

Chapter 17

Practical Geometry

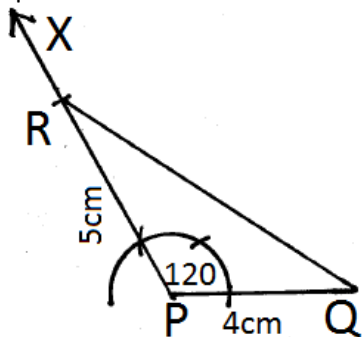
Case-1: length of two sides and measure of the included angles are given

Example 1: Construct a triangle PQR given that

$\overline{PQ} = 4\text{cm}$, $\overline{PR} = 5\text{cm}$ and $m\angle P = 120^\circ$

Sol: Given $\overline{PQ} = 4\text{cm}$, $\overline{PR} = 5\text{cm}$ & $m\angle P = 120^\circ$

Required: Construct a ΔPQR



Steps of construction:

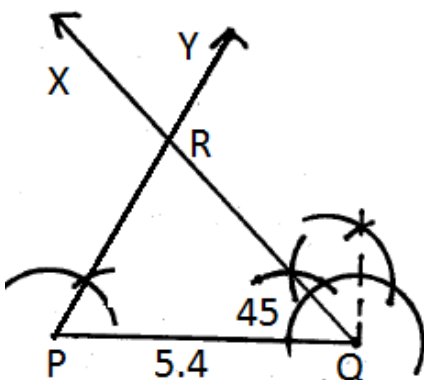
- i). Draw a line segment $\overline{PQ} = 4\text{cm}$
- ii). At point P draw an angle $m\angle QPX = 120^\circ$
- iii). At P draw an arc of radius 5cm which cuts the ray \overline{PX} at R.
- iv). Join Q to R
- v). ΔPQR is required triangle

Case-2: Measure of two angle and included side are given

Example 2: Construct a triangle PQR given that $\overline{PQ} = 5.4\text{cm}$, $m\angle PQR = 45^\circ$ & $m\angle RPQ = 60^\circ$

Sol: Given $\overline{PQ} = 5.4\text{cm}$, $m\angle PQR = 45^\circ$ & $m\angle RPQ = 60^\circ$

Required: Construct a ΔPQR



Steps of construction:

- i). Draw a line segment $\overline{PQ} = 5.4\text{cm}$
- ii). At point P draw an angle $m\angle QPY = 60^\circ$
- iii). At point Q draw an angle $m\angle PQX = 45^\circ$ which intersect the ray \overline{PY} at R.
- iv). ΔPQR is required triangle

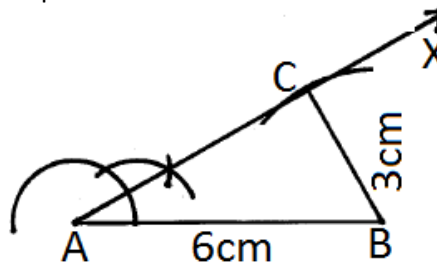
Case 3: Length of two sides & non-adjacent angle

Example 3: Construct a triangle ABC given that $\overline{BC} = 3\text{cm}$, $\overline{AB} = 6\text{cm}$ & $m\angle A = 30^\circ$

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Sol: Given $\overline{BC} = 3\text{cm}$, $\overline{AB} = 6\text{cm}$ & $m\angle A = 30^\circ$

Required: Construct a ΔABC



Steps of construction:

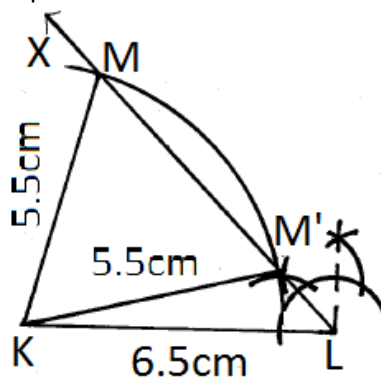
- i). Draw a line segment $\overline{AB} = 6\text{cm}$
- ii). At point A draw an angle $m\angle BAX = 30^\circ$
- iii). At point B draw an arc of radius 3cm which cut the ray \overline{AX} at C.
- iv). Join C to B
- v). ΔABC is required triangle

Example 4: Construct a triangle KLM given that

$\overline{KL} = 6.5\text{cm}$, $\overline{KM} = 5.5\text{cm}$ & $m\angle L = 45^\circ$

Sol: Given $\overline{KL} = 6.5\text{cm}$, $\overline{KM} = 5.5\text{cm}$ & $m\angle L = 45^\circ$

Required: Construct a ΔKLM



Steps of construction:

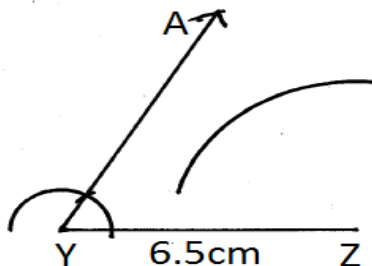
- i). Draw a line segment $\overline{KL} = 6.5\text{cm}$
- ii). At point L draw an angle $m\angle KLX = 45^\circ$
- iii). At point K draw an arc of radius 5.5cm which intersect the ray \overline{LX} at M & M'
- iv). Join K to M & M'
- v). ΔKLM & $\Delta KLM'$ are the required triangles

Example 5: Construct a triangle XYZ given that

$\overline{YZ} = 6.5\text{cm}$, $\overline{ZX} = 4\text{cm}$ & $m\angle Y = 60^\circ$

Sol: Given $\overline{YZ} = 6.5\text{cm}$, $\overline{ZX} = 4\text{cm}$ & $m\angle Y = 60^\circ$

Required: Construct a ΔXYZ



Steps of construction:

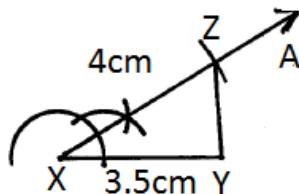
- i). Draw a line segment $\overline{YZ} = 6.5\text{cm}$
- ii). At point Y draw an angle $m\angle ZYA = 60^\circ$
- iii). At point Z draw an arc of radius 4cm which does not intersect the ray \overline{YA}
- iv). Therefore no triangle constructed to satisfy the given data

Exercise 17.1

Q1: i). Construct a $\triangle XYZ$, when $m\angle X = 30^\circ$
 $\overline{XY} = 3.5\text{cm}$, & $\overline{XZ} = 4\text{cm}$

Sol: Given $m\angle X = 30^\circ$ $\overline{XY} = 3.5\text{cm}$, & $\overline{XZ} = 4\text{cm}$

Required: Construct a $\triangle XYZ$



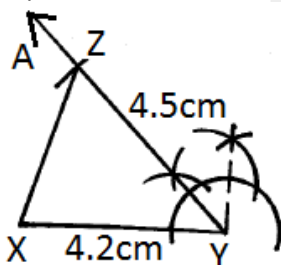
Steps of construction:

- i). Draw a line segment $\overline{XY} = 3.5\text{cm}$
- ii). At point X draw an angle $m\angle YXA = 30^\circ$
- iii). At X draw an arc of radius 4cm which cuts the ray \overline{XA} at Z.
- iv). Join Y to Z
- v). $\triangle XYZ$ is required triangle

Q1: ii). Construct a $\triangle XYZ$, when $m\angle Y = 45^\circ$
 $\overline{XY} = 4.2\text{cm}$, & $\overline{YZ} = 4.5\text{cm}$

Sol: Given $m\angle Y = 45^\circ$ $\overline{XY} = 4.2\text{cm}$, & $\overline{YZ} = 4.5\text{cm}$

Required: Construct a $\triangle XYZ$



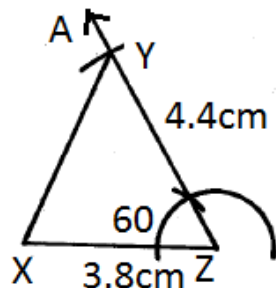
Steps of construction:

- i). Draw a line segment $\overline{XY} = 4.2\text{cm}$
- ii). At point Y draw an angle $m\angle XYA = 45^\circ$
- iii). At Y draw an arc of radius 4.5cm which cuts the ray \overline{YA} at Z.
- iv). Join X to Z
- v). $\triangle XYZ$ is required triangle

Q1: iii). Construct a $\triangle XYZ$, when $m\angle Z = 60^\circ$
 $\overline{XZ} = 3.8\text{cm}$, & $\overline{YZ} = 4.4\text{cm}$

Sol: Given $m\angle Z = 60^\circ$ $\overline{XZ} = 3.8\text{cm}$, & $\overline{YZ} = 4.4\text{cm}$

Required: Construct a $\triangle XYZ$



Steps of construction:

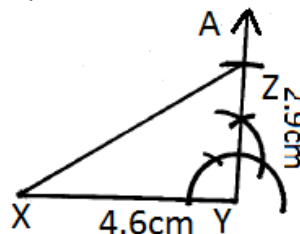
- i). Draw a line segment $\overline{XZ} = 3.8\text{cm}$
- ii). At point Z draw an angle $m\angle XZA = 60^\circ$
- iii). At Z draw an arc of radius 4.4cm which cuts the ray \overline{ZA} at Y.
- iv). Join X to Y

v). $\triangle XYZ$ is required triangle

Q1: iv). Construct a $\triangle XYZ$, when $m\angle Y = 90^\circ$
 $\overline{XY} = 4.6\text{cm}$, & $\overline{YZ} = 2.9\text{cm}$

Sol: Given $m\angle Y = 90^\circ$ $\overline{XY} = 4.6\text{cm}$, & $\overline{YZ} = 2.9\text{cm}$

Required: Construct a $\triangle XYZ$



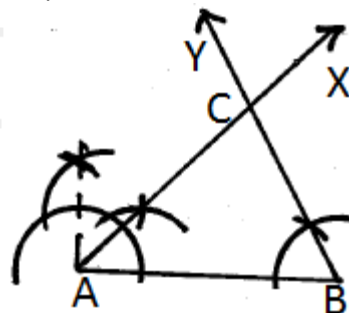
Steps of construction:

- i). Draw a line segment $\overline{XY} = 4.6\text{cm}$
- ii). At point Y draw an angle $m\angle XYA = 90^\circ$
- iii). At Y draw an arc of radius 2.9cm which cuts the ray \overline{YA} at Z.
- iv). Join X to Z
- v). $\triangle XYZ$ is required triangle

Q2: i). Construct a $\triangle ABC$, when $\overline{AB} = 4.5\text{cm}$,
 $m\angle A = 45^\circ$ & $m\angle B = 60^\circ$

Sol: Given $\overline{AB} = 4.5\text{cm}$, $m\angle A = 45^\circ$ & $m\angle B = 60^\circ$

Required: Construct a $\triangle ABC$



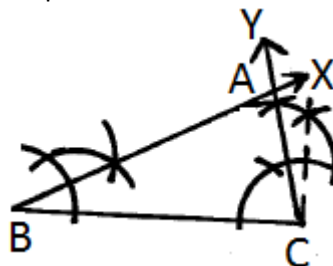
Steps of construction:

- i). Draw a line segment $\overline{AB} = 4.5\text{cm}$
- ii). At point A draw an angle $m\angle BAX = 45^\circ$
- iii). At point B draw an angle $m\angle ABY = 60^\circ$ which intersect the ray \overline{AX} at C.
- iv). $\triangle ABC$ is required triangle

Q2: ii). Construct a $\triangle ABC$, when $\overline{BC} = 5\text{cm}$,
 $m\angle B = 30^\circ$ & $m\angle C = 75^\circ$

Sol: Given $\overline{BC} = 5\text{cm}$, $m\angle B = 30^\circ$ & $m\angle C = 75^\circ$

Required: Construct a $\triangle ABC$



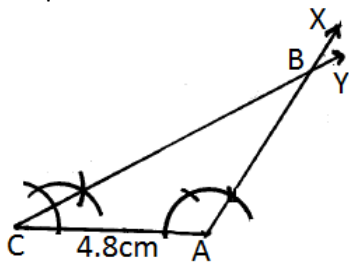
Steps of construction:

- i). Draw a line segment $\overline{BC} = 5\text{cm}$
- ii). At point B draw an angle $m\angle CBX = 30^\circ$
- iii). At point C draw an angle $m\angle BCY = 75^\circ$ which intersect the ray \overline{BX} at A.
- iv). $\triangle ABC$ is required triangle

Q2: iii). Construct a $\triangle ABC$, when $\overline{AC} = 4.8\text{cm}$, $m\angle A = 120^\circ$ & $m\angle C = 30^\circ$

Sol: Given $\overline{AC} = 4.8\text{cm}$, $m\angle A = 120^\circ$ & $m\angle C = 30^\circ$

Required: Construct a $\triangle ABC$



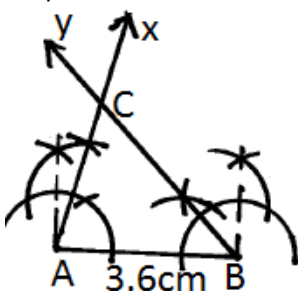
Steps of construction:

- i). Draw a line segment $\overline{AC} = 4.8\text{cm}$
- ii). At point A draw an angle $m\angle CAX = 120^\circ$
- iii). At point C draw an angle $m\angle ACY = 30^\circ$ which intersect the ray \overline{AX} at B.
- iv). $\triangle ABC$ is required triangle

Q2: iv). Construct a $\triangle ABC$, when $\overline{AB} = 3.6\text{cm}$, $m\angle A = 75^\circ$ & $m\angle B = 45^\circ$

Sol: Given $\overline{AB} = 3.6\text{cm}$, $m\angle A = 75^\circ$ & $m\angle B = 45^\circ$

Required: Construct a $\triangle ABC$



Steps of construction:

- i). Draw a line segment $\overline{AB} = 3.6\text{cm}$
- ii). At point A draw an angle $m\angle BAX = 75^\circ$
- iii). At point B draw an angle $m\angle ABY = 45^\circ$ which intersect the ray \overline{AX} at C.
- iv). $\triangle ABC$ is required triangle

Q3: i). Construct a $\triangle KLM$, when $\overline{KL} = 4.8\text{cm}$, $m\angle K = 45^\circ$ & $m\angle M = 60^\circ$

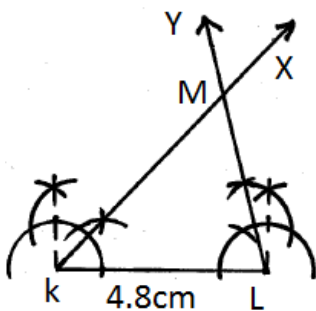
Sol: Given $\overline{KL} = 4.8\text{cm}$, $m\angle K = 45^\circ$ & $m\angle M = 60^\circ$

Required: Construct a $\triangle KLM$, First find

$$m\angle K + m\angle L + m\angle M = 180^\circ$$

$$45^\circ + m\angle L + 60^\circ = 180^\circ$$

$$m\angle L = 180^\circ - 60^\circ - 45^\circ = 75^\circ$$



Steps of construction:

- i). Draw a line segment $\overline{KL} = 4.8\text{cm}$
- ii). At point K draw an angle $m\angle LKX = 45^\circ$
- iii). At point L draw an angle $m\angle KLY = 75^\circ$

which intersect the ray \overline{KX} at M.

iv). $\triangle KLM$ is required triangle

Q3: ii). Construct a $\triangle KLM$, when $\overline{LM} = 3.8\text{cm}$, $m\angle K = 30^\circ$ & $m\angle M = 75^\circ$

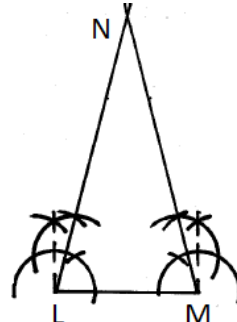
Sol: Given $\overline{LM} = 3.8\text{cm}$, $m\angle K = 30^\circ$ & $m\angle M = 75^\circ$

Required: Construct a $\triangle KLM$, First find

$$m\angle K + m\angle L + m\angle M = 180^\circ$$

$$30^\circ + m\angle L + 75^\circ = 180^\circ$$

$$m\angle L = 180^\circ - 30^\circ - 75^\circ = 75^\circ$$



Steps of construction:

- i). Draw a line segment $\overline{LM} = 3.8\text{cm}$
- ii). At point L draw an angle $m\angle L = 75^\circ$
- iii). At point M draw an angle $m\angle M = 75^\circ$ both angles intersect at K
- iv). $\triangle KLM$ is required triangle

Q3: iii). Construct a $\triangle KLM$, when $\overline{KM} = 5\text{cm}$, $m\angle K = 105^\circ$ & $m\angle L = 45^\circ$

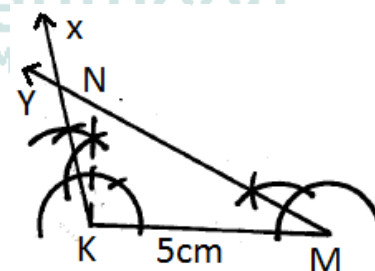
Sol: Given $\overline{KM} = 5\text{cm}$, $m\angle K = 105^\circ$ & $m\angle L = 45^\circ$

Required: Construct a $\triangle KLM$, First find

$$m\angle K + m\angle L + m\angle M = 180^\circ$$

$$105^\circ + 45^\circ + m\angle M = 180^\circ$$

$$m\angle M = 180^\circ - 105^\circ - 45^\circ = 30^\circ$$



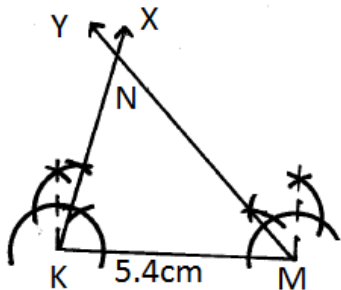
Steps of construction:

- i). Draw a line segment $\overline{KM} = 5\text{cm}$
- ii). At point K draw an angle $m\angle MKX = 105^\circ$
- iii). At point M draw an angle $m\angle KMY = 30^\circ$ which intersect the ray \overline{KX} at L.
- iv). $\triangle KLM$ is required triangle

Q3: iv). Construct a $\triangle KLM$, when $\overline{KM} = 5.4\text{cm}$, $m\angle K = 75^\circ$ & $m\angle M = 45^\circ$

Sol: Given $\overline{KM} = 5.4\text{cm}$, $m\angle K = 75^\circ$ & $m\angle M = 45^\circ$

Required: Construct a $\triangle KLM$

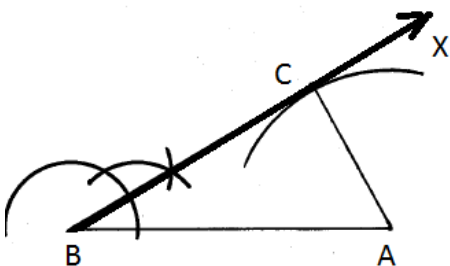


Steps of construction:

- i). Draw a line segment $\overline{KM} = 5.4\text{cm}$
- ii). At point K draw an angle $m\angle MKX = 75^\circ$
- iii). At point M draw an angle $m\angle KMY = 45^\circ$ which intersect the ray \overline{KX} at L.
- iv). $\triangle KLM$ is required triangle

Q4: i). Construct a $\triangle ABC$, when $\overline{AB} = 8\text{cm}$, $\overline{AC} = 4\text{cm}$ & $m\angle B = 30^\circ$

Sol: Given $\overline{AB} = 8\text{cm}$, $\overline{AC} = 4\text{cm}$, & $m\angle B = 30^\circ$
 Required: Construct a $\triangle ABC$

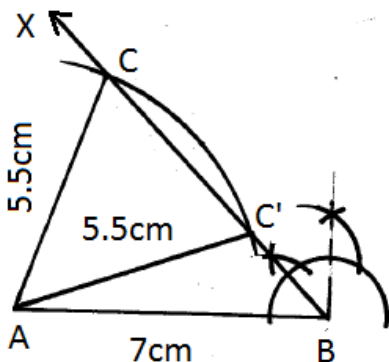


Steps of construction:

- i). Draw a line segment $\overline{AB} = 8\text{cm}$
- ii). At point B draw an angle $m\angle ABX = 30^\circ$
- iii). At point A Draw an arc of radius 4cm which intersect of ray \overline{BX} at C.
- iv). Join A to C.
- v). $\triangle ABC$ is required triangle

Q4: ii). Construct a $\triangle ABC$, when $\overline{AB} = 7\text{cm}$, $\overline{AC} = 5.5\text{cm}$ & $m\angle B = 45^\circ$

Sol: Given $\overline{AB} = 7\text{cm}$, $\overline{AC} = 5.5\text{cm}$, & $m\angle B = 45^\circ$
 Required: Construct a $\triangle ABC$

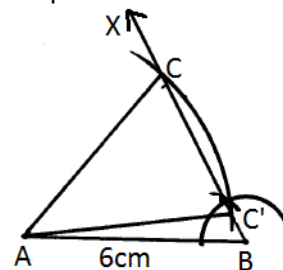


Steps of construction:

- i). Draw a line segment $\overline{AB} = 7\text{cm}$
- ii). At point B draw an angle $m\angle ABX = 45^\circ$
- iii). At point A Draw an arc of radius 5.5cm which intersect of ray \overline{BX} at C & C'.
- iv). Join A to C & C'.
- v). $\triangle ABC$ & $\triangle ABC'$ are required triangles

Q4: iii). Construct a $\triangle ABC$, when $\overline{AB} = 6\text{cm}$, $\overline{AC} = 5.6\text{cm}$ & $m\angle B = 60^\circ$

Sol: Given $\overline{AB} = 6\text{cm}$, $\overline{AC} = 5.6\text{cm}$, & $m\angle B = 60^\circ$
 Required: Construct a $\triangle ABC$

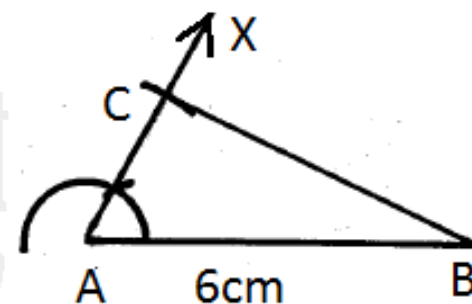


Steps of construction:

- i). Draw a line segment $\overline{AB} = 6\text{cm}$
- ii). At point B draw an angle $m\angle ABX = 60^\circ$
- iii). At point A Draw an arc of radius 5.6cm which intersect of ray \overline{BX} at C & C'.
- iv). Join A to C & C'.
- v). $\triangle ABC$ & $\triangle ABC'$ are required triangles

Q4: iv). Construct a $\triangle ABC$, when $\overline{AB} = 6\text{cm}$, $\overline{AC} = 2.5\text{cm}$ & $m\angle A = 60^\circ$

Sol: Given $\overline{AB} = 6\text{cm}$, $\overline{AC} = 2.5\text{cm}$ & $m\angle A = 60^\circ$
 Required: Construct a $\triangle ABC$

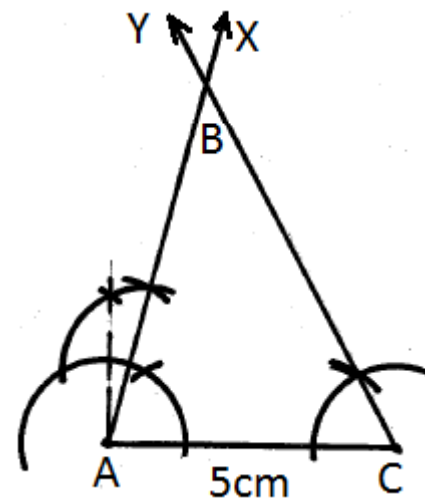


Steps of construction:

- i). Draw a line segment $\overline{AB} = 6\text{cm}$
- ii). At point A draw an angle $m\angle BAX = 60^\circ$
- iii). At point A Draw an arc of radius 2.5cm which intersect of ray \overline{AX} at C.
- iv). Join B to C.
- v). $\triangle ABC$ is required triangle

Q4: v). Construct a $\triangle ABC$, when $\overline{AC} = 5\text{cm}$, $m\angle A = 75^\circ$ & $m\angle C = 60^\circ$

Sol: Given $\overline{AC} = 5\text{cm}$, $m\angle A = 75^\circ$ & $m\angle C = 60^\circ$
 Required: Construct a $\triangle ABC$



Steps of construction:

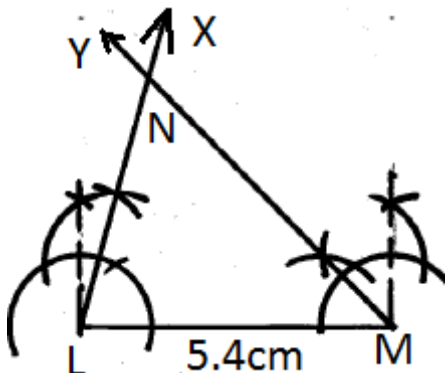
- i). Draw a line segment $\overline{AC} = 5\text{cm}$
- ii). At point A draw an angle $m\angle CAX = 75^\circ$

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- iii). At point A Draw an angle $m\angle ACY = 60^\circ$ which intersect of ray \overrightarrow{AX} at B.
 iv). $\triangle ABC$ is required triangle

Q5: Construct a $\triangle LMN$, when $\overline{LM} = 5.4\text{cm}$, $m\angle L = 75^\circ$ & $m\angle M = 45^\circ$

Sol: Given $\overline{LM} = 5.4\text{cm}$, $m\angle L = 75^\circ$, $m\angle M = 45^\circ$
 Required: Construct a $\triangle LMN$

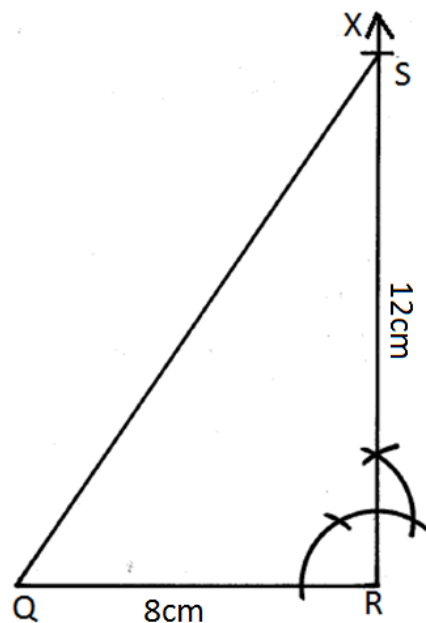


Steps of construction:

- i). Draw a line segment $\overline{LM} = 5.4\text{cm}$
- ii). At point L draw an angle $m\angle MLX = 75^\circ$
- iii). At point M Draw an angle $m\angle LMY = 45^\circ$ which intersect of ray \overrightarrow{LX} at N.
- iv). $\triangle LMN$ is required triangle

Q6: Construct a $\triangle QRS$, when $\overline{QR} = 8\text{cm}$, $\overline{RS} = 12\text{cm}$ & $m\angle R = 90^\circ$

Sol: Given $\overline{QR} = 8\text{cm}$, $\overline{RS} = 12\text{cm}$ & $m\angle R = 90^\circ$
 Required: Construct a $\triangle QRS$

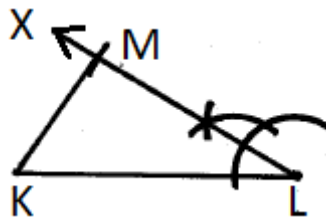


Steps of construction:

- i). Draw a line segment $\overline{QR} = 8\text{cm}$
- ii). At point R draw an angle $m\angle QRX = 90^\circ$
- iii). At point R draw an arc of radius 12cm which intersect of ray \overrightarrow{RX} at S.
- iv). $\triangle QRS$ is required triangle

Q7: Construct a $\triangle KLM$, when $\overline{KL} = 4.8\text{cm}$, $\overline{LM} = 3.9\text{cm}$ & $m\angle L = 30^\circ$

Sol: Given $\overline{KL} = 4.8\text{cm}$, $\overline{LM} = 3.9\text{cm}$ & $m\angle L = 30^\circ$
 Required: Construct a $\triangle KLM$



Steps of construction:

- i). Draw a line segment $\overline{KL} = 4.8\text{cm}$
- ii). At point L draw an angle $m\angle K LX = 30^\circ$
- iii). At point L draw an arc of radius 3.9cm which intersect of ray \overrightarrow{LX} at M.
- iv). $\triangle KLM$ is required triangle

Q8: Construct a $\triangle PQR$, when $\overline{QR} = 6.5\text{cm}$, $m\angle P = 30^\circ$ & $m\angle Q = 60^\circ$

Sol: Given $\overline{QR} = 6.5\text{cm}$, $m\angle P = 30^\circ$ & $m\angle Q = 60^\circ$

Required: Construct a $\triangle PQR$, First find $m\angle P + m\angle Q + m\angle R = 180^\circ$

$$30^\circ + 60^\circ + m\angle R = 180^\circ$$

$$m\angle R = 180^\circ - 60^\circ - 30^\circ = 90^\circ$$

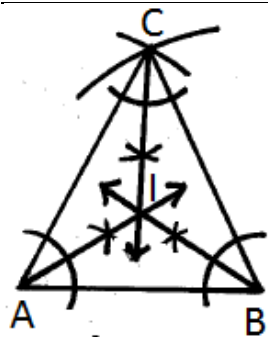


Steps of construction:

- i). Draw a line segment $\overline{QR} = 6.5\text{cm}$
- ii). At point R draw an angle $m\angle QRX = 90^\circ$
- iii). At point Q Draw an angle $m\angle RQY = 60^\circ$ which intersect of ray \overrightarrow{RX} at P.
- iv). $\triangle PQR$ is required triangle

Example 6: Construct $\triangle ABC$ whose $\overline{AB} = 4.6\text{cm}$, $\overline{BC} = 5\text{cm}$ and $\overline{CA} = 5.1\text{cm}$. Draw angle bisectors of the triangle & verify that these are concurrent.

Sol: Given $\overline{AB} = 4.6\text{cm}$, $\overline{BC} = 5\text{cm}$ & $\overline{CA} = 5.1\text{cm}$
 Required: Angle bisectors of a $\triangle ABC$ are concurrent.

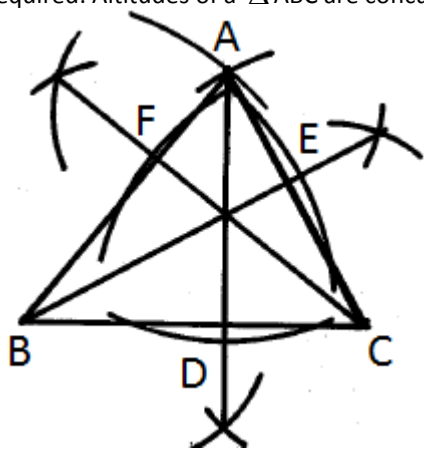


Steps of construction:

- i). Draw a line segment $\overline{AB} = 4.6$ cm
- ii). At point A draw an arc of radius 5.1cm
- iii). At point B Draw an arc of radius 5cm which intersect at C.
- iv). Join C to A & B. $\triangle ABC$ is constructed
- v). Draw bisectors of angles A,B & C. these bisectors passes through the same point I. thus angle bisectors of a triangle are concurrent.

Example 7: Construct $\triangle ABC$ whose $\overline{AB} = 5.6$ cm, $\overline{BC} = 6$ cm and $\overline{CA} = 5$ cm. Draw its altitudes of the triangle & verify that these are concurrent.

Sol: Given $\overline{AB} = 5.6$ cm, $\overline{BC} = 6$ cm and $\overline{CA} = 5$ cm
 Required: Altitudes of a $\triangle ABC$ are concurrent.

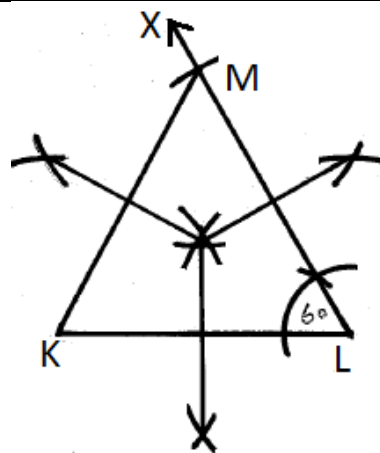


Steps of construction:

- i). Draw a line segment $\overline{BC} = 6$ cm
- ii). At point B draw an arc of radius 5.6cm
- iii). At point C Draw an arc of radius 5cm which intersect at A.
- iv). $\triangle ABC$ is constructed
- v). Draw perpendiculars from A to \overline{BC} , B to \overline{CA} & C to \overline{AB}
- vi). \overline{AD} , \overline{BE} & \overline{CF} are altitudes. These altitudes passes through the same point. thus altitudes of a triangle are concurrent.

Example 8: Construct $\triangle KLM$ whose $\overline{KL} = 5.8$ cm, $\overline{LM} = 6$ cm & $m\angle L = 60^\circ$. Draw its Right bisectors and verify their concurrency.

Sol: Given $\overline{KL} = 5.8$ cm, $\overline{LM} = 6$ cm & $m\angle L = 60^\circ$
 Required: Right bisectors of a $\triangle ABC$ are concurrent.



Steps of construction:

- i). Draw a line segment $\overline{KL} = 5.8$ cm
- ii). At point L draw an angle $m\angle K LX = 60^\circ$
- iii). At point L Draw an arc of radius 6cm which intersect the ray \overline{LX} at M.
- iv). Join K to M. $\triangle KLM$ is constructed
- v). Draw perpendiculars Bisectors of the sides \overline{KL} , \overline{LM} & \overline{MK} These right bisectors passes through the same point. thus right bisectors of a triangle are concurrent.

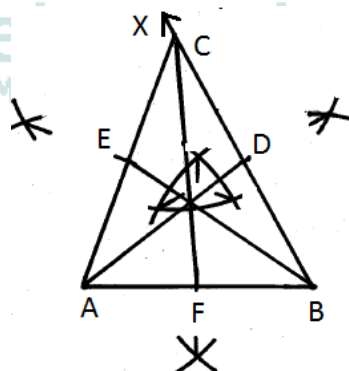
Example 9: Construct $\triangle ABC$ whose $\overline{AB} = 6$ cm, $m\angle A = 70^\circ$ & $m\angle C = 50^\circ$. Draw its medians and verify their concurrency.

Sol: Given $\overline{AB} = 6$ cm, $m\angle A = 70^\circ$ & $m\angle C = 50^\circ$
 Required: medians of $\triangle ABC$ are concurrent. First find

$$m\angle A + m\angle B + m\angle C = 180^\circ$$

$$70^\circ + m\angle B + 50^\circ = 180^\circ$$

$$m\angle B = 180^\circ - 70^\circ - 50^\circ = 60^\circ$$



Steps of construction:

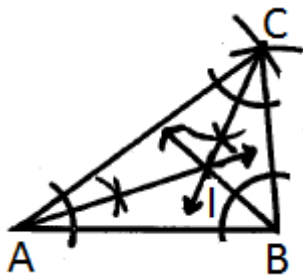
- i). Draw a line segment $\overline{AB} = 6$ cm
- ii). At point B draw an angle $m\angle ABX = 60^\circ$
- iii). At point A Draw an angle $m\angle A = 70^\circ$
- iv). $\triangle ABC$ is constructed
- v). By method of right bisectors of the side we find the mid points D,E & F of the sides of triangle
- vi). By joining A to D, B to E & C to F medians are constructed these medians passes through the same point. thus medians of a triangle are concurrent.

Exercise 17.2

Q1: i). Construct $\triangle ABC$ whose $\overline{AB} = 4.5$ cm, $\overline{BC} = 3.1$ cm & $\overline{CA} = 5.2$ cm. Draw angle bisectors of the triangle & verify their concurrency.

Sol: Given $\overline{AB} = 4.5$ cm, $\overline{BC} = 3.1$ cm & $\overline{CA} = 5.2$ cm

Required: Angle bisectors of a $\triangle ABC$ are concurrent.



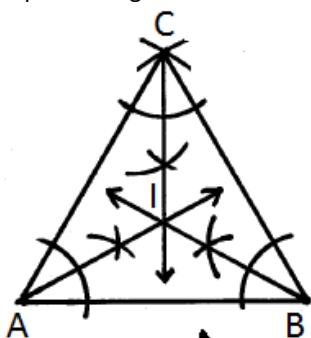
Steps of construction:

- i). Draw a line segment $\overline{AB} = 4.5$ cm
- ii). At point A draw an arc of radius 5.2cm
- iii). At point B Draw an arc of radius 3.1cm which intersect at C.
- iv). Join C to A & B. $\triangle ABC$ is constructed
- v). Draw bisectors of angles A,B & C. these bisectors passes through the same point I. thus angle bisectors of a triangle are concurrent.

Q1: ii). Construct \triangle whose $\overline{AB} = \overline{BC} = \overline{CA} = 12$ cm. Draw angle bisectors of the triangle & verify their concurrency.

Sol: Given $\overline{AB} = \overline{BC} = \overline{CA} = 12$ cm

Required: Angle bisectors of a $\triangle ABC$ are concurrent.



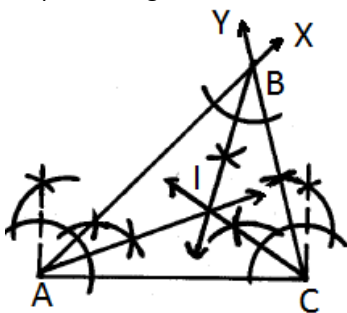
Steps of construction:

- i). Draw a line segment $\overline{AB} = 12$ cm
- ii). At point A draw an arc of radius 12cm
- iii). At point B Draw an arc of radius 12cm which intersect at C.
- iv). Join C to A and B, $\triangle ABC$ is constructed
- v). Draw bisectors of angles A,B & C. these bisectors passes through the same point I. thus angle bisectors of a triangle are concurrent.

Q1: iii) Construct $\triangle ABC$ whose $m\angle A = 45^\circ$, $m\angle C = 75^\circ$ & $\overline{CA} = 5.8$ cm. Draw angle bisectors of the triangle & verify their concurrency.

Sol: Given $m\angle A = 45^\circ$, $m\angle C = 75^\circ$ & $\overline{CA} = 5.8$ cm

Required: Angle bisectors of a $\triangle ABC$ are concurrent.



Steps of construction:

- i). Draw a line segment $\overline{CA} = 5.8$ cm
- ii). At point A draw an angle $m\angle CAX = 45^\circ$

iii). At point C Draw an angle $m\angle ACY = 75^\circ$

which intersect the ray \overline{AX} at B

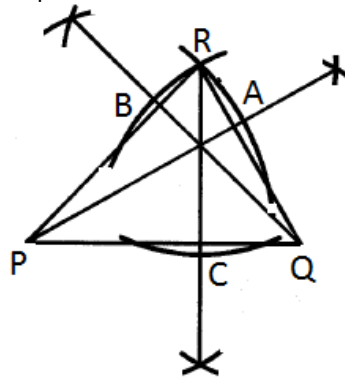
iv). $\triangle ABC$ is constructed

v). Draw bisectors of angles A,B & C. these bisectors passes through the same point I. thus angle bisectors of a triangle are concurrent.

Q2: i). Construct $\triangle PQR$ whose $\overline{PQ} = 6$ cm, $\overline{QR} = 4.5$ cm and $\overline{PR} = 5.5$ cm. Draw its altitudes of the triangle & verify their concurrency.

Sol: Given $\overline{PQ} = 6$ cm, $\overline{QR} = 4.5$ cm & $\overline{PR} = 5.5$ cm

Required: Altitudes of a $\triangle PQR$ are concurrent.



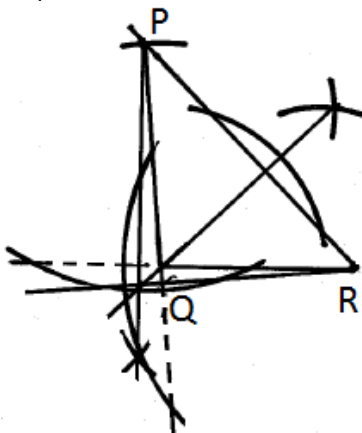
Steps of construction:

- i). Draw a line segment $\overline{PQ} = 6$ cm
- ii). At point P draw an arc of radius 5.5cm
- iii). At point Q Draw an arc of radius 4.5cm which intersect at R.
- iv). Join R to P and Q. $\triangle PQR$ is constructed
- v). Draw perpendiculars from P to \overline{QR} , Q to \overline{PR} & R to \overline{PQ} these altitudes \overline{PA} , \overline{QB} & \overline{RC} passes through the same point. thus altitudes of a triangle are concurrent.

Q2: ii). Construct $\triangle PQR$ whose $\overline{PQ} = 4.5$ cm, $\overline{QR} = 3.9$ cm & $m\angle R = 45^\circ$. Draw its altitudes of the triangle & verify their concurrency.

Sol: Given $\overline{PQ} = 4.5$ cm, $\overline{QR} = 3.9$ cm & $m\angle R = 45^\circ$

Required: Altitudes of a $\triangle PQR$ are concurrent.



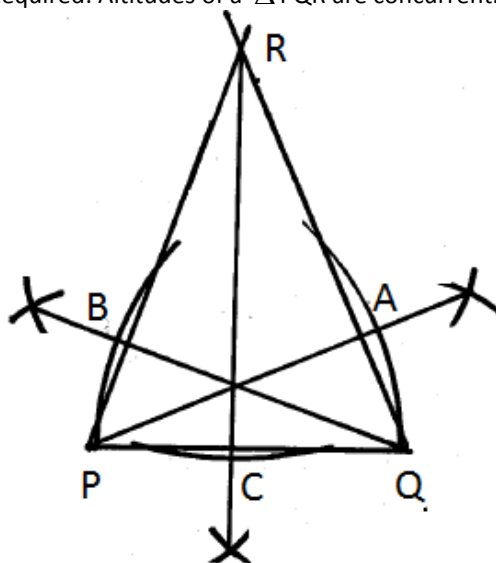
Steps of construction:

- i). Draw a line segment $\overline{QR} = 3.9$ cm
- ii). At point R draw an angle $m\angle R = 45^\circ$
- iii). At point Q Draw an arc of radius 4.5cm which intersect at P.
- iv). Join P to Q. $\triangle PQR$ is constructed

v). Draw perpendiculars from P to \overline{QR} , Q to \overline{PR} & R to \overline{PQ} these altitudes same point. thus altitudes of a triangle are concurrent.

Q2: iii). Construct ΔPQR whose $\overline{PQ} = 6\text{cm}$, $m\angle P = 70^\circ$ & $m\angle Q = 65^\circ$. Draw its altitudes of the triangle & verify that these are concurrent.

Sol: Given $\overline{PQ} = 6\text{cm}$, $m\angle P = 70^\circ$ & $m\angle Q = 65^\circ$
 Required: Altitudes of a ΔPQR are concurrent.

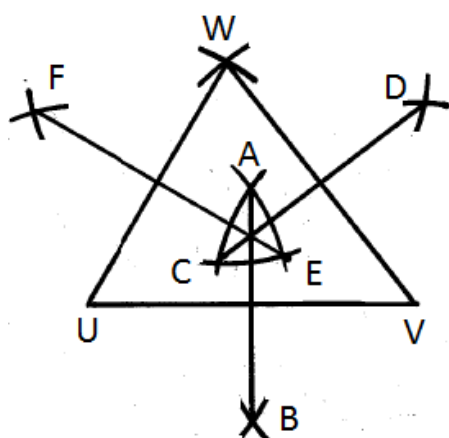


Steps of construction:

- i). Draw a line segment $\overline{PQ} = 6\text{ cm}$
- ii). At point P draw an angle $m\angle P = 70^\circ$
- iii). At point Q Draw an angle $m\angle Q = 65^\circ$ which intersect at R.
- iv). ΔPQR is constructed
- v). Draw perpendiculars from P to \overline{QR} , Q to \overline{PR} & R to \overline{PQ} these altitudes \overline{PA} , \overline{QB} & \overline{RC} passes through the same point. thus altitudes of a triangle are concurrent.

Q3: i). Construct ΔUVW whose $\overline{UV} = 7\text{cm}$, $\overline{VW} = 6.5\text{cm}$ & $\overline{WU} = 5.8\text{cm}$. Draw its perpendicular bisectors and & verify their concurrency.

Sol: Given $\overline{UV} = 7\text{cm}$, $\overline{VW} = 6.5\text{cm}$ & $\overline{WU} = 5.8\text{cm}$
 Required: Perpendicular bisectors are concurrent



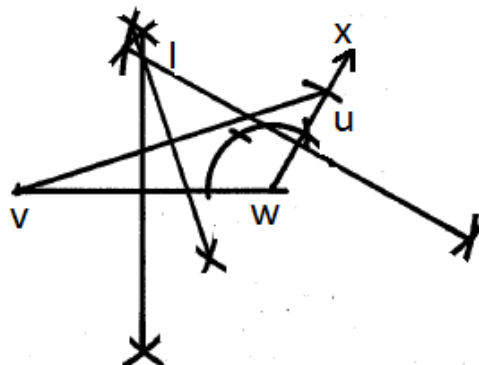
Steps of construction:

- i). Draw a line segment $\overline{UV} = 7\text{cm}$
- ii). At point V draw an arc of radius $\overline{VW} = 6.5\text{cm}$
- iii). At point U Draw an arc of radius $\overline{WU} = 5.8\text{cm}$

iv). Join W to U & V. ΔUVW is constructed
 v). Draw perpendiculars Bisectors of the sides \overline{UV} , \overline{VW} & \overline{UW} These right bisectors passes through the same point. Thus right bisectors of a triangle are concurrent.

Q3: ii). Construct ΔUVW whose $\overline{VW} = 10\text{cm}$, $\overline{WU} = 4.2\text{cm}$ & $m\angle W = 120^\circ$. Draw its Right bisectors & verify their concurrency.

Sol: Given $\overline{VW} = 10\text{cm}$, $\overline{WU} = 4.2\text{cm}$ & $m\angle W = 120^\circ$
 Required: Perpendicular bisectors are concurrent

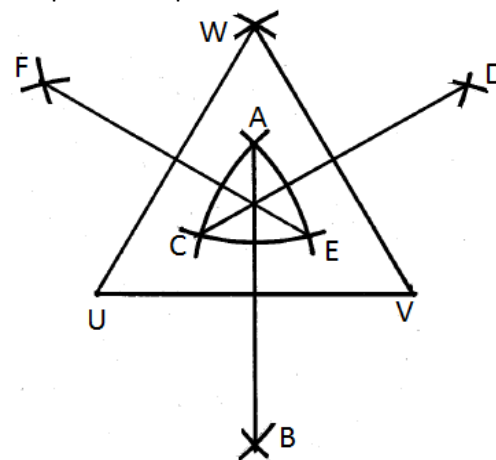


Steps of construction:

- i). Draw a line segment $\overline{VW} = 10\text{cm}$
- ii). At point W draw an angle $m\angle W = 120^\circ$
- iii). At point W Draw an arc of radius 4.2cm
- iv). Join V to U. ΔUVW is constructed
- v). Draw perpendiculars Bisectors of the sides \overline{UV} , \overline{VW} & \overline{UW} These right bisectors passes through the same point. Thus right bisectors of a triangle are concurrent.

Q3: iii). Construct ΔUVW whose $\overline{UV} = \overline{VW} = \overline{WU} = 0.8\text{dm}$. Draw its perpendicular bisectors and & verify their concurrency.

Sol: Given $\overline{UV} = \overline{VW} = \overline{WU} = 0.8\text{dm} = 8\text{cm}$
 Required: Perpendicular bisectors are concurrent



Steps of construction:

- i). Draw a line segment $\overline{UV} = 8\text{cm}$
- ii). At point U Draw an arc of radius 8cm
- iii). At point V Draw an arc of radius 8cm which intersect at W
- iv). Join W to V & U. ΔUVW is constructed
- v). Draw perpendiculars Bisectors of the sides \overline{UV} , \overline{VW} & \overline{UW} These right bisectors passes through the same point. Thus right bisectors of a triangle are concurrent.

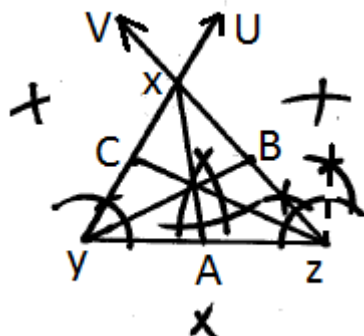
Q4: i). Construct $\triangle XYZ$ whose $\overline{YZ} = 4.1\text{cm}$, $m\angle Y = 60^\circ$ & $m\angle X = 75^\circ$. Draw their medians and verify their concurrency.

Sol: Given $\overline{YZ} = 4.1\text{cm}$, $m\angle Y = 60^\circ$ & $m\angle X = 75^\circ$
 Required: Medians are concurrent

$$m\angle X + m\angle Y + m\angle Z = 180^\circ$$

$$75^\circ + 60^\circ + m\angle Z = 180^\circ$$

$$m\angle Z = 180^\circ - 75^\circ - 60^\circ = 45^\circ$$



Steps of construction:

- i). Draw a line segment $\overline{YZ} = 4.1\text{cm}$
- ii). At point Y draw an angle $m\angle ZYU = 60^\circ$
- iii). At point Z Draw an angle $m\angle YZV = 45^\circ$
- iv). $\triangle XYZ$ is constructed
- v). By method of right bisectors of the side we find the mid points A, B & C of the sides of triangle
- vi). By joining A to X, B to Y & C to Z medians are constructed these medians passes through the same point. thus medians of a triangle are concurrent.

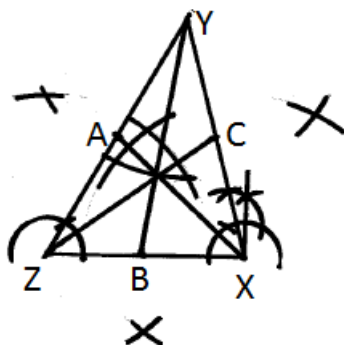
Q4: ii). Construct $\triangle XYZ$ whose $\overline{ZX} = 4.3\text{cm}$, $m\angle Y = 45^\circ$ & $m\angle X = 75^\circ$. Draw their medians and verify their concurrency.

Sol: Given $\overline{ZX} = 4.3\text{cm}$, $m\angle Y = 45^\circ$, $m\angle X = 75^\circ$
 Required: Medians are concurrent, First find

$$m\angle X + m\angle Y + m\angle Z = 180^\circ$$

$$75^\circ + 45^\circ + m\angle Z = 180^\circ$$

$$m\angle Z = 180^\circ - 75^\circ - 45^\circ = 60^\circ$$

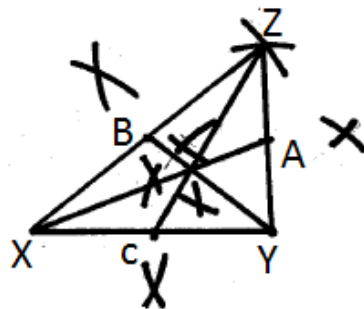


Steps of construction:

- i). Draw a line segment $\overline{ZX} = 4.3\text{cm}$
- ii). At point X draw an angle $m\angle X = 75^\circ$
- iii). At point Z Draw an angle $m\angle Z = 60^\circ$
- iv). $\triangle XYZ$ is constructed
- v). By method of right bisectors of the side we find the mid points A, B & C of the sides of triangle
- vi). By joining A to X, B to Y & C to Z medians are constructed these medians passes through the same point. thus medians of a triangle are concurrent.

Q4: iii). Construct $\triangle XYZ$ whose $\overline{XY} = 4.5\text{cm}$, $\overline{YZ} = 3.4\text{cm}$ & $\overline{ZX} = 5.6\text{cm}$. Draw their medians and verify their concurrency.

Sol: Given $\overline{XY} = 4.5\text{cm}$, $\overline{YZ} = 3.4\text{cm}$ & $\overline{ZX} = 5.6\text{cm}$
 Required: Medians are concurrent



Steps of construction:

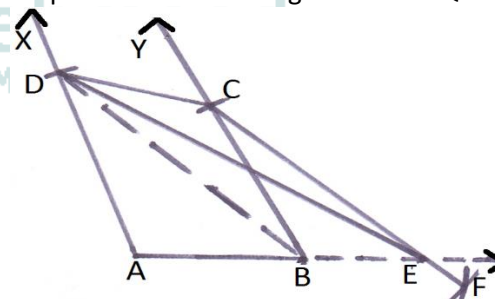
- i). Draw a line segment $\overline{XY} = 4.5\text{cm}$
- ii). At point X draw an arc of radius 5.6cm
- iii). At point Y Draw an arc of radius 3.4cm which intersect at Z.
- iv). Join Z to X & Y. $\triangle XYZ$ is constructed
- v). By method of right bisectors of the side we find the mid points A, B & C of the sides of triangle
- vi). By joining A to X, B to Y & C to Z medians are constructed these medians passes through the same point. thus medians of a triangle are concurrent.

Exercise 17.3

Q1: Draw a quadrilateral ABCD, such that $m\overline{AB} = 3\text{cm}$, $m\overline{BC} = 3.5\text{cm}$, $m\overline{AD} = 4\text{cm}$, $m\angle B = 60^\circ$, $m\angle A = 110^\circ$. Construct a triangle equal in area to quadrilateral.

Sol: Given $m\overline{AB} = 3\text{cm}$, $m\angle B = 60^\circ$, $m\angle A = 110^\circ$, $m\overline{BC} = 3.5\text{cm}$, $m\overline{AD} = 4\text{cm}$

Required: Area of Triangle = Area of Quadrilateral



Steps of construction:

- i). Draw a line segment $m\overline{AB} = 3\text{cm}$
- ii). At point B construct an angle $m\angle ABY = 60^\circ$
- iii). At point A construct an angle $m\angle BAX = 110^\circ$
- iv). At D draw an arc of radius 4cm which intersect the ray \overline{AX} at D and at B draw an arc of radius 3.5cm which intersect the ray \overline{BY} at C, Join C to D
- v). quadrilateral ABCD is constructed.
- vi). Join B to D with dotted line
- vii). At C draw an arc of radius = \overline{BD} , at B draw another arc of radius = \overline{CD} which intersects at F. Join C to F to get $\overline{BD} \parallel \overline{CF}$ to meet \overline{AB} at E
- viii). Join D to E we get required triangle \therefore area of quadrilateral = area of triangle

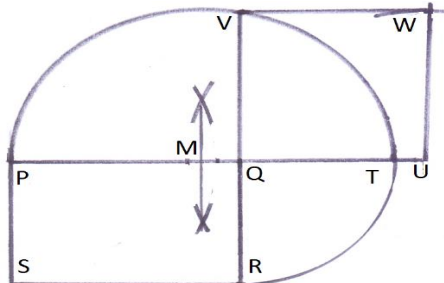
Q2: Draw a rectangle PQRS such that $m\overline{PQ} = 5\text{cm}$ and $m\overline{QR} = 3.5\text{cm}$ construct a square equal in area to the rectangle PQRS

Chapter 17

Sol: Given adjacent sides of rectangle

$$m\overline{PQ} = 5\text{cm} \text{ and } m\overline{QR} = 3.5\text{cm}$$

Required: Area of rectangle = Area of square



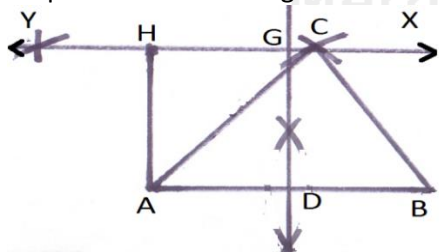
Steps of construction.

- i). Draw a line segment $m\overline{SR} = 5\text{cm}$
 - ii). At point S and R draw an angle of 90°
 - iii). At R and S draw an arc of radius 3.5cm which intersect at P and Q.
 - iv). By Joining P to Q. Rectangle PQRS is constructed
 - v). At Q draw arc of radius QR which intersect \overline{PQ} at T
 - vi). Draw right bisector of \overline{PT} which intersect at M
 - vii). At M draw a semi-circle which intersect \overline{QR} at V
 - viii). At Q draw an arc of radius QV which intersect \overline{PQ} at U, similarly at U and V which intersects at W
- \therefore Area of rectangle PQRS = Area of Square QUVW

Q3: Draw a triangle ABC such that $m\overline{AB} = 5\text{cm}$
 $m\overline{BC} = 4\text{cm}$ and $m\overline{CA} = 4.5\text{cm}$ Construct a rectangle equal in area to the given triangle

Sol: Given $m\overline{AB} = 5\text{cm}$ $m\overline{BC} = 4\text{cm}$ & $m\overline{CA} = 4.5\text{cm}$

Required: Area of triangle = Area of rectangle



Steps of constructions

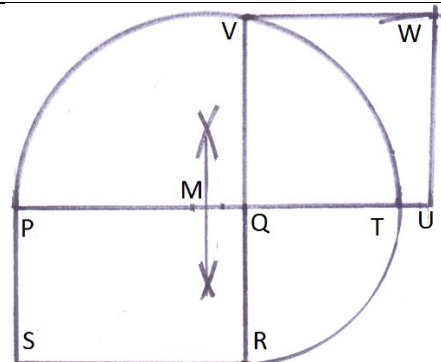
- i). Draw a line segment $m\overline{AB} = 5\text{cm}$
- ii). At B and A draw an arc of radius 4cm & at A draw an arc of radius 4.5cm which intersects at C
- iii). Join C to A and B, i.e. $\triangle ABC$ is formed
- iv). At C draw an arc of radius 5cm which cuts at Y
- v). Join C to Y and extended to get $\overline{AB} \parallel \overline{XY}$
- vi). Draw right bisector of AB which passes through D and intersect XY at G
- vii). At G draw an arc of radius AD which intersects \overline{XY} at H. Join A to H

\therefore Area of triangle ABC = area of rectangle ADGH

Q4. Construct a square having area equal to the given rectangle.

Sol: Let adjacent sides of rectangle $m\overline{PQ} = 5\text{cm}$
 and $m\overline{QR} = 3.5\text{cm}$

Required: Area of rectangle = Area of square



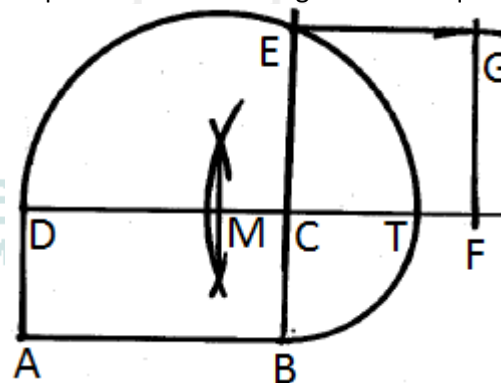
Steps of construction.

- i). Draw a line segment $m\overline{SR} = 5\text{cm}$
 - ii). At point S and R draw an angle of 90°
 - iii). At R and S draw an arc of radius 3.5cm which intersect at P and Q.
 - iv). By Joining P to Q. Rectangle PQRS is constructed
 - v). At Q draw arc of radius QR which intersect \overline{PQ} at T
 - vi). Draw right bisector of \overline{PT} which intersect at M
 - vii). At M draw a semi-circle which intersect \overline{QR} at V
 - viii). At Q draw an arc of radius QV which intersect \overline{PQ} at U, similarly at U and V which intersects at W
- \therefore Area of rectangle PQRS = Area of Square QUVW

Q5. Construct a square equal in area to a rectangle whose adjacent side are 4.5cm and 2.2cm respectively. Measure the sides of square and find its area and compare with the rectangle.

Sol: Given adjacent sides of rectangle are 4.5cm & 2.2cm

Required: area of rectangle = area of square



Steps of construction.

- i). Draw a line segment $m\overline{AB} = 4.5\text{cm}$
 - ii). At point A and B draw an angle of 90°
 - iii). At A and B draw an arc of radius 2.2cm which intersect at C and D.
 - iv). By Joining C to D. Rectangle ABCD is constructed
 - v). At C draw arc of radius BC which intersect \overline{DC} at T
 - vi). Draw right bisector of \overline{DT} which intersect at M
 - vii). At M draw a semi-circle which intersect \overline{BC} at E
 - viii). At C draw arc of radius CE which intersect \overline{DC} at F, similarly at C and E draw arc which intersects at G
- \therefore Area of rectangle ABCD = Area of Square CFGE

$$m\overline{AB} \times m\overline{BC} = (m\overline{CF})^2$$

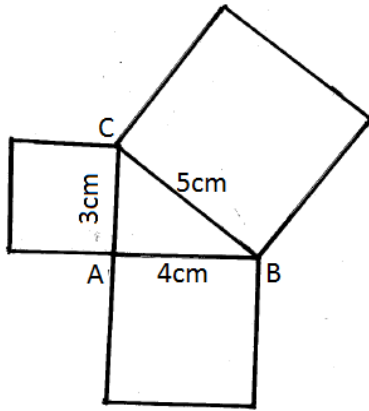
$$4.5\text{cm} \times 2.2\text{cm} = (3.15\text{cm})^2$$

$$9.9\text{cm}^2 = 9.9\text{cm}^2$$

Q6. Construct a square equal in area in the sum of two square having sides 3cm and 4cm respectively.

Sol: Given squares having sides 3cm and 4cm

Required: Make a new square whose are equal to area of given square

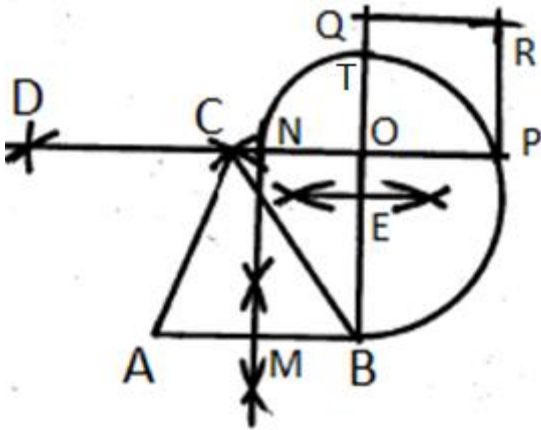


Steps of construction:

- i). Draw a line segment $\overline{AB} = 4\text{cm}$
 - ii). At A draw an arc of radius 3cm
 - iii). At B draw an arc of radius 5cm which intersect at C.
 - iv) draw square on each side of triangle
- Hence

$$\begin{aligned} \text{Sum of square of the sides} &= \text{square of the hypotenuse} \\ 4^2 + 3^2 &= 5^2 \\ 16 + 9 &= 25 \\ 25 &= 25 \end{aligned}$$

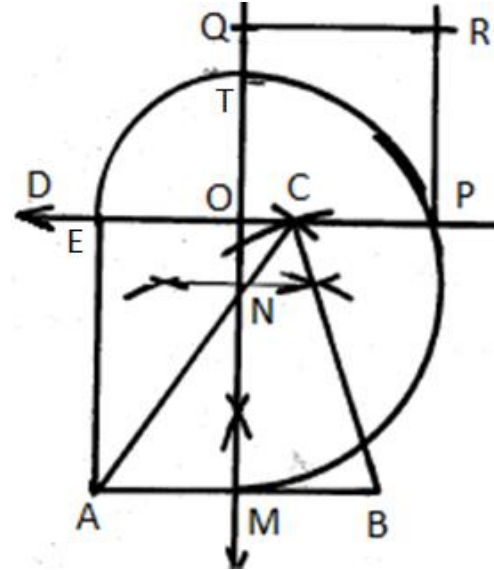
Q7. Construct a triangle having base 3.5cm and other two sides equal to 3.4cm and 3.8cm respectively. transform it into an equal square.



Steps of constructions

- i). Draw a line segment $m\overline{AB} = 3.5\text{cm}$
 - ii). At B and A draw an arc of radius 3.8cm & at A draw an arc of radius 3.4cm which intersects at C
 - iii). Join C to A and B, i.e. $\triangle ABC$ is formed
 - iv). At C draw an arc of radius 3.5cm which cuts at D
 - v). Join C to D and extended to get $\overline{AB} \parallel \overline{CD}$
 - vi). Draw right bisector of AB which passes through M and intersect CD at N
 - vii). At N draw an arc of radius AM which intersects CD at O. Join O to B
 - viii). At O draw arc of radius ON which cut \overline{OB} at T
 - ix). Draw right bisector of \overline{BT} which intersect at E
 - x). At E draw a semi-circle which intersect \overline{CD} at P
 - xi). At O draw an arc of radius OP which cut \overline{OB} at Q, similarly at P and Q draw an arc which cut at R
- \therefore Area of triangle ABC = Area of Square OPWQ

Q8. Construct a triangle having base 5cm and other sides equal to 5cm and 6cm. also construct a square equal in area to the given triangle.



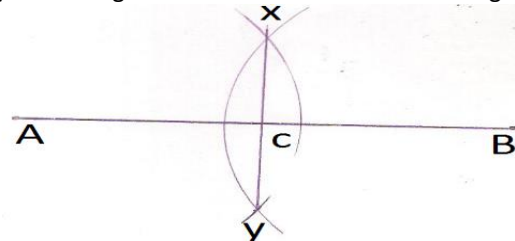
Steps of constructions

- i). Draw a line segment $m\overline{AB} = 5\text{cm}$
 - ii). At B and A draw an arc of radius 5cm & at A draw an arc of radius 6cm which intersects at C
 - iii). Join C to A and B, i.e. $\triangle ABC$ is formed
 - iv). At C draw an arc of radius 5cm which cuts at D
 - v). Join C to D and extended to get $\overline{AB} \parallel \overline{CD}$
 - vi). Draw right bisector of AB which passes through M and intersect CD at O
 - vii). At O draw an arc of radius AM which intersects CD at E. Join A to E
 - viii). At O draw arc of radius OE which cut \overline{OM} at T
 - ix). Draw right bisector of \overline{MT} which intersect at N
 - x). At N draw a semi-circle of radius MN which cut \overline{CD} at P
 - xi). At O draw an arc of radius OP which cut \overline{OM} at Q, similarly at P and Q draw an arc which cut at R
- \therefore Area of triangle ABC = Area of Square OPWQ

Review Exercise 17

Q1: Select the correct answer.

- i). What is first step in constructing an angle bisector
 - a). Draw a ray
 - b). Measure the line
 - c). label the point of intersection
 - d). Place the compass point on the vertex
- ii). What is geometric construction shown in figure

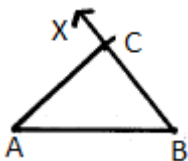


- a). A line parallel to a given line
 - b). An angle congruent to a given angle
 - c). An angle bisector
 - d). A perpendicular bisector
- iii). A line segment joining the midpoint of one side of a triangle to its opposite vertex is called
- a). Right bisector
 - b). Median
 - c). Altitude
 - d). Angle bisector

Chapter 17

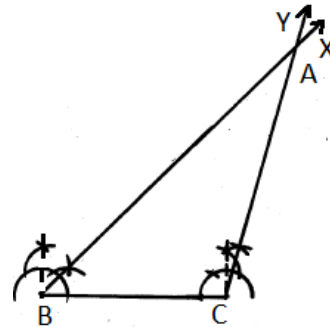
- iv). You are looking at a triangle orthocenter, centroid and circumcenter are all the same point. What type of triangle are you looking at?
 a). Scalene b). Isosceles
 c). Equilateral d). Right angled
- v). The centroid of a triangle divides the medians into the ratio of
 a). 2:1 b). 3:1
 c). 4:1 d). 5:1
- vi). The centroid of a triangle divides the median into the ratio of
 a). 2:1 b). 3:1
 c). 4:1 d). 5:1
- vii). A line which is perpendicular to a line segment at its midpoint is called a/an
 a). Right bisector b). Median
 c). Altitude d). Angle bisector
- viii). The point of intersection of the bisectors of the angles of a triangle is equidistant from the Of the triangle
 a). Vertices b). Sides
 c). Altitudes d). Medians
- ix). Altitude of a triangle are
 a). equal in length b). concurrent
 c). equidistant from the vertices
 d). Perpendicular bisector
- x). If Measure of three angles of a triangle are known how many triangles can be constructed?
 a). Only one triangle b). Two triangles
 c). No Triangle d). Infinite triangles
- xi). the point of intersection of the perpendicular bisectors of the sides of a triangle is equidistant from the Of the triangle.
 a). Altitude b). Medians
 c). Sides d). Vertex

Q2. Construct $\triangle ABC$ such that $\overline{AB} = 3.7\text{cm}$, $\overline{BC} = 2.5\text{cm}$ and $m\angle B = 50^\circ$
 Sol: Given $\overline{AB} = 3.7\text{cm}$, $\overline{BC} = 2.5\text{cm}$, $m\angle B = 50^\circ$
 Required: Construct triangle ABC



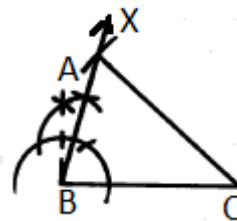
Step of construction:
 i). Draw a line segment $\overline{AB} = 3.7\text{cm}$
 ii). At point B draw an angle $m\angle ABX = 50^\circ$
 iii). At Point B draw an arc of radius 2.5cm which cuts at C
 iv). Join A to C.
 v). $\triangle ABC$ is constructed

Q3. Construct $\triangle ABC$ such that $\overline{BC} = 5.8\text{cm}$, $m\angle A = 30^\circ$ and $m\angle B = 45^\circ$
 Sol: Given $\overline{BC} = 5.8\text{cm}$, $m\angle A = 30^\circ$, $m\angle B = 45^\circ$
 Required: Construct Triangle ABC
 $m\angle A + m\angle B + m\angle C = 180^\circ$
 $30^\circ + 45^\circ + m\angle C = 180^\circ$
 $m\angle C = 180^\circ - 30^\circ - 45^\circ = 105^\circ$



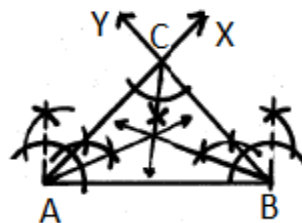
Step of construction:
 i). Draw a line segment $\overline{BC} = 5.8\text{cm}$
 ii). At point B draw an angle $m\angle CBX = 45^\circ$
 iii). At point C draw an angle $m\angle BCY = 105^\circ$ which cuts at A
 iv). $\triangle ABC$ is constructed

Q4. Construct $\triangle ABC$ such that $\overline{AC} = 4.5\text{cm}$, $\overline{BC} = 4.1\text{cm}$ and $m\angle B = 75^\circ$
 Sol: Given $\overline{AC} = 4.5\text{cm}$, $\overline{BC} = 4.1\text{cm}$ & $m\angle B = 75^\circ$
 Required: Construct $\triangle ABC$



Step of construction:
 i). Draw a line segment $\overline{BC} = 4.1\text{cm}$
 ii). At point B draw an angle $m\angle CBX = 75^\circ$
 iii). At point C draw an arc of radius 4.5cm which cuts at A
 iv). $\triangle ABC$ is constructed

Q5. Construct $\triangle ABC$, Draw their angle bisectors and verify their concurrency when $\overline{AB} = 3.5\text{cm}$, $m\angle A = 45^\circ$ and $m\angle B = 45^\circ$
 Sol: Given $\overline{AB} = 3.5\text{cm}$, $m\angle A = 45^\circ$ & $m\angle B = 45^\circ$
 Required: Angles bisectors are concurrent.



Step of construction:
 i). Draw a line segment $\overline{AB} = 3.5\text{cm}$
 ii). At point A draw an angle $m\angle BAX = 45^\circ$
 iii). At point B draw an angle $m\angle ABY = 45^\circ$ which intersect at C
 iv). $\triangle ABC$ is constructed
 v). Draw angles bisectors of A,B,C which passes through the same point. Thus angle bisectors are concurrent.

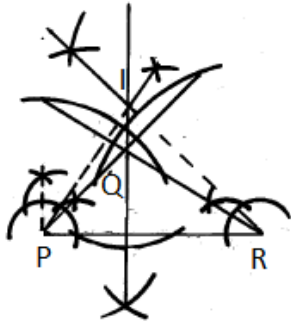
Q6. Construct $\triangle PQR$, Draw their altitudes and verify their concurrency when $\overline{PR} = 5.8\text{cm}$, $m\angle P = 45^\circ$ and $m\angle Q = 105^\circ$
 Sol: Given $\overline{PR} = 5.8\text{cm}$, $m\angle P = 45^\circ$, $m\angle Q = 105^\circ$
 Required: Altitudes of a triangle are concurrent

Chapter 17

$$m\angle P + m\angle Q + m\angle R = 180^\circ$$

$$45^\circ + 105^\circ + m\angle R = 180^\circ$$

$$m\angle R = 180^\circ - 45^\circ - 105^\circ = 30^\circ$$



Step of construction:

- i). Draw a line segment $\overline{PR} = 5.8\text{cm}$
- ii). At point P draw an angle $m\angle P = 45^\circ$
- iii). At point R draw an angle $m\angle R = 30^\circ$ which intersect at Q
- iv). ΔPQR is constructed
- v). Draw altitudes From P to QR, R to PQ & Q to PQ which intersect at the same point I. Thus altitudes of the ΔPQR are concurrent.

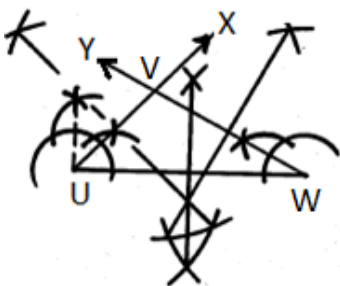
Q7. Construct ΔUVW , Draw their Perpendicular bisectors and verify their concurrency when $\overline{UW} = 5.8\text{cm}$, $m\angle U = 45^\circ$ and $m\angle V = 105^\circ$

Sol: Given $\overline{UW} = 5.8\text{cm}$, $m\angle U = 45^\circ$ & $m\angle V = 105^\circ$
 Required: Right bisector of the Δ are concurrent

$$m\angle U + m\angle V + m\angle W = 180^\circ$$

$$45^\circ + 105^\circ + m\angle W = 180^\circ$$

$$m\angle W = 180^\circ - 105^\circ - 45^\circ = 30^\circ$$



Step of construction:

- i). Draw a line segment $\overline{UW} = 5.8\text{cm}$
- ii). At point U draw an angle $m\angle WUX = 45^\circ$
- iii). At point W draw an angle $m\angle UWY = 30^\circ$ which intersect at V
- iv). ΔUVW is constructed
- v). Draw right bisectors of UV, VW & UW which intersect at the same point. Thus Right bisectors of the ΔPQR are concurrent.

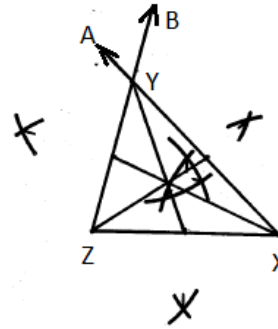
Q8. Construct ΔXYZ , Draw their medians and verify their concurrency when $\overline{ZX} = 6\text{cm}$, $m\angle Y = 60^\circ$ and $m\angle Z = 75^\circ$

Sol: Given $\overline{ZX} = 6\text{cm}$, $m\angle Y = 60^\circ$ & $m\angle Z = 75^\circ$
 Required: Medians of Δ are concurrent

$$m\angle X + m\angle Y + m\angle Z = 180^\circ$$

$$m\angle X + 60^\circ + 75^\circ = 180^\circ$$

$$m\angle X = 180^\circ - 75^\circ - 60^\circ = 45^\circ$$

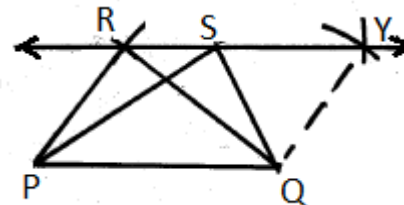


Step of construction:

- i). Draw a line segment $\overline{ZX} = 3.5\text{cm}$
- ii). At point Z draw an angle $m\angle XZB = 75^\circ$
- iii). At point X draw an angle $m\angle ZXA = 45^\circ$ which intersect at Y
- iv). ΔXYZ is constructed
- v). Find midpoint of ZX, XY & ZY and then joining the opposite vertex Y, Z & X which passes through same point. Thus Medians are concurrent.

Q4: Draw a triangle PQR such that $\overline{PQ} = 5.6\text{cm}$, $\overline{QR} = 4.5\text{cm}$ & $m\angle P = 34^\circ$ Construct a triangle SPQ equivalent in area to the triangle PQR.

Sol: Given $\overline{PQ} = 5.6\text{cm}$, $\overline{QR} = 4.5\text{cm}$, $m\angle P = 34^\circ$
 Required: Area of Triangle PQR = Area of Triangle PQS

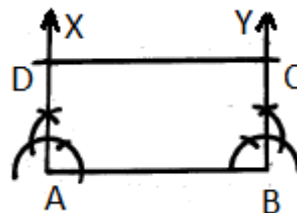


- i). Draw a line segment $m\overline{PQ} = 5.6\text{cm}$
- ii). At Q draw an arc radius 4.5cm and at P draw an arc of radius 3.4cm which intersects at R
- iii). Join R to P and Q, i.e. ΔPQR is formed
- iv). At Q draw an arc of radius 3.4cm and at R draw an arc of radius 5.6cm which intersects at Y. Join R to Y we get $\overline{PQ} \parallel \overline{RY}$

v). Take any point S on \overline{XY} and join to P and Q.

Q10: Construct a rectangle whose adjacent sides are 2.5cm & 5cm respectively.

Sol: Given adjacent sides of rectangle 2.5cm & 5cm
 Required: Draw a rectangle



Step of construction:

- i). Draw a line segment $\overline{AB} = 5\text{cm}$
- ii). At point A draw an angle $m\angle BAX = 90^\circ$
- iii). At point B draw an angle $m\angle ABY = 90^\circ$
- iv). Draw an arc of radius 2.5cm at A and B which cut at C and D
- v). Join C to D
- vi). Rectangle ABCD is constructed.