Exercise 7.5 (Solutions) mathcity.org TEXTBOOK OF ALGEBRA AND TRIGONOMETRY FOR CLASS XI

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Merging man and maths

Question # 1

Total possible outcomes = n(S) = 1

Suppose *A* is the event that sweet is orange flavoured. (i) Since box only contained orange flavoured sweets So favourable outcomes = n(A) = 1

Probability =
$$P(A) = \frac{n(A)}{n(S)} = \frac{1}{1} = 1$$

(ii) Let B be the event that the sweet is lemon-flavoured. Since box only contained orange-flavoured sweet So favourable outcomes = n(B) = 0

Probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{0}{1} = 0$$

Question #2

Since there are three possibilities that Pakistan wins, loses or the match tied. Therefore possible outcomes = n(S) = 3

(i) Let A be the event that Pakistan wins Favourable outcomes = n(A) = 1

Required probability = $P(A) = \frac{n(A)}{n(S)} = \frac{1}{3}$

(ii) Let *B* be the event that India does not lose. If India does not lose then India may win or the match tied Therefore favourable outcomes = n(B) = 2

Required probability = $P(B) = \frac{n(B)}{n(S)} = \frac{2}{3}$

Question #3

Total number of balls = 5 + 3 = 8Therefore possible outcomes = n(S) = 8Let *A* be event that the ball is green (i) Then favourable outcomes = n(A) = 5So probability = $P(A) = \frac{n(A)}{n(S)} = \frac{5}{8}$ *(ii)* Let *B* be the event that the ball is red

Then favourable outcomes = n(B) = 3

So probability = $P(A) = \frac{n(B)}{n(S)} = \frac{3}{8}$

Question #4

When a fair coin is tossed three times, the possible outcomes are HHH, HHT, HTH, THH, HTT, THT, TTH, TTT.

So total possible outcomes = n(S) = 8

(i) Let A be the event that the coin shows one tail then favourable outcomes are HHT, HTH, THH,

i.e.
$$n(A) = 3$$

So required probability = $P(A) = \frac{n(A)}{n(S)} = \frac{3}{8}$

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(*ii*) Let *B* be the event that coin shows at least one head then favourable outcomes are HHH, HHT, HTH, THH, HTT, THT, TTH.

i.e.
$$n(B) = 7$$

So required probability = $P(B) = \frac{n(B)}{n(S)} = \frac{7}{8}$

Queston # 5

The possible outcomes are that die show 1, 2, 3, 4, 5, 6. So possible outcomes = n(S) = 6

(i) Let A be the event that die show 3 or 4. Then favourable outcomes = n(A) = 2

So required probability = $P(A) = \frac{n(A)}{n(S)} = \frac{2}{6} = \frac{1}{3}$

(ii) Let *B* be the event that top of the die show dots less than 5 then Favourable outcomes = n(B) = 4

So required probability = $P(B) = \frac{n(B)}{n(S)} = \frac{4}{6} = \frac{2}{3}$

Question # 6

Since the box contain 5 slips So possible outcomes = n(S) = 5

(i) Let A be the event that the number on the slip are prime numbers 2, 3 or 5 Then favourable outcomes = n(A) = 3

So required probability = $P(A) = \frac{n(A)}{n(S)} = \frac{3}{5}$

(ii) Let *B* be the event that number on the slips are multiple of 3 then Favourable outcomes = n(B) = 1

So probability = $P(B) = \frac{n(B)}{n(S)} = \frac{1}{5}$

Question # 7

When two dice are rolled, the possible outcomes are

(1, 1)	(1, 2)	(1, 3)	(1, 4)	(1, 5)	(1, 6)
(2, 1)	(2, 2)	(2, 3)	(2, 4)	(2, 5)	(2, 6)
(3, 1)	(3, 2)	(3, 3)	(3, 4)	(3, 5)	(3, 6)
(4, 1)	(4, 2)	(4, 3)	(4, 4)	(4, 5)	(4, 6)
(5, 1)	(5, 2)	(5, 3)	(5, 4)	(5, 5)	(5, 6)
(6, 1)	(6, 2)	(6, 3)	(6, 4)	(6, 5)	(6, 6)

This show possible outcomes = n(S) = 36

(i) Let A be the event that the total of two scores is 5 then favourable outcome are (1, 4), (2, 3), (3, 2), (4, 1)

i.e. favourable outcomes = n(A) = 4

So required probability = $P(A) = \frac{n(A)}{n(S)} = \frac{4}{36} = \frac{1}{9}$

(ii) Let B be the event that the total of two scores is 7 then favourable outcomes are (1, 6), (2, 5), (3, 4), (4, 3), (5, 2), (6, 1)

i.e. favourable outcomes = n(B) = 6

So probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{6}{36} = \frac{1}{6}$$

(iii) Let C be the event that the total of two score is 11 then favourable outcomes are (5, 6), (6, 5) i.e. n(C) = 2

So probability = $P(B) = \frac{n(B)}{n(S)} = \frac{2}{36} = \frac{1}{18}$

Question # 8

	Total number of balls = 40 i.e. $n(S) = 40$					
	Black balls = 15, Green balls = 5, Yellow balls = $40 - (15+5) = 20$					
(i)	Let <i>A</i> be the event that the ball is black then $n(A) = 15$					
	So required probability = $P(A) = \frac{n(A)}{n(S)} = \frac{15}{40} = \frac{3}{8}$					
(<i>ii</i>)	Let <i>B</i> denotes the event that the ball is green then $n(B) = 5$					
	So required probability = $P(B) = \frac{n(B)}{n(S)} = \frac{5}{40} = \frac{1}{8}$					
	Let <i>C</i> denotes the event that the ball is not green then ball is either black of yellow therefore favourable outcomes = $n(C) = 15 + 20 = 35$					
	So required probability = $P(C) = \frac{n(C)}{n(S)} = \frac{35}{40} = \frac{7}{8}$					
Oue	stion # 9					

Number of students = 30

Then possible outcomes = n(S) = 30

Now if *A* be the event that the monitor is the boy then *(i)* Favourable outcomes = n(A) = 18

So probability = $P(A) = \frac{n(A)}{n(S)} = \frac{18}{30} = \frac{3}{5}$

(ii) Now if *B* be the event that the monitor is the girl then Favourable outcomes = n(B) = 12

So probability =
$$P(B) = \frac{n(B)}{n(S)} = \frac{12}{30} = \frac{2}{5}$$

Question # 10

When the coin is tossed four times the possible outcomes are

			1	
Η	HHT	HHTH	HTHH	THHH
Η	HTT	HTTH	TTHH	THHT
Η	TTT	TTTH	TTHT	THTT
T	ГТТ	HHHH	THTH	HTHT
i.e. $n(S)$)=16			

(i) Let *A* be the event that the top shows all head then favourable outcome is HHHH i.e. n(A) = 1

Now probability =
$$P(A) = \frac{n(A)}{n(S)} = \frac{1}{16}$$

Let *B* be the event that the top shows 2 head and two tails the favourable *(ii)* outcomes are HHTT, HTTH, TTHH, THHT, THTH, HTHT i.e. n(B) = 6

Now probability = $P(B) = \frac{n(B)}{n(S)} = \frac{6}{16} = \frac{3}{8}$

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