

**Q.1 Four possible answers to each statement are given below. Tick (✓) the correct answer**

(i) If  $n$  is a prime number, then  $\sqrt{n}$  is

- (a) Real number                      (b) Rational number      (c) Irrational number      (d) Complex number

(ii)  $p \wedge q$  represents

- (a) Disjunction                      (b) Conjunction              (c) Conditional              (d) Quantifier

(iii)  $(AB)^{-1} =$

- (a)  $AB$                                   (b)  $BA$                                   (c)  $A^{-1}B^{-1}$                       (d)  $B^{-1}A^{-1}$

(iv) A Homogenous system of linear equation has:

- (a) Finite Solution                      (b) Unique Solution              (c) Infinite Solution              (d) Two Solution

(v) Sum of four roots of unity is:

- (a) 1    (b) -1    (c) 0    (d) I

(vi) Equation having same solution is called:

- (a) Exponential equation      (b) Radical equation      (c) Simultaneous equation      (d) Reciprocal equation

(vii) The partial fraction of  $\frac{1}{(x^2-1)}$  are of type

- (a)  $\frac{A}{(x+1)} + \frac{B}{(x-1)}$               (b)  $\frac{A}{(x-1)} + \frac{B}{(x-1)^2}$               (c)  $\frac{A}{(x+1)} + \frac{B}{(x+1)^2}$               (d)  $\frac{A}{(x-1)} + \frac{B}{(x-1)}$

(viii) If in an A.P  $a_n = \frac{n}{2n+1}$ , then  $a_4$  is equal to:

- (a) 4    (b) 3    (c)  $\frac{4}{3}$     (d)  $\frac{4}{9}$

(ix) Geometric mean between 2 and 8 is:

- (a) 2    (b) 8    (c) 4    (d) 16

(x)  $\sum_{k=1}^n k =:$

- (a)  $nk$     (b)  $\frac{n(n+1)}{2}$     (c)  $\frac{k(k+1)}{2}$     (d)  $k^n$

(xi) If A and B are disjoint event, then  $P(A \cup B) =$

- (a)  $P(A) + P(B)$                       (b)  $P(A) + P(B) - P(A \cup B)$               (c)  $P(A) + P(B) - P(A \cap B)$               (d)  $P(A) - P(B)$

(xii)  $0!$  is equal to:

- (a) 0 (b) 1 (c) 10 (d) 100

(xiii) Expansion of  $(8 - 2x)^{-1}$  is valid if :

- (a)  $|x| > 4$  (b)  $|x| < 4$  (c)  $|x| = 0$  (d)  $|x| = 4$

(xiv)  $\theta^\circ$  is measured in:

- (a) Circular system (b) Sexagesimal system (c) Radian measure (d) Rotation measure

(xv) Sum of all angles in a triangle is equal to:

- (a)  $90^\circ$  (b)  $180^\circ$  (c)  $270^\circ$  (d)  $360^\circ$

(xvi) Period of  $\sin 3x$  is:

- (a)  $3\pi$  (b)  $2\pi$  (c)  $\frac{\pi}{3}$  (d)  $\frac{2\pi}{3}$

(xvii) Angle below the surface line is called angle of:

- (a) Right angle (b) Oblique angle (c) Depression (d) Elevation

(xviii) The greatest angle is opposite to:

- (a) Smallest side (b) Greatest side (c) Same side (d) Right side

(xix)  $\tan^{-1} A - \tan^{-1} B =$

- (a)  $\tan^{-1} \frac{AB}{1+AB}$  (b)  $\tan^{-1} \frac{A-B}{1+AB}$  (c)  $\tan^{-1} \frac{A-B}{1-AB}$  (d)  $\tan^{-1} \frac{AB}{1-AB}$

(xx) Equation, containing at least one trigonometric function is called:

- (a) Exponential equation (b) Partial equation  
(c) Trigonometric equation (d) General equation

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**Section – I**

**Note:** Write any Twenty-Five (25) short answers. While writing answer write its part number carefully.  
Each part carries two marks. 50

**Q # 1:**

- (i) Find the multiplicative inverse of  $(-4, -7)$
- (ii) Find modulus and conjugate of  $z = 1 - i\sqrt{3}$
- (iii) Explain set of natural number is neither monoid nor a group w.r.t “**t**”
- (iv) Define conjunction and disjunction of two statements  $p$  and  $q$
- (v) If  $A = \{1, 2, 3, 4, 5, \}$  and  $B = \{4, 5, 6, 7, 8, 9, \}$  then find  $A-B$  and  $B-A$
- (vi) If  $\begin{bmatrix} i & 0 \\ 1 & -i \end{bmatrix} = A$  show that  $A^{-1} = I_2$
- (vii) Define symmetric and hermitian matrix.
- (viii) If  $\begin{bmatrix} 2 & 5 & -1 \\ 3 & 4 & 2 \\ 1 & 2 & -2 \end{bmatrix}$  find  $|A|$
- (ix) Solve  $x^2 + 7x + 12 = 0$
- (x) Evaluate  $w^{28} + w^{29} + 1$
- (xi) Discuss the nature of roots of  $25x^2 - 30x + 9 = 0$
- (xii)  $\alpha, \beta$  are roots of  $5x^2 - x - 2 = 0$  form the equation whose roots are  $\frac{3}{\alpha}$  and  $\frac{3}{\beta}$
- (xiii) Find partial fraction of  $\frac{3x}{(x-1)(x+2)}$
- (xiv) Define conditional equation and improper rational fraction.
- (xv) If the  $n$ th term of the A.P is  $(3n - 1)$  find the A.P.?
- (xvi) Sum the series  $-3 + (-1) + 1 \dots$  upto 16 terms.
- (xvii) Find value of  $r$  if  $a_4 = \frac{8}{27}$  and  $a_7 = \frac{-64}{729}$  of a G.P.
- (xviii) Sum the series  $1 + 2x + 4x^2 + \dots \infty$
- (xix) Find two G.M's between 1 and 8
- (xx) Find 8<sup>th</sup> term of H.P.  $\frac{1}{2}, \frac{1}{5}, \frac{1}{8} \dots$
- (xxi) How many different 4 digit number can be formed out of the digit 1,2,3,4,5,6 when no digit is repeated?
- (xxii)  ${}^n C_{10} = \frac{12 \times 11}{2}$  find  $n$
- (xxiii) There are 5 green and 3 red balls in a box, one ball is taken out. What is probability that the ball is green?
- (xxiv) Find first three terms in the expansion of  $(\frac{a}{2} - \frac{2}{a})^6$  by using binomial theorem.
- (xxv) Neglecting square and higher powers of “ $x$ ” show that  $\frac{\sqrt{1+2x}}{\sqrt{1-x}} = 1 + \frac{3x}{2}$
- (xxvi) Show that the inequality  $4^n > 3^n + 4$  is true for  $n = 3, 4$
- (xxvii) Find  $r$  when  $l = 56cm. \theta = 45^\circ$

(xxviii)	$\sin \theta = -\frac{1}{\sqrt{2}}$ and terminal arm of the angle is not in Quadrant III, find values of $\tan \theta$ and $\cos \theta$
(xxix)	Prove that $\sin(\theta + \frac{\pi}{6}) + \cos(\theta + \frac{\pi}{3}) = \cos \theta$
(xxx)	Prove that $\sin 2\alpha = 2 \sin \alpha \cos \alpha$
(xxxi)	What is the range and domain of the cotangent function?
(xxxii)	At the top of a cliff 80m high, the angle of depression of a boat is $12^\circ$ . How far is the boat from the cliff?
(xxxiii)	If in a triangle ABC $\beta = 60^\circ, \gamma = 15^\circ, b = \sqrt{6}$ find a.
(xxxiv)	Show that $r_2 = s \tan(\frac{\beta}{2})$
(xxxv)	If sides of triangle ABC $a = 34, b = 20, c = 42$ find area of the triangle.
(xxxvi)	Find the value of $\tan\left(\sin^{-1}\left(\frac{-1}{2}\right)\right)$
(xxxvii)	Solve the equation $\cot^2 \theta = \frac{1}{3}$

### Section – II

*Note: Attempt any THREE questions.*

<b>Q # 3 (a)</b> Show that the set consisting of elements of the form $(a + \sqrt{3}b)$ ( $a, b$ are rationals) is an abelian group w.r.t addition.	5
<b>(b)</b> Solve the equation $\sqrt{x+8} + \sqrt{x+3} = \sqrt{12x+13}$	5
<b>Q # 4 (a)</b> Solve the system of linear equations $2x - y + z = 8, x + 2y + 2z = 6, x - 2y - z = 1$ by Cramer's rule.	5
<b>(b)</b> Find the values of $n$ and $r$ when ${}^{n-1}C_{r-1} : {}^nC_r : {}^{n+1}C_{r+1} = 3 : 6 : 11$	5
<b>Q # 5 (a)</b> Sum the series $3 + 5 - 7 + 9 + 11 - 13 + 15 + 17 - 19 + \dots$ to $3n$ terms.	5
<b>(b)</b> If $x$ is so small that its square and higher power by neglected, then show that	
$\frac{(9+7x)^{\frac{1}{2}} - (16+3x)^{\frac{1}{4}}}{4+5x} = \frac{1}{4} - \frac{17}{384}x$	5
<b>Q # 6 (a)</b> Draw the graph of $y = \sin(\frac{x}{2})$ for $x \in [0, 2\pi]$	5
<b>(b)</b> Express $\cos A + \cos 3A + \cos 5A + \cos 7A$ as a product.	5
<b>Q # 7 (a)</b> Solve the triangle ABC in which $a = 53, \beta = 88^\circ 36', \gamma = 31^\circ 54'$	5
<b>(b)</b> Prove that $r = \frac{\Delta}{s}$ with usual notations.	5

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