

d) $\frac{p}{2}$

- x) If $y = 0$ then the point $P(x, y)$ is on
 a) Origin
 b) y-axis
 c) x-axis
 d) 4th quadrant
- xi) IF $(2, 4), (4, 6)$ & $(3, 5)$ are the vertices of a triangle then its centroid is
 a) $\left(\frac{10}{4}, \frac{14}{3}\right)$
 b) $(3, 5)$
 c) $\left(\frac{8}{3}, \frac{11}{3}\right)$
 d) $(3, 4)$
- xii) If $b = 0$ then $ax + by + c = 0$ shows that line is
 a) Parallel to x-axis
 b) Parallel to y-axis
 c) Perpendicular to y-axis
 d) None of these
- xiii) The lines represented by $ax^2 + 2hxy + by^2 = 0$
 a) $h^2 - ab < 0$
 b) $h^2 - ab > 0$
 c) $h^2 - ab = 0$
 d) $h^2 + ab = 0$
- xiv) To find the optional solution evaluate the objective function at
 a) All points of feasible region
 b) Corner points
 c) Origin only
 d) None of these
- xv) If $C(h, k)$ is the centre and r is the radius of a circle then equation of the circle is
 a) $(x + h)^2 + (y + k)^2 = r^2$
 b) $(x - h)^2 + (y - k)^2 = r^2$
 c) $(x - h) + (y - k) = r$
 d) $(x + h) + (y + k) = r$
- xvi) The directrix of the parabola $y^2 = 8x$ is
 a) $x + 2 = 0$
 b) $x - 2 = 0$
 c) $y + 2 = 0$
 d) $y - 2 = 0$
- xvii) If equation of ellipse is $\frac{x^2}{a} + \frac{y^2}{b} = 1$
 a) $(0, 0)$
 b) (a, b)
 c) (b, a)
 d) $(-a, -b)$
- xviii) If the equation of hyperbola is $\frac{x^2}{a} - \frac{y^2}{b} = 1$ then vertices are
 a) $(+a, 0)$
 b) $(+b, 0)$
 c) $(0, \pm b)$
 d) $(0, \pm a)$
- xix) If the angle α, β, γ are direction angles of a vector then $\text{Cos}\alpha, \text{Cos}\beta, \text{Cos}\gamma$ are called
 a) Components
 b) Direction cosines
 c) Both (a) & (b)
 d) None of these
- xx) If \underline{a} & \underline{b} are two non-zero vectors then $\underline{a} \times \underline{b} =$
 a) \underline{ab}
 b) ab
 c) $-\underline{b} \times \underline{a}$
 d) None of these

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Section – I*Note: All questions are to be attempted on answer book.***Q # 1: Write any TWENTY-FIVE short answers of the following questions:**

- (i) Evaluate $\lim_{x \rightarrow 0} \frac{\sqrt{x+a} - \sqrt{a}}{x}$
- (ii) If $f(x) = -2x + 8$, find $f^{-1}(x)$
- (iii) If $f(x) = \frac{x-1}{x-4}$, $x \neq 4$, then find domain of $f^{-1}(x)$
- (iv) What is differentiation?
- (v) Find $\frac{dy}{dx}$ if $y = \text{Cos } h(2x)$
- (vi) What is the geometrical interpretation of a derivative?
- (vii) Find the extreme values of $f(x) = x^2 - x - 2$
- (viii) Find $\frac{dy}{dx}$ if $y = \text{Sin}^{-1}\left(\frac{x}{a}\right)$
- (ix) What is integration?
- (x) Evaluate $\int \frac{x^2 - 1}{x^2 + 1} .dx$
- (xi) Evaluate $\int \ln x .dx$
- (xii) Evaluate $\int \text{Tan}^2 x .dx$
- (xiii) Evaluate $\int \text{Sec}^4 x .dx$
- (xiv) Evaluate $\int \frac{1}{e^x + e^{-x}} dx$
- (xv) Evaluate $\int \frac{dx}{\sqrt{x+a} + \sqrt{x}}$
- (xvi) Solve the differential equation $x.dy + y.dx = 0$
- (xvii) Evaluate $\int_{-1}^5 |x-3|.dx$
- (xviii) Find the area bounded by Cosine function from $x = -\frac{P}{2}$ to $x = \frac{P}{2}$
- (xix) Define inclination and slope of a line.
- (xx) Find h such that points $A(-1, h)$, $B(3, 2)$ and $C(7, 3)$ are collinear.
- (xxi) Find the measure of the angle between the lines represented by $x^2 - xy - 6y^2 = 0$
- (xxii) Find the distance of the point $(6, -1)$ from the line $6x - 4y + 9 = 0$.
- (xxiii) What is an objective function?
- (xxiv) What is an inequality?
- (xxv) What is a feasible region?
- (xxvi) Find the slope of the tangent to parabola $y^2 = 4ax$ at the point $(at^2, 2at)$
- (xxvii) Find the Centre and foci of the ellipse $\frac{x^2}{9} + \frac{y^2}{16} = 1$
- (xxviii) Check the position of the point $(5, 6)$ w. r. t. the circle $2x^2 + 2y^2 + 12x - 8y + 1 = 0$
- (xxix) What are the characteristics of the general equation of a circle?
- (xxx) Find the equ. of hyperbola if foci are $(\pm 5, 0)$ and vertex is $(3, 0)$.
- (xxxi) Transform the equation $x^2 + 6x - 8y + 17 = 0$ referred to $O'(-3, 0)$ as origin, axes remaining parallel to the old axes.
- (xxxii) Prove that the length of latus rectum of the ellipse $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ is $\frac{2b^2}{a}$
- (xxxiii) What is a position vector?

(xxxiv)	If the vectors $2\mathbf{i} + 4\mathbf{j} - 7\mathbf{k}$ and $2\mathbf{i} + 6\mathbf{j} + x\mathbf{k}$ are perpendicular to each other, find the value of x.
(xxxv)	If $\mathbf{a} + \mathbf{b} + \mathbf{c} = \mathbf{0}$, prove that $\mathbf{a} \times \mathbf{b} = \mathbf{b} \times \mathbf{c} = \mathbf{c} \times \mathbf{a}$
(xxxvi)	Find the values of α so that $\mathbf{u} = \alpha\mathbf{i} + \mathbf{j}$, $\mathbf{v} = \mathbf{i} + \mathbf{j} + 3\mathbf{k}$ and $\mathbf{w} = 2\mathbf{i} + \mathbf{j} - \mathbf{k}$ are coplanar.
(xxxvii)	Find the direction cosines of the vector $\mathbf{v} = 2\mathbf{i} - \mathbf{j} + 2\mathbf{k}$

Section - II	
<i>Note: Attempt any THREE questions.</i>	
Q # 2 (a)	If θ is measured in radians, prove that $\lim_{x \rightarrow 0} \frac{\sin x}{x} = 1$
(b)	Show that $x^2 \frac{dy^2}{dx^2} + x \frac{dy}{dx} + y = 0$. If $y = a \cos(\ln x) + b \sin(\ln x)$
Q # 3 (a)	Evaluate $\int \sqrt{a^2 + x^2} dx$
(b)	Find the area bounded by the curve $y = x^3 - 4x$ and the x -axis.
Q # 4 (a)	Find the equation of a st. line through the intersection of the lines $x - y - 4 = 0$ and $7x + y + 20 = 0$ and perpendicular to the line $6x + y - 14 = 0$
(b)	Find the maximum and minimum values of $f(x, y) = 4x + 5y$ under the constraints <div> $2x - 3y \leq 6$, $2x + y \geq 2$ and $2x + 3y \leq 12, \quad x \geq 0, \quad y \geq 0$. </div>
Q # 5 (a)	Define parabola and derive the equation of parabola in standard form.
(b)	Analyze the equation. $4x^2 + 9y^2 = 36$
Q # 6 (a)	Show that the line segment joining the mid. Pts. of the sides of a quadrilateral taken in order from a parallelogram.
(b)	Find the volume of the tetrahedron with vertices $A(0,1,2)$, $B(3,2,1)$, $C(1,2,1)$ & $D(5,5,6)$.

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