

6.1

1. Find the next four terms of each sequence

Exercise 6.1
Mathematics 11 (PECTAA)
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Available at MathCity.org

(i) 12, 16, 20,

First term = 12, 16, 20,

4 is added every time, so

$$\text{Next term} = 20 + 4 = 24$$

$$\text{2nd term} = 24 + 4 = 28$$

$$\text{3rd term} = 28 + 4 = 32$$

$$\text{4th term} = 32 + 4 = 36$$

(ii) 3, 1, -1,

2 is subtracted every time, so
get new term, so

$$\text{Next first term} = -1 - 2 = -3$$

$$\text{2nd term} = -3 - 2 = -5$$

$$\text{3rd term} = -5 - 2 = -7$$

$$\text{4th term} = -7 - 2 = -9$$

2. Write down the first three terms of each of the following sequences:

$$(i) a_n = 3n + 5$$

$$\text{Put } n=1$$

$$a_1 = 3(1) + 5 = 3 + 5 = 8$$

$$\text{Put } n=2$$

$$a_2 = 3(2) + 5 = 6 + 5 = 11$$

$$\text{Put } n=3$$

$$a_3 = 3(3) + 5 = 9 + 5 = 14$$

$$8, 11, 14$$

$$(ii) a_{n+1} = 4a_n - 7 \text{ and } a_1 = 3$$

$$a_1 = 3$$

$$\text{let } n=1$$

$$a_{1+1} = 4a_1 - 7$$

$$a_2 = 4(3) - 7$$

$$a_2 = 12 - 7$$

$$a_2 = 5$$

$$\text{Put } n=2$$

$$a_{2+1} = 4a_2 - 7$$

$$a_3 = 4(5) - 7$$

$$a_3 = 20 - 7 = 13$$

$$3, 5, 13$$

$$(iii) a_n = (n-3)(n+1)$$

$$\text{if } n=1$$

$$a_1 = (1-3)(1+1)$$

$$= (-2)(2)$$

$$a_1 = -4$$

$$\text{Put } n=2$$

$$a_2 = (2-3)(2+1)$$

$$a_2 = (-1)(3)$$

$$a_2 = -3$$

$$\text{Put } n=3$$

$$a_3 = (\cancel{3}-\cancel{3})(3+1)$$

$$a_3 = (0)(4)$$

$$a_3 = 0$$

$$-4, -3, 0$$

$$(iv) a_1 = -1, a_{n+1} = \frac{3}{a_{n+2}}$$

$$\text{let } n=1$$

$$a_{1+1} = \frac{3}{a_{1+2}}$$

$$a_2 = \frac{3}{a_3}$$

$$a_2 = \frac{3}{-1+2}$$

$$= \frac{3}{1} = 3$$

$$a_2 = \frac{3}{1} = 3$$

Put $n=2$

$$a_{2+1} = 3$$

$$a_{2+2}$$

$$a_3 = 3$$

$$3+2$$

$$a_3 = \frac{3}{5}$$

$$-1, 3, \frac{3}{5}$$

$$(v) a_n = 8 - \frac{20}{3+n}$$

$$3+n$$

Put $n=1$

$$a_1 = 8 - \frac{20}{3+1}$$

$$3+1$$

$$a_1 = 8 - \frac{20 \cdot 5}{4}$$

$$a_1 = 8 - 5 = 3$$

Put $n=2$

$$a_2 = 8 - \frac{20}{3+2}$$

$$3+2$$

$$a_2 = 8 - \frac{20 \cdot 4}{5}$$

$$a_2 = 8 - 4 = 4$$

Put $n=3$

$$a_3 = 8 - \frac{20}{3+3}$$

$$a_3 = 8 - \frac{20}{6}$$

$$a_3 = \frac{48-20}{6} = \frac{28}{6}$$

$$a_3 = \frac{14}{3}$$

$$3, 4, \frac{14}{3}$$

(vi) $a_1 = 1, a_{n+1} = (3a_n + 2)^2$

Put $n=1$

$$a_{1+1} = (3a_1 + 2)^2$$

$$a_2 = (3(1) + 2)^2$$

$$a_2 = (5)^2 = 25$$

Put $n=2$

$$a_{2+1} = (3a_2 + 2)^2$$

$$a_3 = (3(25) + 2)^2$$

$$a_3 = (75 + 2)^2 = (77)^2 = 5929$$

$$1, 25, 5929$$

(vii) $a_n = (-2n)^2$

Put $n=1$

$$a_1 = (-2(1))^2$$

$$a_1 = (-2)^2 = 4$$

Put $n=2$

$$a_2 = (-2(2))^2$$

$$a_2 = (-4)^2 = 16$$

Put $n=3$

$$a_3 = (-2(3))^2$$

$$a_3 = (-6)^2 = 36 \quad 4, 16, 36$$

(viii) $a_n = (-1)^n 7n^2$

Put $n=1$

$$a_1 = (-1)^1 7(1)^2$$

$$a_1 = -1 \times 7 = -7$$

Put $n=2$

$$a_2 = (-1)^2 7(2)^2$$

$$a_2 = 1 \times 7 \times 4$$

$$a_2 = 28$$

Put $n=3$

$$a_3 = (-1)^3 7(3)^2$$

$$a_3 = (-1) \times 7(9)$$

$$a_3 = -63$$

$$-7, 28, -63$$

3. An expression for the n^{th} triangular number is $\frac{n(n+1)}{2}$. Write down the 15th triangular number. Make a triangle of dots by taking $n=5$.

$$n\text{th term} = \frac{n(n+1)}{2}$$

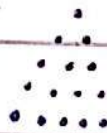
$$\text{let } n=15$$

$$15\text{th term} = \frac{15(15+1)}{2}$$

$$15\text{th term} = \frac{15 \times 16}{2} = 15 \times \frac{16}{2}$$

$$15\text{th term} = 15 \times 8 = 120$$

Now triangle with $n=5$ dots.



4. Write down the n^{th} term of each of the following sequences:

(i) 1, 4, 9, ...

$$(1)^2, (2)^2, (3)^2, \dots$$

$$n\text{th term} = n^2$$

(ii) 1, 1+2, 1+2+3, ...

first term with single term

second term with two term

3rd term with three term

So,

$$n\text{th term} = 1+2+3+4, \dots +n$$

(iii) $a_1 b_1, a_2 b_2, a_3 b_3, \dots$

First term = $a_1 b_1$

Second term = $a_2 b_2$

Third term = $a_3 b_3$

nth term = $a_n b_n$

(iv) $x, 2x^2, 3x^3, \dots$

$$a_1 = x$$

$$a_2 = 2x^2$$

.....

$$a_n = nx^{n^2}$$

(v) $a_1, a_1 + d, a_1 + 2d, \dots$

first term = a_1

2nd term = $a_1 + d$

3rd term = $a_1 + 2d$

nth term = $a_1 + (n-1)d$

(vi) $a_1, a_1 r, a_1 r^2, \dots$

1st term = a_1

2nd term = $a_1 r$

3rd term = $a_1 r^2$

nth term = $a_1 r^{(n-1)}$

(vii) $a_1, 2a_2, 3a_3, \dots$

$b_1 + c_1, b_2 + c_2, b_3 + c_3$

$$\text{1st term} = \frac{a_1}{b_1 + c_1}$$

$$\text{2nd term} = \frac{2a_2}{b_2 + c_2}$$

$$\text{3rd term} = \frac{3a_3}{b_3 + c_3}$$

$$\text{nth term} = \frac{nan}{b_n + c_n}$$

(viii) $1, 1, 1, \dots$

$$a_1, a_1 + d, a_1 + 2d$$

$$\text{1st term} = \frac{1}{a_1}$$

$$\text{2nd term} = \frac{1}{a_1 + d}$$

$$\text{3rd term} = \frac{1}{a_1 + 2d}$$

$$\text{nth term} = a_n = \frac{1}{a_1 + (n-1)d}$$

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