



**COMSATS University Islamabad**  
Synopsis for MS  Ph.D.

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| Name: Muhammad Latif Khan Wali   | Registration No.: CIIT/FA14-RMT-001/ATK              |
| Program: RMT   | Area of Specialization (if any as per approved SoS): |
| Department: Mathematics  | Campus: Attock                                       |
| Date of admission: 13-04-2023  | Date of synopsis submission: 23-09-2023              |
| Proposed Title of the Thesis: (Use title case capitalization): The Gamma Function $\Gamma$ and Their Properties with Applications. |  |
| <b>Supervisory Committee</b>   |  |
| Name and Designation   | Role   |
| Dr. Super Visor (Tenured Associate Professor)  | Supervisor   |
| Dr. Co Super Visor (Assistant Professor)   | Cosupervisor/Member                                  |
| Dr. Pervais Shah (Lecturer)  | Member   |
| Dr. 2nd Sahadfad (Tenured Professor)   | Member   |

Student's Signature: \_\_\_\_\_

**Summary of the Research** Assume that  $\alpha$  is monotonically increasing on  $[a, \infty)$  and  $f \in \mathcal{R}(\alpha; a, b)$  for every  $b \geq a$ . If  $0 \leq f_1(x) \leq f_2(x)$  for every  $x \geq a$  and  $\int_a^\infty f_2 d\alpha$  converges, then prove that  $\int_a^\infty f_1 d\alpha$  converges and we have  $\int_a^\infty f_1 d\alpha \leq \int_a^\infty f_2 d\alpha$ . Let  $\{f_n\}$  be a sequence of functions defined on an interval  $I$ , and  $x_0 \in I$ . If the sequence  $\{f_n\}$  converges uniformly to some function  $f$  on  $I$  and if each of the function  $f_n$  is continuous at  $x_0$ , then prove that the function  $f$  is also continuous at  $x_0$ .

## 1. Introduction

This section includes introduction starting from major domain and narrowing, down to specific domain. It should highlight motivation and includes introduction starting includes introduction starting.

## 2. Literature Review

Our aim is to derived Hadamard type inequality for  $h$  convex function on coordinates. We will introduce  $(h - m)$ -convex function on coordinates in rectangle in a plane and will derive the Hadamard type inequality connected to it.

Our aim is also to consider non-negative difference of these Hadamard type inequalities as a functional to discuss its various properties for different classes of  $\hat{h}$ -convex and  $(h - m)$ -convex function on coordinates.

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## 3. Problem Statement

After having a basic knowledge about the convex functions. I will read research paper [7] in detail, in which Ozdemir et al. discussed  $(h-m)$ -convex function, derived some Hermite-Hadamard inequalities for  $(h - m)$ -convex functions and proved some of their properties. And also I will read research paper [6], in which Sarikaya et. al. established a new Hadamard type inequality for  $h$ -convex functions. Moreover, I will

## 4. Research Objectives

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## 5. Research Methodology (or Material and Methods)

After having a basic knowledge about the convex functions. I will read research paper [7] in detail, in which Ozdemir et al. discussed  $(h-m)$ -convex function, derived some Hermite-Hadamard inequalities

## References

- [1] S. S. Dragmoir, C. E. M. Pearce, Selected topics on Hermite-Hadamard inequalities and applications, RGMIA Monographs, Victoria University, 2000. Math. Sic. Marh. Roum., 47(2004),3-14.
- [2] M. Alomari, M. Darus, *On the Hadamard's inequality for log convex functions on ccoordinated*, J. Inequal. Appl.2009(2009)13. Article ID 283147.
- [3] A. G. Azpeitia, *Convex functions and the Hadamard inequality*, Revista Colombina Mat. 28(1994)7-12.

## Tentative Schedule

| Tasks                             | July to Sep 2017 | Oct to Dec 2017 | Jan to Mar 2018 | Apr to Jun 2018 | July to Sep 2018 | Oct to Dec 2018 |
|-----------------------------------|------------------|-----------------|-----------------|-----------------|------------------|-----------------|
| Literature review                 | ✓                |                 |                 |                 |                  |                 |
| Problem formulation               |                  | ✓               |                 |                 |                  |                 |
| Solving problem                   |                  |                 | ✓               |                 |                  |                 |
| Paper submission                  |                  |                 |                 | ✓               |                  |                 |
| Extensions of problem             |                  |                 |                 |                 | ✓                |                 |
| Write up and submission of thesis |                  |                 |                 |                 |                  | ✓               |

## Details of Completed Coursework

(or attach provisional transcript)

| Sr. | Course Code and Title                   | Credit Hours | Grade Points | Semester    |
|-----|---|--------------|--------------|-------------|
| 1.  | MTH525: Advanced Convex Analysis        | 3            | 2.9          | Fall 2023   |
| 2.  | MTH623: Long Long Course Title and Good | 3            | 3.1          | Spring 2023 |
| 3.  |   |              |              |             |
| 4.  |   |              |              |             |
| 5.  |   |              |              |             |
| 6.  |   |              |              |             |
| 7.  |   |              |              |             |
| 8.  |   |              |              |             |