



# COMSATS University Islamabad

Synopsis for MS ☒ Ph.D. ☐

Name: Muhammad Latif Khan Wali	Registration No.: CIIT/FA14-RMT-001/ATK
Program: RMT	Area of Specialization (if any as per approved SoS):
Department: Mathematics	Campus: Attock
Date of admission: 13-04-2023	Date of synopsis submission: 23-09-2023
Proposed Title of the Thesis: (Use title case capitalization): The Gamma Function $\Gamma$ and Their Properties with Applications.	
<b>Supervisory Committee</b>	
Name and Designation	Role
Dr. Super Visor (Tenured Associate Professor)	Supervisor
Dr. Co Super Visor (Assistant Professor)	Cosupervisor/Member
Dr. Pervais Shah (Lecturer)	Member
Dr. 2nd Sahadfad (Tenured Professor)	Member

Student's Signature: \_\_\_\_\_

**Summary of the Research** Assume that  $\alpha$  is monotonically increasing on  $[a, \infty)$  and  $f \in \mathcal{R}(\alpha; a, b)$  for every  $b \geq a$ . If  $0 \leq f_1(x) \leq f_2(x)$  for every  $x \geq a$  and  $\int_a^\infty f_2 d\alpha$  converges, then prove that  $\int_a^\infty f_1 d\alpha$  converges and we have  $\int_a^\infty f_1 d\alpha \leq \int_a^\infty f_2 d\alpha$ . Let  $\{f_n\}$  be a sequence of functions defined on an interval  $I$ , and  $x_0 \in I$ . If the sequence  $\{f_n\}$  converges uniformly to some function  $f$  on  $I$  and if each of the function  $f_n$  is continuous at  $x_0$ , then prove that the function  $f$  is also continuous at  $x_0$ .

## 1. Introduction

This section includes introduction starting from major domain and narrowing, down to specific domain. It should highlight motivation and includes introduction starting includes introduction starting.

## 2. Literature Review

Our aim is to derived Hadamard type inequality for  $h$  convex function on coordinates. We will introduce  $(h - m)$ -convex function on coordinates in rectangle in a plane and will derive the Hadamard type inequality connected to it.

Our aim is also to consider non-negative difference of these Hadamard type inequalities as a functional to discuss its various properties for different classes of  $\hat{h}$ -convex and  $(h - m)$ -convex function on coordinates.

Our aim is also to consider non-negative difference of these Hadamard type inequalities as a functional to discuss its various properties for different classes of  $h$ -convex and  $(h - m)$ -convex function on coordinates.

## 3. Problem Statement

After having a basic knowledge about the convex functions. I will read research paper [7] in detail, in which Ozdemir et al. discussed  $(h-m)$ -convex function, derived some Hermite-Hadamard inequalities for  $(h - m)$ -convex functions and proved some of their properties. And also I will read research paper [6], in which Sarikaya et. al. established a new Hadamard type inequality for  $h$ -convex functions. Moreover, I will

## 4. Research Objectives

After having a basic knowledge about the convex functions. I will read research paper [7] in detail, in which Ozdemir et al. discussed  $(h-m)$ -convex function, derived some Hermite-Hadamard inequalities for  $(h - m)$ -convex functions and proved some of their properties. And also I will read research paper [6], in which Sarikaya et. al. established a new Hadamard type inequality for  $h$ -convex functions. Moreover, I will

## 5. Research Methodology (or Material and Methods)

After having a basic knowledge about the convex functions. I will read research paper [7] in detail, in which Ozdemir et al. discussed  $(h-m)$ -convex function, derived some Hermite-Hadamard inequalities

## References

- [1] S. S. Dragmoir, C. E. M. Pearce, Selected topics on Hermite-Hadamard inequalities and applications, RGMIA Monographs, Victoria University, 2000. Math. Sic. Marh. Roum., 47(2004),3-14.
- [2] M. Alomari, M. Darus, *On the Hadamard's inequality for log convex functions on ccoordinated*, J. Inequal. Appl.2009(2009)13. Article ID 283147.
- [3] A. G. Azpeitia, *Convex functions and the Hadamard inequality*, Revista Colombina Mat. 28(1994)7-12.

## Tentative Schedule

Tasks	July to Sep 2017	Oct to Dec 2017	Jan to Mar 2018	Apr to Jun 2018	July to Sep 2018	Oct to Dec 2018
Literature review	✓					
Problem formulation		✓				
Solving problem			✓			
Paper submission				✓		
Extensions of problem					✓	
Write up and submission of thesis						✓

## Details of Completed Coursework

(or attach provisional transcript)

Sr.	Course Code and Title	Credit Hours	Grade Points	Semester
1.	MTH525: Advanced Convex Analysis	3	2.9	Fall 2023
2.	MTH623: Long Long Course Title and Good	3	3.1	Spring 2023
3.				
4.				
5.				
6.				
7.				
8.				