

Ø Question # 1

The sequence of deposit is 8, 24, 72,

$$\text{Here } a_1 = 8 \quad r = \frac{24}{8} = \frac{72}{24} = 3, \quad n = 5$$

$$\text{Since } S_n = \frac{a_1(r^n - 1)}{r - 1} \quad \Rightarrow \quad S_5 = \frac{8(3^5 - 1)}{3 - 1} = \frac{8(243 - 1)}{2} = 4(242) = 968$$

Thus he has to deposited Rs. 968 up to the fifth year.

Ø Question # 2

Here $a_1 = 8$, $r = 2$, $S_n = 32760$, $n = ?$, $a_n = ?$

$$\text{Since } S_n = \frac{a_1(r^n - 1)}{r - 1}$$

$$\Rightarrow 32760 = \frac{8(2^n - 1)}{2 - 1} \quad \Rightarrow 32760 = \frac{8(2^n - 1)}{1} \quad \Rightarrow 32760 = 8(2^n - 1)$$

$$\Rightarrow 4095 = (2^n - 1) \quad \Rightarrow 4095 + 1 = 2^n \quad \Rightarrow 4096 = 2^n$$

$$\Rightarrow (2)^{12} = 2^n \quad \Rightarrow 12 = n$$

$$\text{Now } a_{12} = a_1 r^{11} \quad \Rightarrow a_{12} = (8)(2)^{11} = (8)(2048) = 16384$$

Hence the last instalment is Rs. 16384.

Ø Question # 3

$$\text{Here } a_1 = 62500, \quad n = 4, \quad r = 1 + \frac{4}{100} = 1 + 0.04 = 1.04$$

$$\text{Since } a_n = a_1 r^{n-1} \quad \Rightarrow \quad a_4 = (62500)(1.04)^{4-1} = (62500)(1.04)^3 \\ = (62500)(1.1249) = 70304$$

Thus the population after 3 years is 70304.

Ø Question # 4

Let the enrolment in 1970 is a_1

also $a_n = 6000$, $r = 2$, $n = 4$

$$\text{Since } a_n = a_1 r^{n-1}$$

$$\Rightarrow 6000 = a_1(2)^{4-1} \quad \Rightarrow 6000 = a_1(2)^3 \quad \Rightarrow 6000 = a_1(8)$$

$$\Rightarrow \frac{6000}{8} = a_1 \quad \Rightarrow a_1 = 750$$

Thus the enrolment was 750.

**Ø Question # 5**

The colony of bacteria in the start = $a_1 = A$

Then $r = 2$, $n = 2n + 1$

$$\text{Since } a_n = a_1 r^{n-1} \quad \Rightarrow \quad a_{2n+1} = (A)(2)^{2n+1-1} = A(2)^{2n}$$

Thus bacteria after n hours will be $A(2)^n$.

Ø Question # 6

$$\text{Here } a_1 = \frac{3}{2}, \quad r = \frac{1}{2}$$

$$\text{So the series is } \frac{3}{2} + \frac{3}{4} + \frac{3}{8} + \dots$$

Which is infinite geometric series

$$\text{Now } S = \frac{a_1}{1 - r} = \frac{\frac{3}{2}}{1 - \frac{1}{2}} = \frac{\frac{3}{2}}{\frac{1}{2}} = 3 \quad \text{Answer}$$