

COMSATS University Islamabad

Attock Campus

Department of Mathematics

Assignment # 04

Class: BSM-V **Due Date:** 22-12-2022 (3:00PM)

Subject: Real Analysis I Course Code: MTH321

Instructor: Dr. Atiq ur Rehman **Marks:** 10

Note: *Please follow the due date & time strictly.*

Student must submit the hard copy of the assignment during office time.

Q 1: For what values of x, the following series is convergent (use ratio test).

$$\frac{2^2}{3^2} + \frac{2^2 \cdot 4^2}{3^2 \cdot 5^2} x + \frac{2^2 \cdot 4^2 \cdot 6^2}{3^2 \cdot 5^2 \cdot 7^2} x^2 + \dots$$

Q 2: Consider the function $f: \mathbb{R} \to \mathbb{R}$ defined as

$$f(x) = \begin{cases} 0 & \text{if } x \text{ is rational} \\ 1 & \text{if } x \text{ is irratioanl} \end{cases}$$

Prove that $\lim_{x\to 0} f(x)$ does not exist.

Academic Honesty Requirements:

You are encouraged to work with others in the completion of assignments, but it doesn't include copying. However, in the spirit of Academic Honesty, which includes crediting others for their contribution to your work, please include one of the following statements with every submitted assignment on title page:

- 1. I worked alone on this assignment.
- 2. I worked with the following: List their full names. Include their relationship to you if they are not also a member of this class.