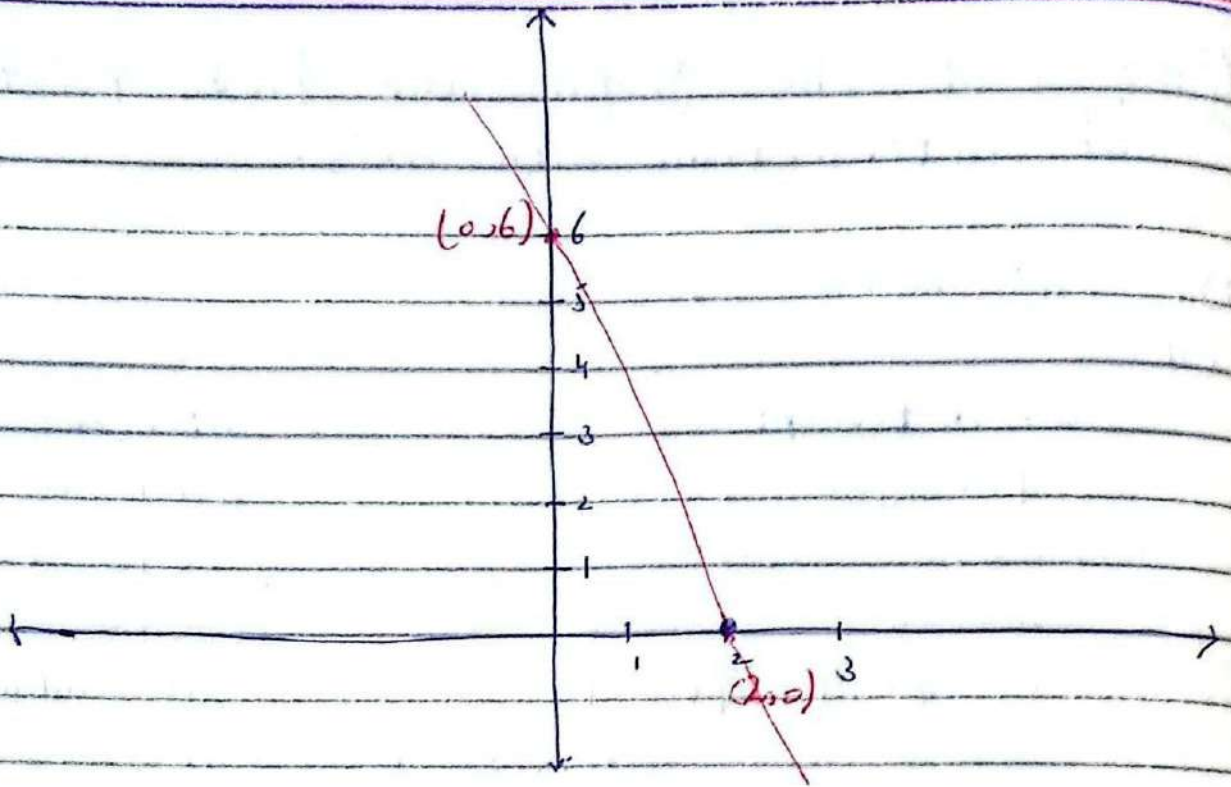
$(2, 0)$ is the X-intercept

Y-intercept

Put $x = 0$

$$y = 6$$

$(0, 6)$ is the Y-intercept



(iii) $y = x^2 - 5x$

$a = 1, b = -5, c = 0$

Sol

x-intercept

Put $y = 0$

$x^2 - 5x = 0$

$x(x - 5) = 0$

$x = 0 \quad x - 5 = 0$

$x = 0 \quad x = 5$

$(0, 0)$ $(5, 0)$ is the

x-intercept

y-intercept

Put $x = 0$

$y = 0$

$(0, 0)$ is the y-intercept

کیونکہ یہ Quadratic Function ہے تو اس کا Graph Parabola ہے، Parabola کے لئے Vertex پائی جاتی ہے، ابھی ہم Vertex معلوم کرنے کے ہیں۔

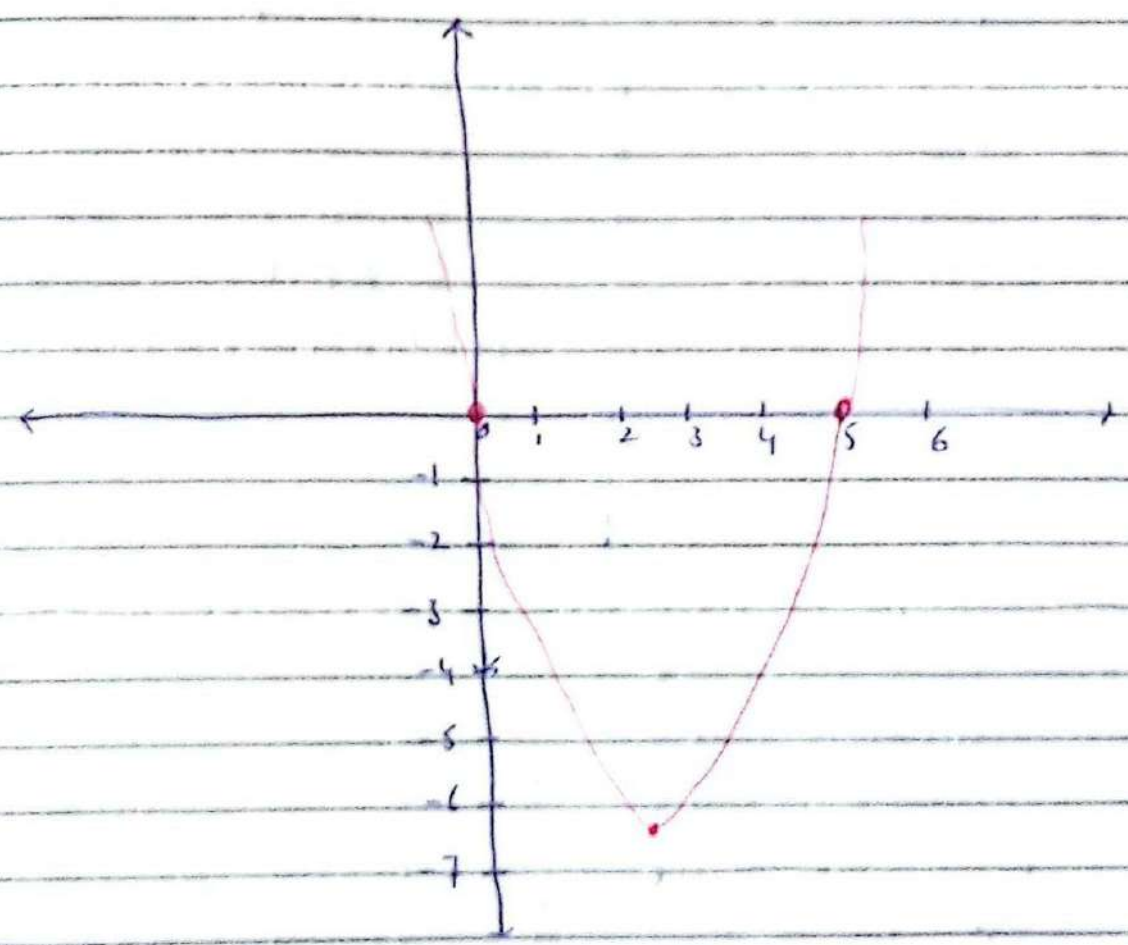
Vertex

$$x = \frac{-b}{2a} = \frac{-(-5)}{2(1)} = \frac{5}{2} = 2.5$$

Put $x = 2.5$ in given function:

$$y = x^2 - 5x$$
$$y = (2.5)^2 - 5(2.5)$$
$$y = -6.25$$

$(2.5, -6.25)$ is the vertex point.



Q#7: Find graphical solution of

1) $F(x) = 4 - 3x$

$g(x) = -x + 1$

SOL Let

$y = 4 - 3x$ —(i)

$y = -x + 1$

Rough work نکات سے بات کریں

$$4 - 3x = -x + 1$$

$$-3x + x = 1 - 4$$

$$-2x = -3 \quad x = \frac{3}{2} = 1.5$$

$y = 4 - 3x$ —(i)

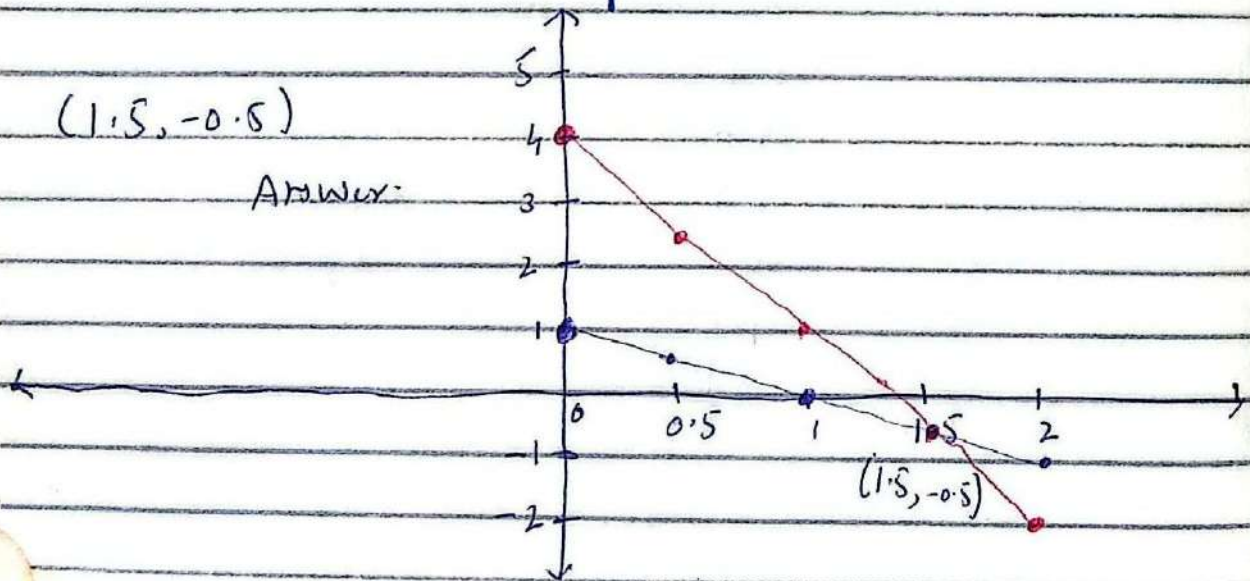
$y = -x + 1$ —(ii)

x	0	0.5	1	1.5	2
y	4	2.5	1	-0.5	-2

x	0	0.5	1	1.5	2
y	1	0.5	0	-0.5	-1

(1.5, -0.5)

Answer:



iii) $F(x) = 2(2+x)$, $g(x) = x^2 + 1$

Sol

Let $y = 2(2+x)$ - (i) $y = x^2 + 1$ - (ii)

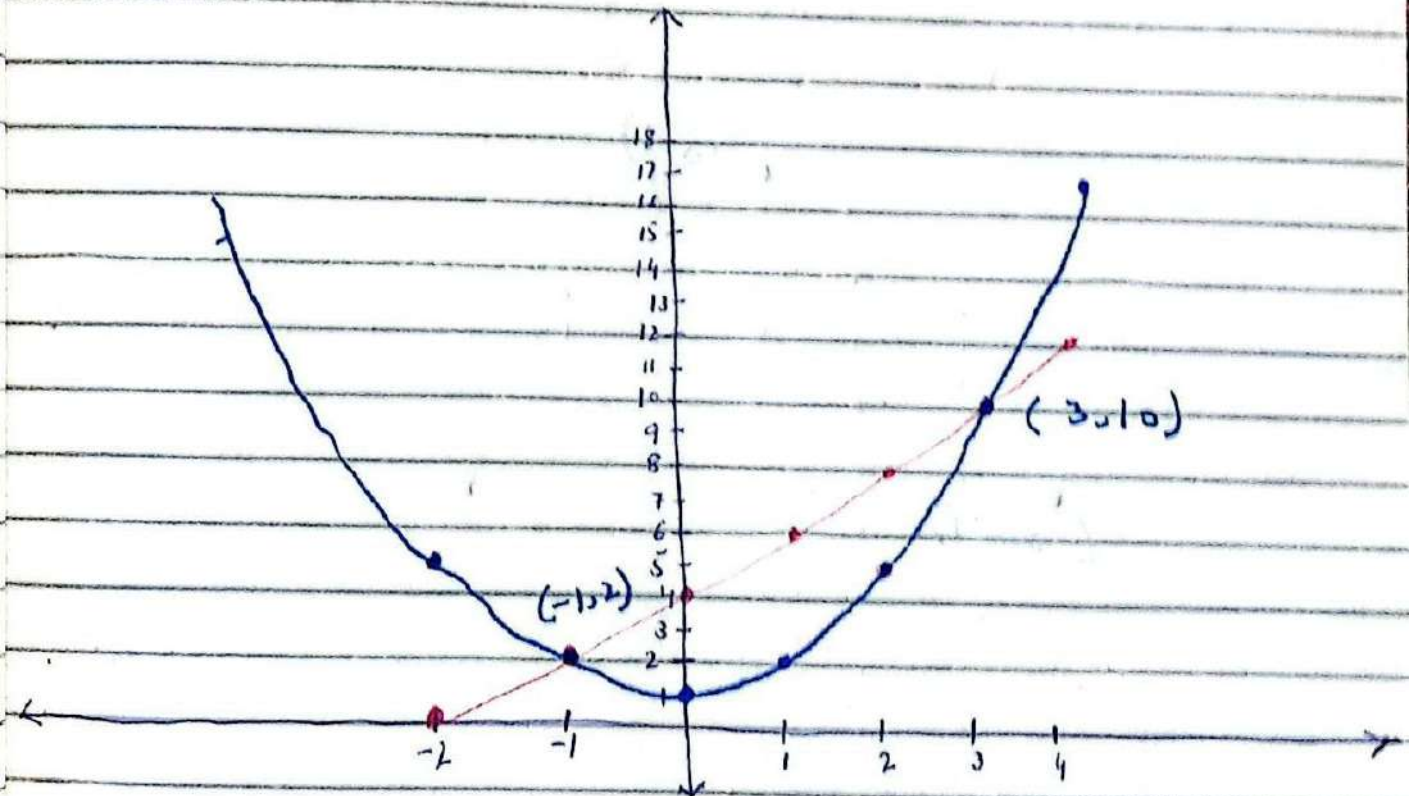
R.W	$2(2+x) = x^2 + 1$
	$4 + 2x = x^2 + 1$
	$x^2 + 1 - 2x - 4 = 0$
	$x^2 - 2x - 3 = 0$
	$x^2 - 3x + x - 3 = 0$
	$x(x-3) + (x-3) = 0$
	$(x+1) = 0$ $x-3 = 0$
	$x = -1$ $x = 3$

$y = 2(2+x)$

$y = x^2 + 1$

x	-2	-1	0	1	2	3	4
y	0	2	4	6	8	10	12

x	-2	-1	0	1	2	3	4
y	5	2	1	2	5	10	17



(iii) $f(x) = 5 + 3x$

$g(x) = -x^2 + 5$

Sol

$y = 5 + 3x$

$y = -x^2 + 5$

R.W

$$5 + 3x = -x^2 + 5$$

$$x^2 + 5 + 3x - 5 = 0$$

$$x^2 + 3x = 0$$

$$x(x + 3) = 0$$

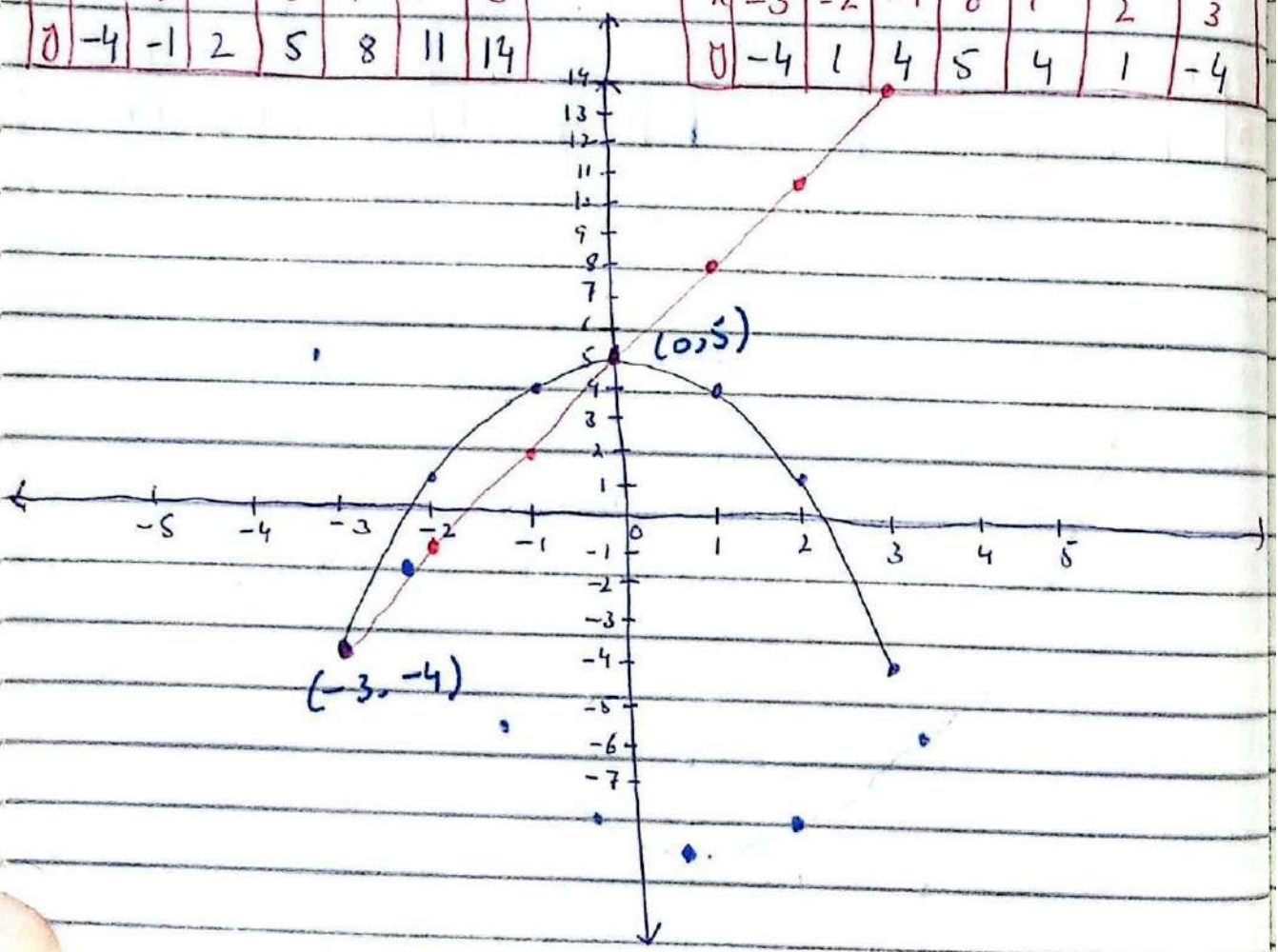
$$x = 0 \qquad x = -3$$

$y = 5 + 3x$

$y = -x^2 + 5$

x	-3	-2	-1	0	1	2	3
y	-4	-1	2	5	8	11	14

x	-3	-2	-1	0	1	2	3
y	-4	1	4	5	4	1	-4



(iv) $g(x) = -2x^2 + 2x + 5$

$F(x) = 1$

Sol

$y = 1$

$y = -2x^2 + 2x + 5$

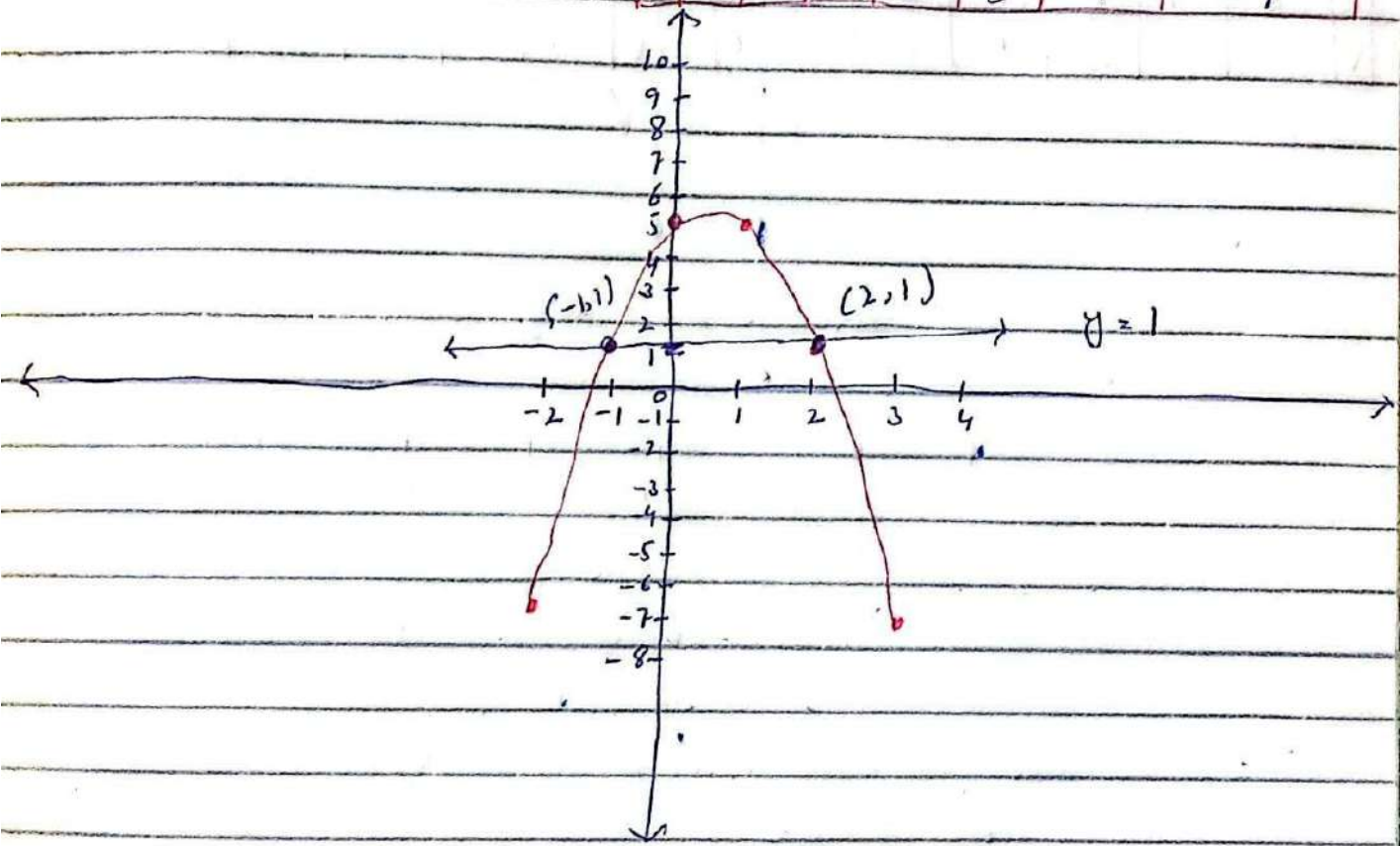
R-w	$-2x^2 + 2x + 5 = 1$
	$-2x^2 + 2x + 5 - 1 = 0$
	$-2x^2 + 2x + 4 = 0$
	$x^2 - x - 2 = 0$
	$x^2 - 2x + x - 2 = 0$
	$x(x-2) + 1(x-2) = 0$
	$(x+1)(x-2) = 0$
	$x = -1 \quad \quad x = 2$

$y = 1$

$y = -2x^2 + 2x + 5$

(No Table)

x	-3	-2	-1	0	1	2	3
y	-19	-7	1	5	5	1	-7



(v) $f(x) = 2 + 3x + x^2$

$g(x) = 5 + 3x - 2x^2$

Sol

$y = 2 + 3x + x^2$

$y = 5 + 3x - 2x^2$

R-w

$$2 + 3x + x^2 = 5 + 3x - 2x^2$$

$$2 + 3x + x^2 - 5 - 3x + 2x^2 = 0$$

$$3x^2 - 3 = 0$$

$$3(x^2 - 1) = 0$$

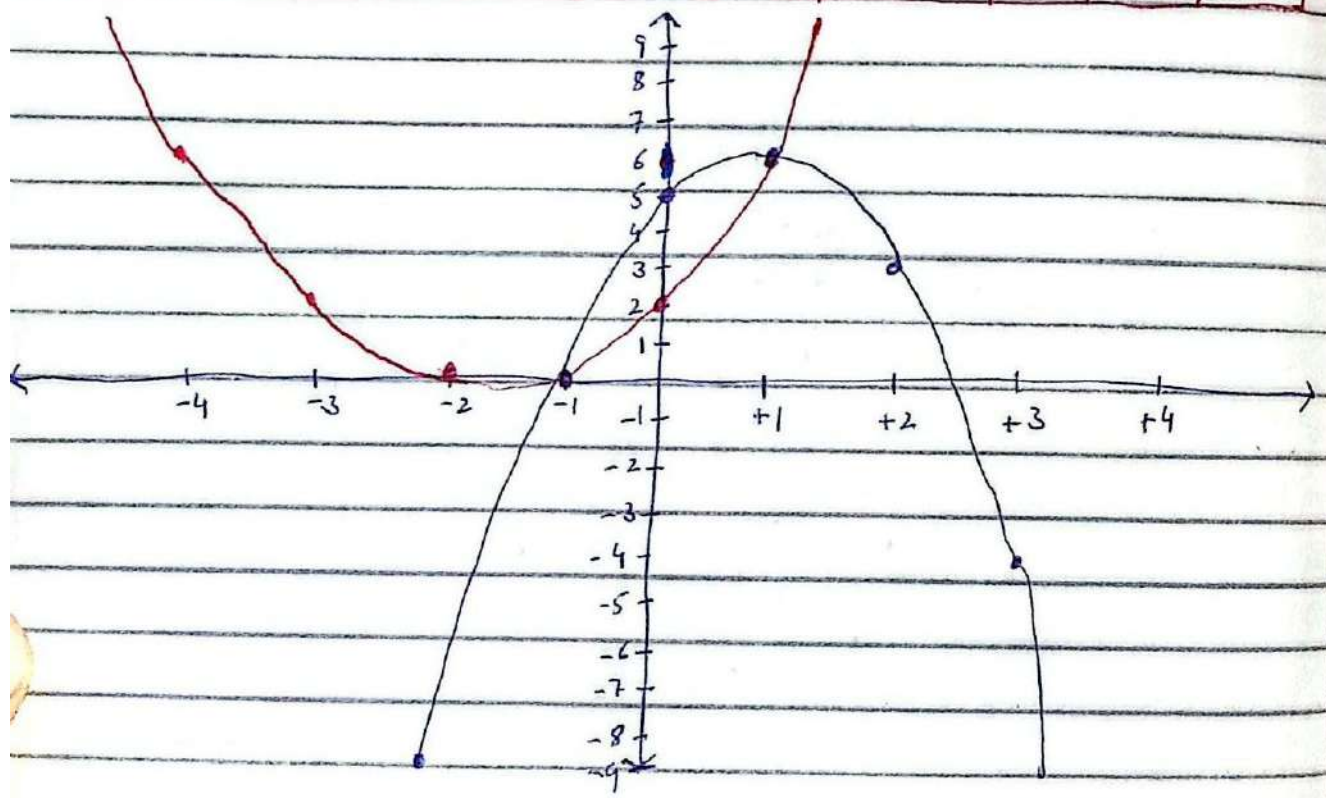
$$(x+1)(x-1) = 0$$

$$x = -1, \quad x = 1$$

$y = 2 + 3x + x^2$

$y = 5 + 3x - 2x^2$

x	-2	-1	0	1	2	-3	-4	x	-2	-1	0	1	2	3
y	0	0	2	6	12	2	6	y	-9	0	5	6	3	

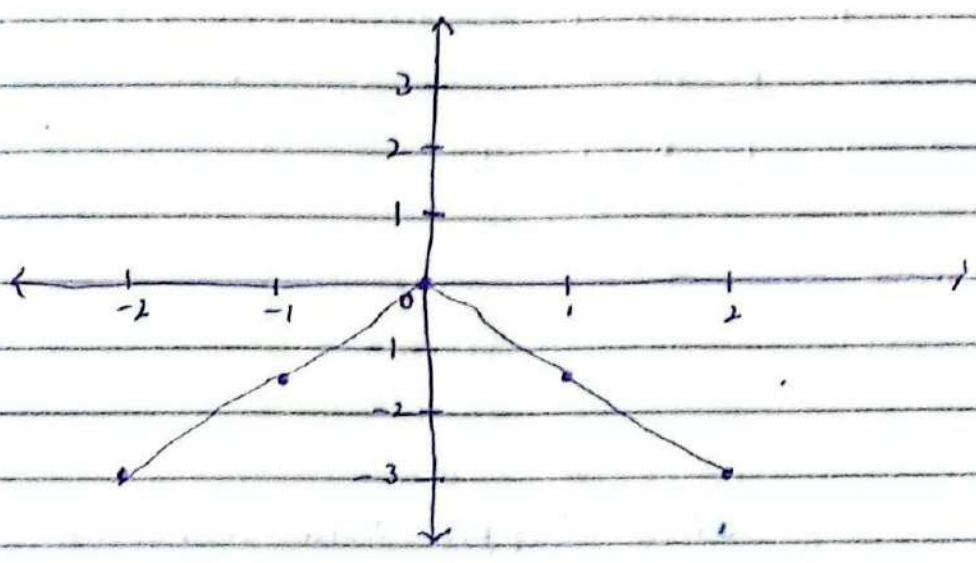


Q#8 Draw the Graph of Modulus Function

i) $f(x) = -1.5|x|$

Sol

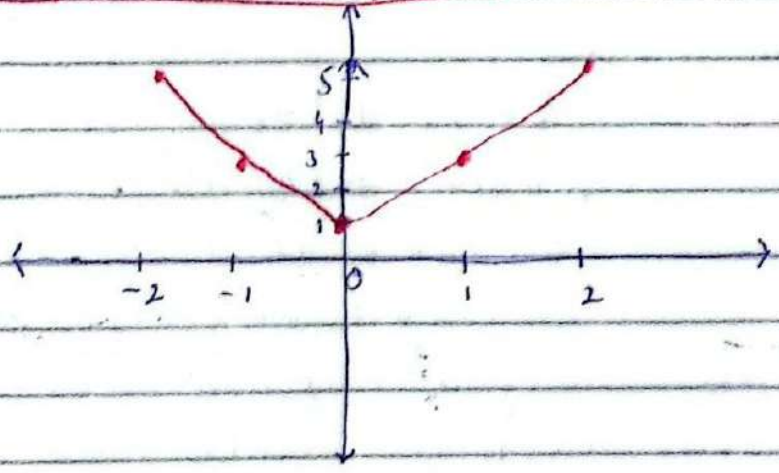
x	-2	-1	0	1	2
f	-3	-1.5	0	-1.5	-3



ii) $f(x) = 1 + 2|x|$

Sol

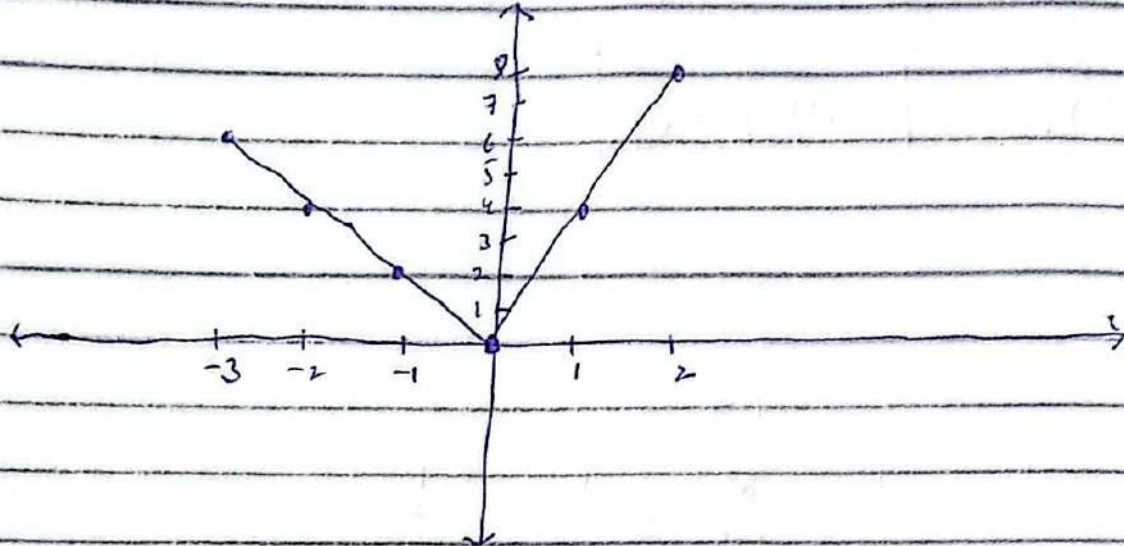
x	-2	-1	0	1	2
f	5	3	1	3	5



$$(iii) f(x) = 3|x| + x$$

Sol

x	3	-2	-1	0	1	2
y	6	4	2	0	4	8



Q#9

The Eq. for supply and demand are given by two linear equation.

Sol $S(x) = 2x + 10$ —(i) $D(x) = -3x + 40$ —(ii)

Condition

$$S(x) = D(x)$$

$$2x + 10 = -3x + 40$$

$$2x + 3x = 40 - 10$$

$$5x = 30$$

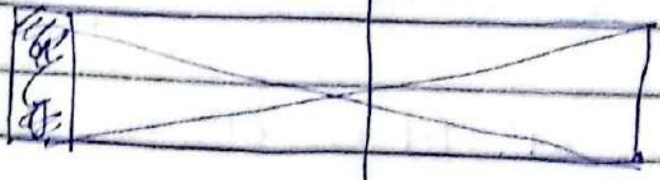
$$x = 6$$

Put in (i)

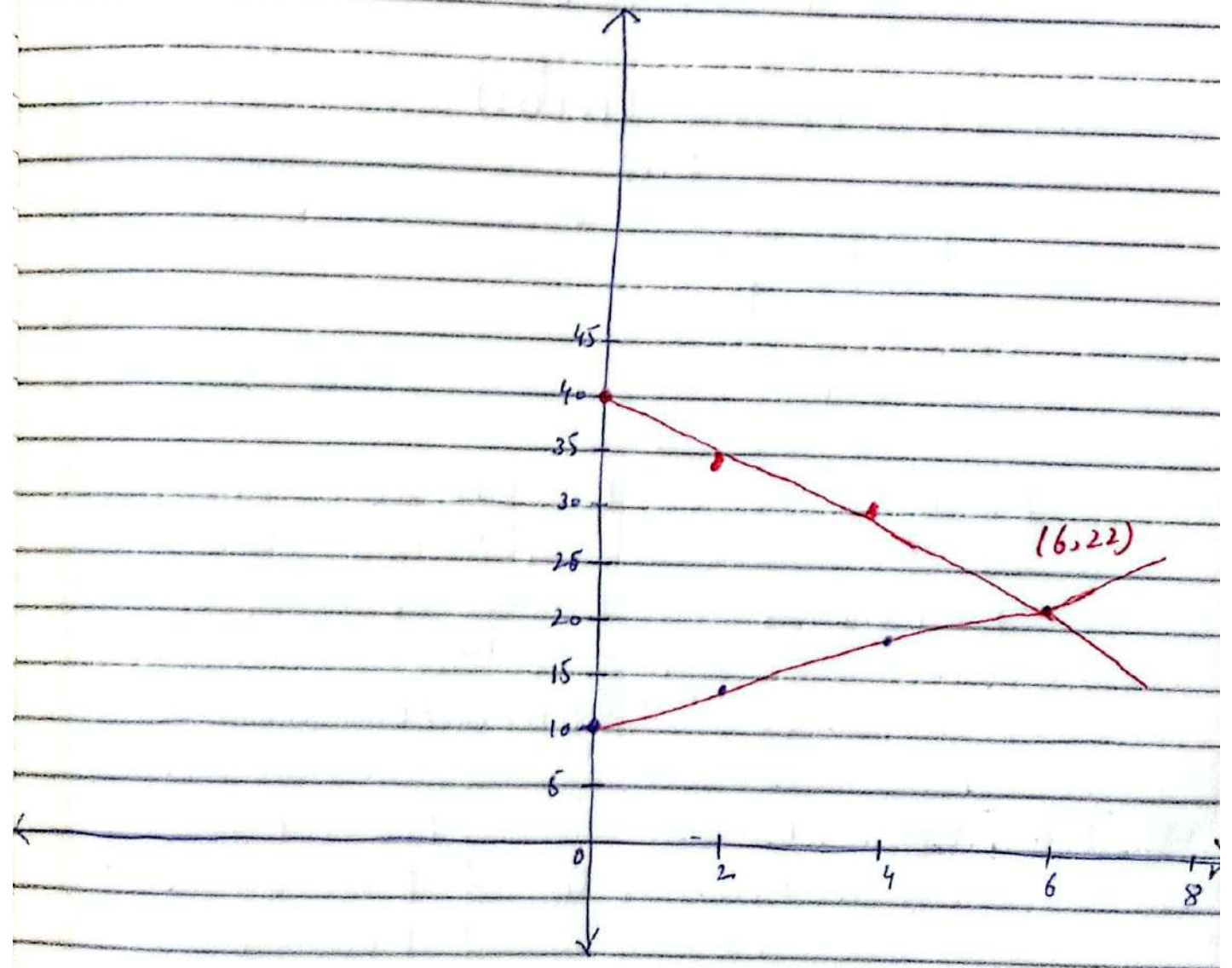
Put in (ii)

$$S(6) = 2(6) + 10$$
$$S(6) = 22$$

$$D(6) = -3(6) + 40$$
$$D(6) = 22$$



x	0	2	4	6		x	0	2	4	6
y	10	14	18	22		y	40	34	32	22



Q#10 Suppose a ball is thrown into the air

Sol

$$h(t) = -6t^2 + 10t + 5 \quad \text{---(i)}$$

$$h(t) = 9t \quad \text{---(ii)}$$

$$\text{Eq (i)} = \text{Eq (ii)}$$

$$-6t^2 + 10t + 5 = 9t$$

$$6t^2 - 10t - 5 + 9t = 0$$

$$6t^2 - t - 5 = 0$$

$$a = 6, \quad b = -1, \quad c = -5$$

$$t = \frac{1 \pm \sqrt{(-1)^2 - 4(6)(-5)}}{2(6)}$$

$$t = \frac{1 \pm \sqrt{1 + 120}}{12}$$

$$t = \frac{1 \pm 11}{12}$$

$$t = \frac{12}{12}$$

$$t = 1 \text{ sec}$$

$$t = \frac{-10}{12}$$

$$t = \frac{-10}{12}$$

(Distance/Time cannot be negative)

Put $t = 1$ in (ii)

$$h(1) = 9(1)$$

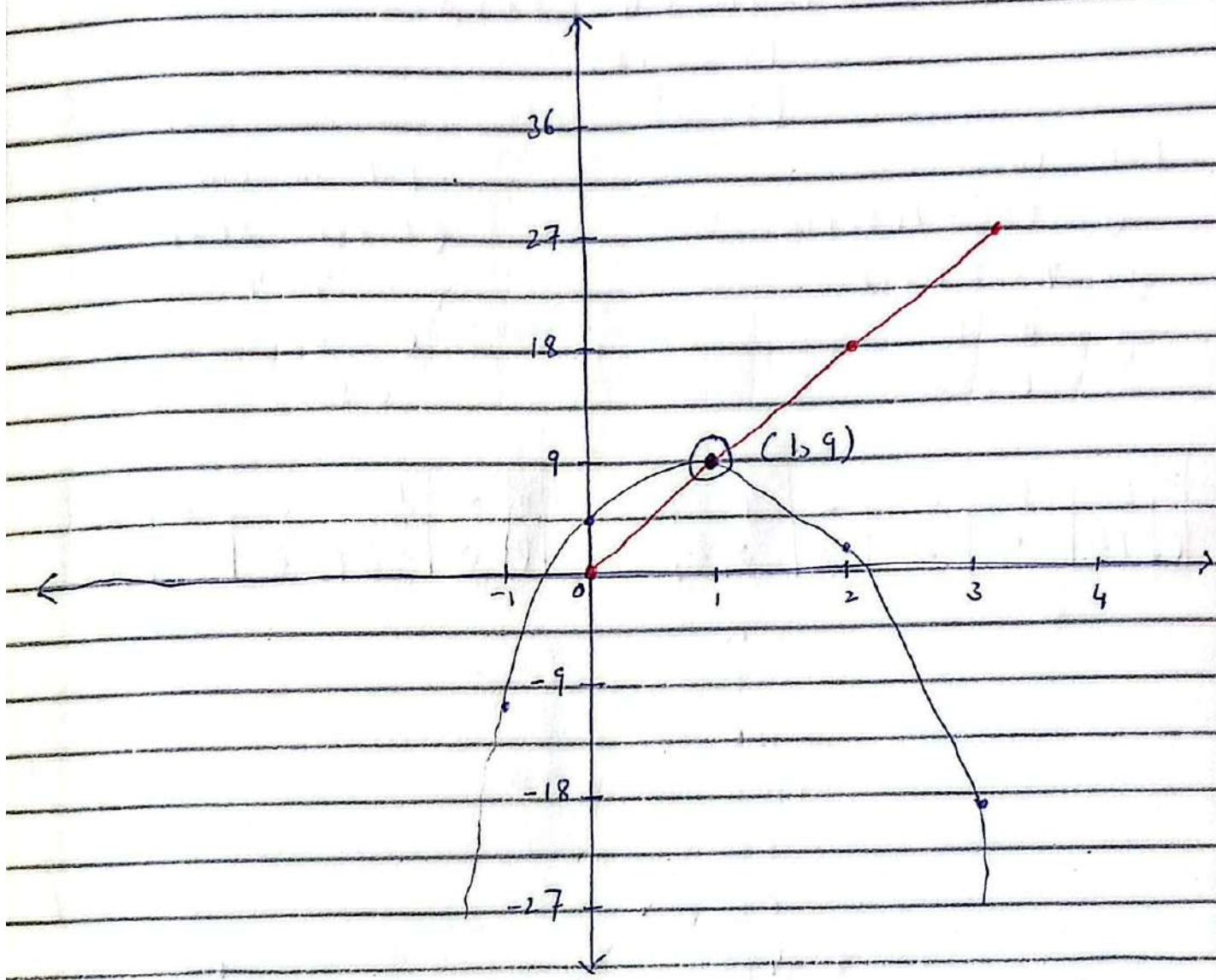
$$h(1) = 9$$

Put $t = 1$ in (i)

$$h(1) = -6(1)^2 + 10(1) + 5$$

$$h(1) = 9$$

t	0	1	2	3	-1	t	0	1	2	3
0	5	9	1	-19	-11	0	0	9	18	27



Q#11 Two asteroids are following the Parabolas.

Sol

$$F(n) = n^2 - 7n + 12 \text{ --- (1)}$$

$$g(n) = n(n-3) \text{ --- (2)}$$

$$y = n^2 - 7n + 12$$

$$y = n^2 - 3n$$

Eq (i) = Eq (ii)

$$x^2 - 7x + 12 = x^2 - 3x$$

$$x^2 - 7x + 12 - x^2 + 3x = 0$$

$$-4x = -12$$

$$x = 3$$

Put in (i)

$$y = (3)^2 - 7(3) + 12$$

$$y = 9 - 21 + 12$$

$$y = 0$$

(3, 0)

Put in (ii)

$$y = (3)^2 - 3(3)$$

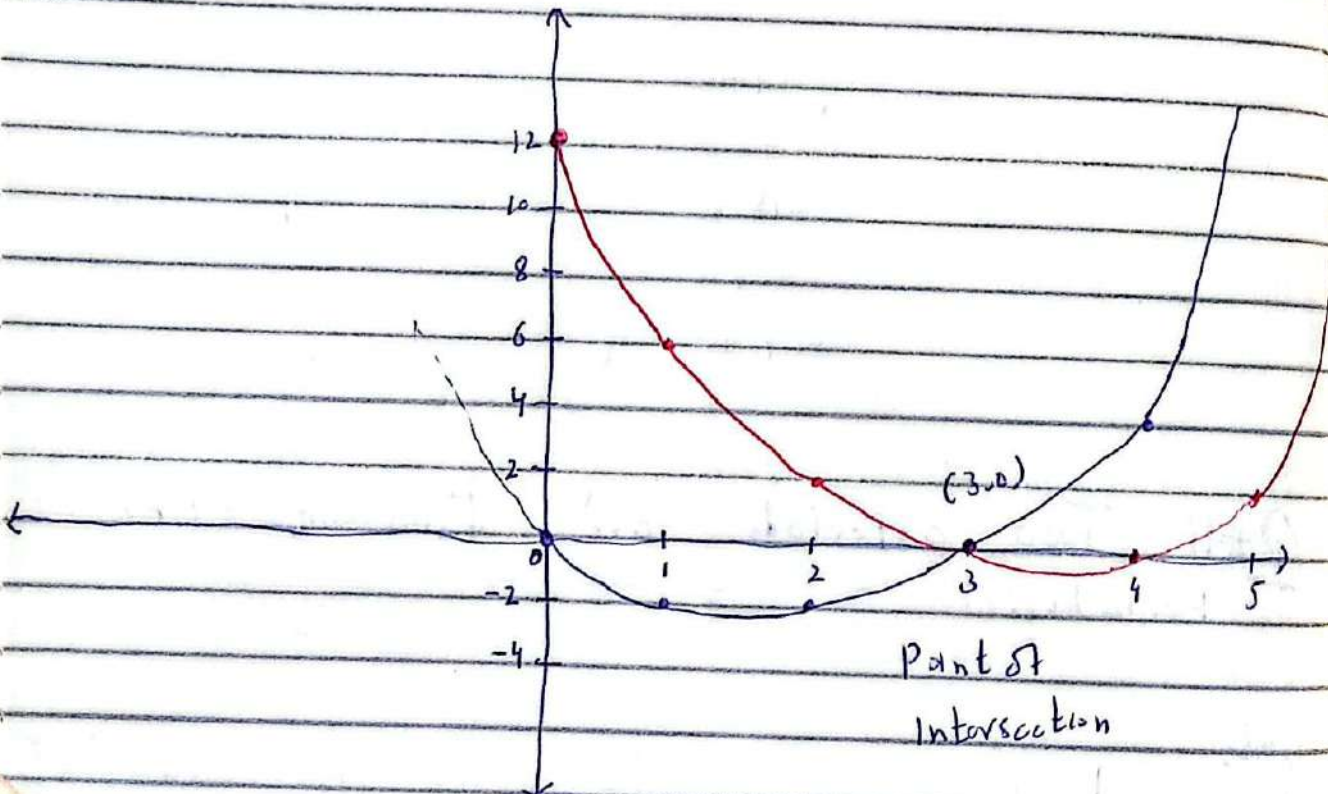
$$y = 9 - 9$$

$$y = 0$$

(3, 0)

x	0	1	2	3	4	5
y	12	6	2	0	0	2

x	0	1	2	3	4
y	0	-2	-2	0	4



Complete